

Recent Developments in the Use of Satellite Observations in Numerical Weather Prediction:

Ocean Data Assimilation

Keith Haines

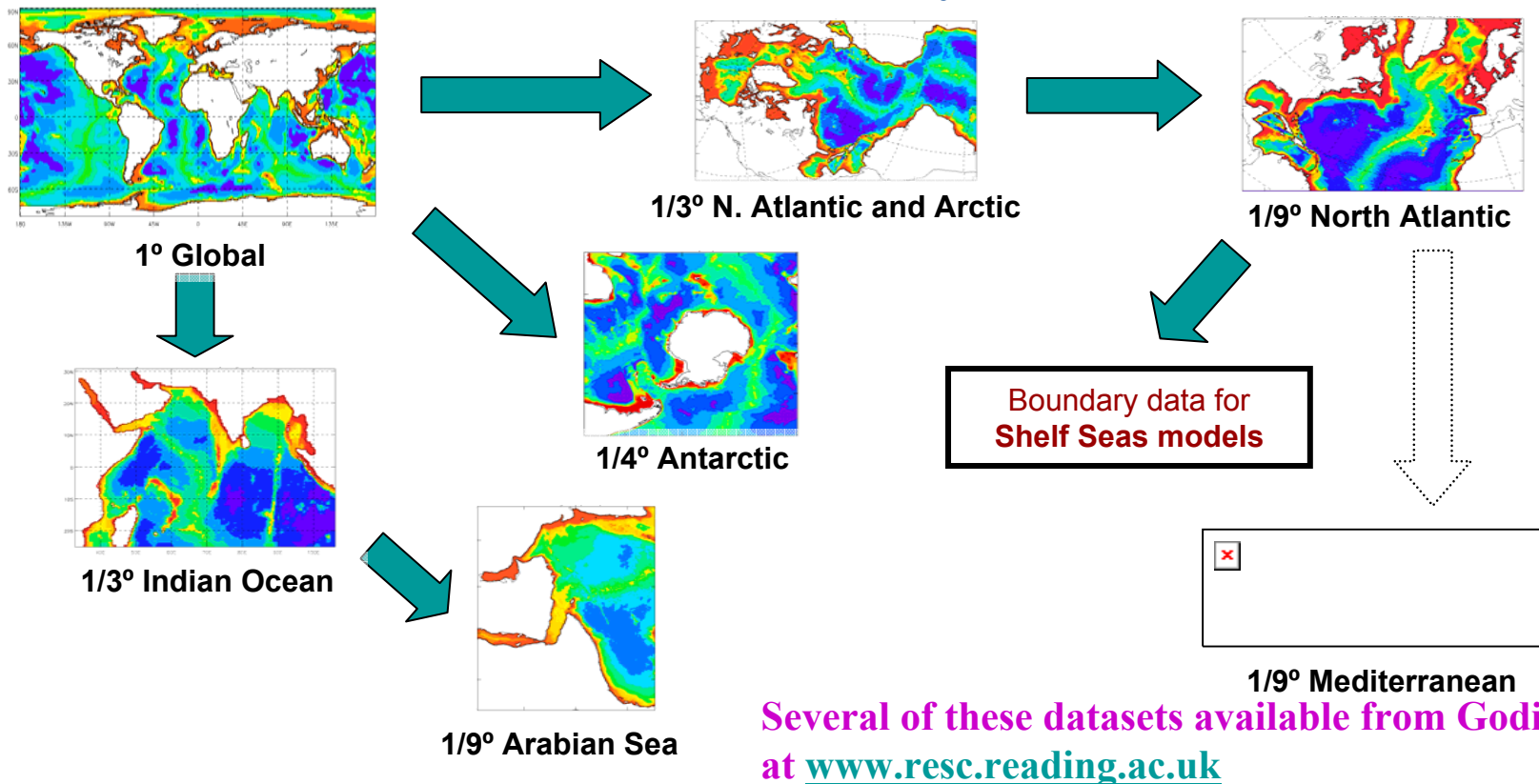
Environmental Systems Science Centre (ESSC),
Reading University

Topics

- Applications of Ocean DA
 - Operational Oceanography
 - Ocean Synthesis/Reanalysis
 - Seasonal – Interannual Forecasting (coupled models)
- Assimilation data sets
 - Altimeter sea level anomalies
 - The Geoid and the Mean Dynamic Topography
 - In Situ data, (T,S) and Argo
- Assimilation techniques
 - Bias treatment
 - State dependent covariances
 - Coupled model assimilation

Operational oceanography at the MetO

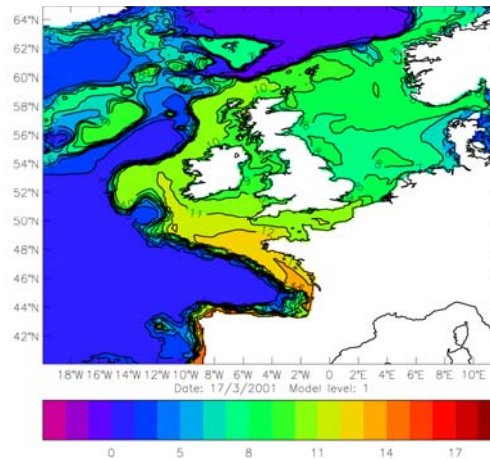
- Model resolution is key to capturing the dynamic processes
- All models in transition to NEMO (MetO will run $\frac{1}{4}$ global version)
- In Situ and **Altimeter** data sets are key for assimilation



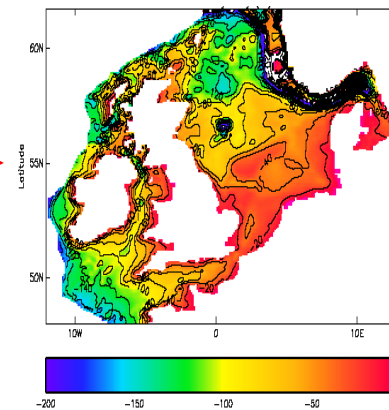
Shelf seas models at MetO

- State of the art model developed with POL
- Driven with Met Office Numerical Weather Prediction
- Can produce a range of output
 - tidal, met & density driven currents
 - temperature, salinity, seasonal stratification
- Forecasts of tidal currents and sea level elevation available years ahead, through NCOF
- Currently assimilation under research

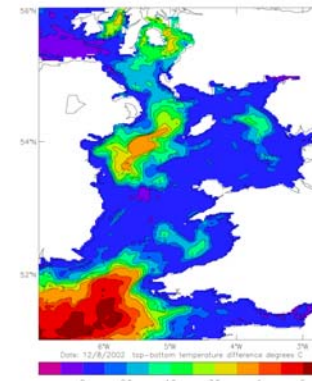
Atlantic Margin Model (AMM) – 12km Resolution



Medium Resolution Continental Shelf (MRCS) – 6km Resolution



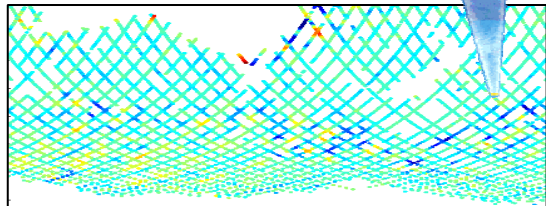
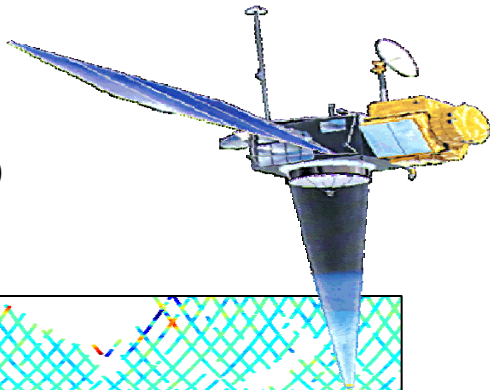
Irish Sea – 1.8km Resolution



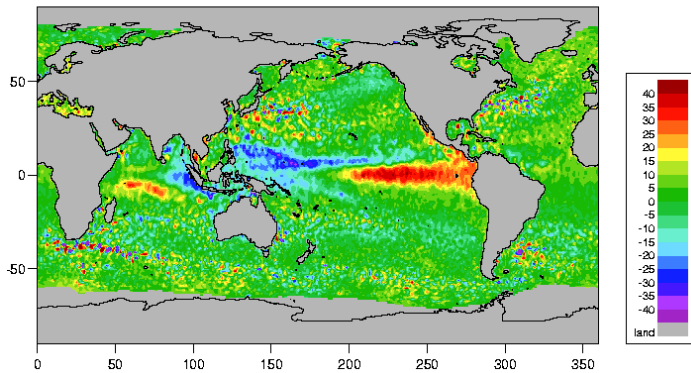
Key Data for Operational Oceanography

Altimetric Sea level **anomalies**

Repeat track
SSH= η
every 10 days
(Topex-Jason)

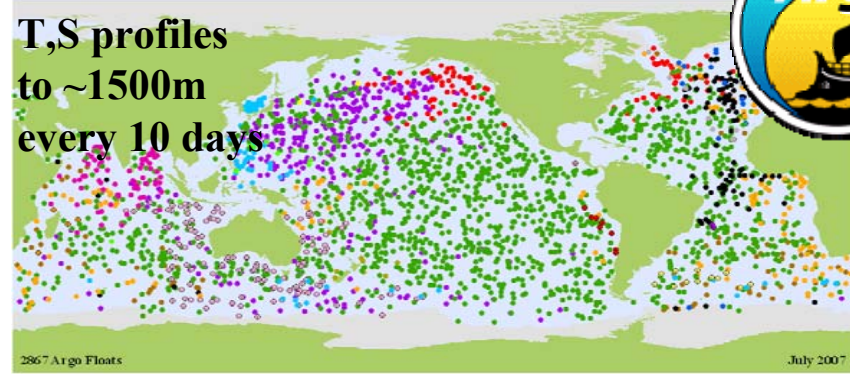


TOPEX + ERS2 sea surface height anomaly (cm). 25 November 1997.

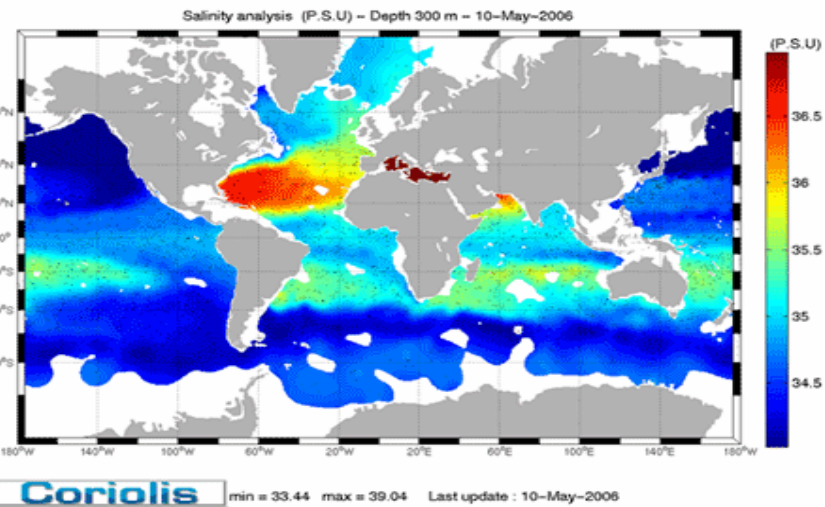


In Situ data from Argo and TAO

T,S profiles
to ~1500m
every 10 days



- 2967 Argo Floats
- ARGENTINA (12)
 - CHINA (2)
 - FRANCE (185)
 - JAPAN (271)
 - NETHERLANDS (10)
 - SPAIN (2)
 - AUSTRALIA (134)
 - CHINA (2)
 - GERMANY (123)
 - SOUTH KOREA (16)
 - NEW ZEALAND (3)
 - UNITED KINGDOM (8)
 - BRAZIL (2)
 - COSTA RICA (1)
 - INDIA (75)
 - MAURITIUS (4)
 - NORWAY (8)
 - UNITED STATES (1610)
 - CANADA (97)
 - EUROPEAN UNION (29)
 - IRELAND (0)
 - MEXICO (1)
 - RUSSIAN FEDERATION (2)



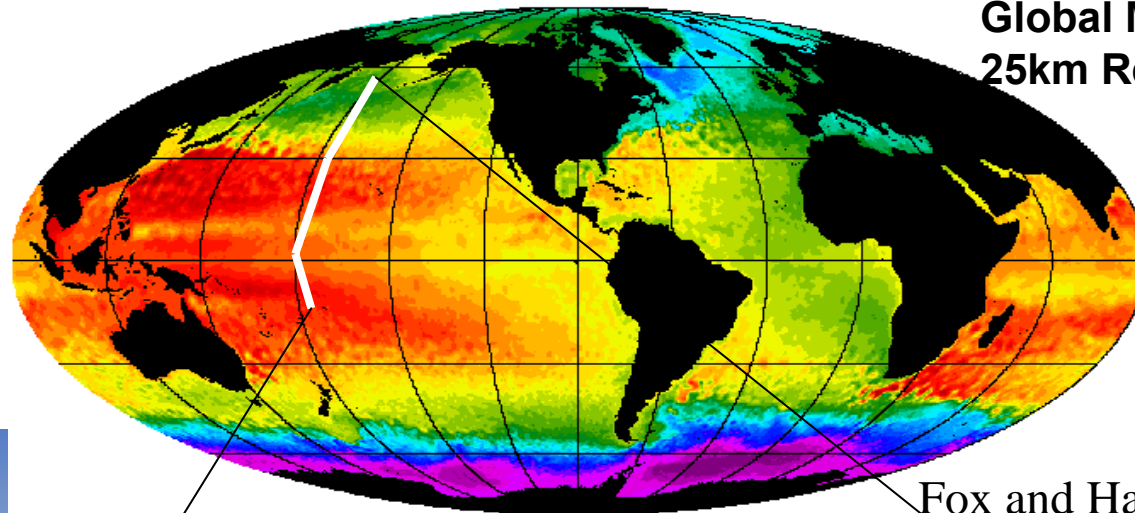
Two Key problems of Altimeter Assimilation

- Projecting the sea surface height signal below the surface
 - Covariance functions
 - Physically based methods
- How to treat the mean sea surface height or Mean Dynamic Topography?
 - MDT from elsewhere eg. Ocean model
 - Error characteristics very different from Altimeter anomalies
 - Problem in Observation bias

Assimilation of Satellite Altimeter

Global Model
25km Resolution

Altimeter
SSH_anomaly
 η_a



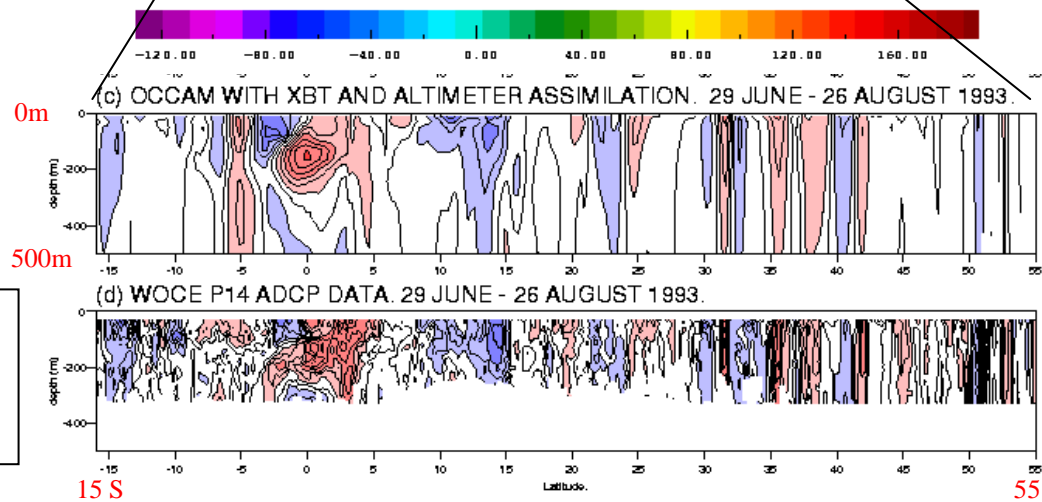
In Situ
T(z)



Fox and Haines 2003

Assimilation

Ship Validation
WOCE Cruise



Covariance vertical projection of sea level

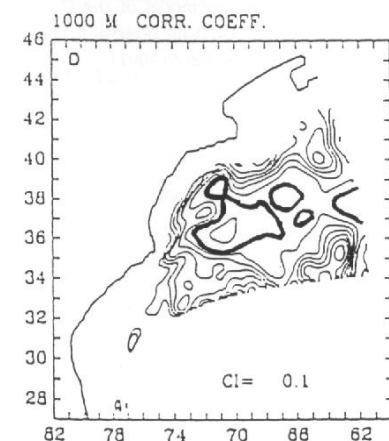
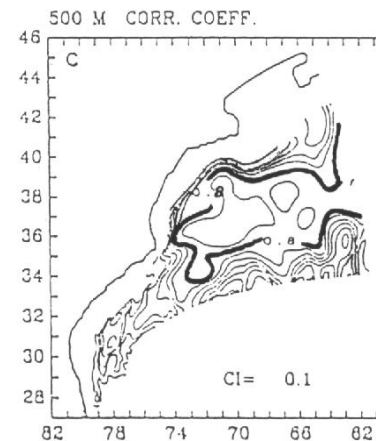
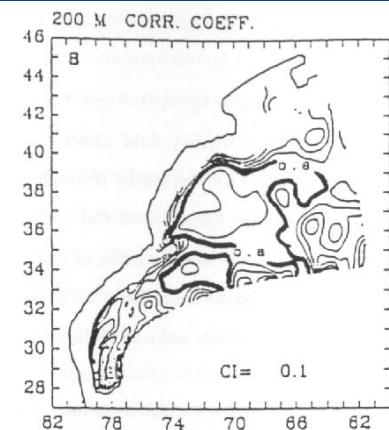
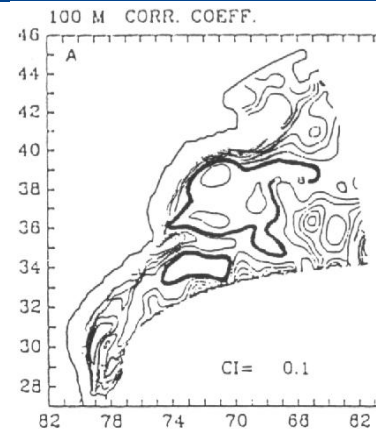
US East Coast model

Mellor and Ezer (1991)

- Sea level correlated with subsurface density
- Correlations based on **model variability**

Potential problems

- Must perform long model runs to generate correlations
- Must store and retrieve correlations for assimilation (which may vary in x, y, t)
- State dependent covariance may be needed, eg. ENSO v. non-ENSO years, (could forecast covariances)



Solid contour = correlation coeff.
of $\rho(z)$ with η of 0.8

Altimeter assimilation by thermocline displacement Δh

Sea surface height correlated with thermocline displacements

Displacements \propto Stratification

PV and water mass conserving

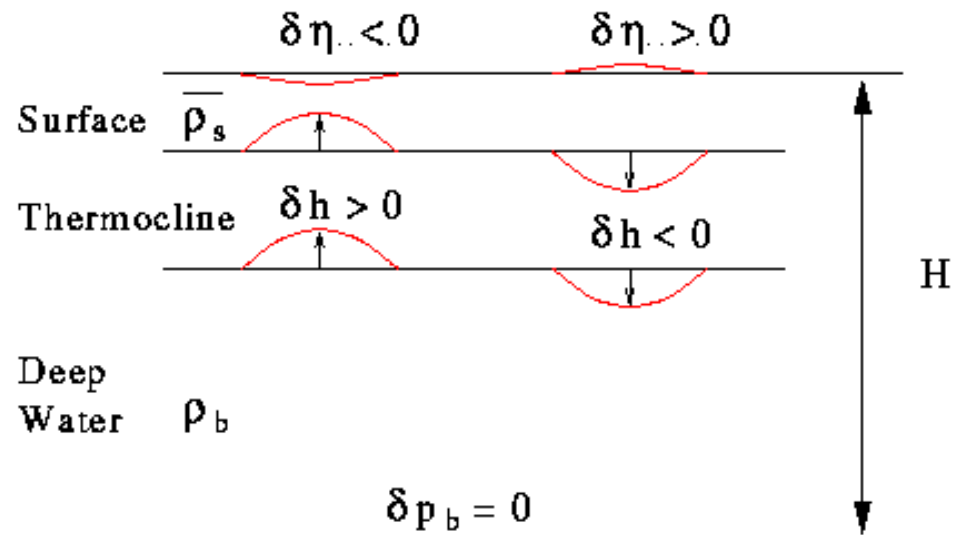
$$\mathbf{q} = \frac{f}{\rho_0} \frac{\partial \rho}{\partial \mathbf{z}}$$

Model $\mathbf{q}(\rho)$ is preserved by Assimilation provided;

$$\Delta \rho = \frac{\partial \rho}{\partial \mathbf{z}} \Delta \mathbf{h},$$

Solve for $\Delta \mathbf{h}$ by assuming deep pressure unchanged

$$-\rho_0 g \delta \eta = \mathbf{g} \int_{-H}^0 \Delta \rho dz,$$



Cooper and Haines (1996)

- Simple to implement
- Gives flow dependent covariances
- Allows other *in situ* data to alter water masses
- Can build physical covariances as **balancing operators** eg. **Var assimilation schemes** eg. **Weaver et al 2005, QJ**

$$\Delta \rho = \frac{\partial \rho}{\partial \mathbf{z}} \Delta \mathbf{h},$$

- But won't work for deep barotropic circulations eg. at high latitudes

A linearized balance operator for global ocean assimilation (Weaver *et al.*, 2005, QJRMS)



- Balance Operator based on Observed Ocean Temperature

Temperature $\delta T^k = \delta T^k = \delta T^k$

Salinity $\delta S^k = \mathbf{K}_{ST}^{k-1} \delta T^k + \delta S_U^k = \delta S_B^k + \delta S_U^k$

SSH $\delta \eta^k = \mathbf{K}_{\eta\rho}^{k-1} \delta \rho^k + \delta \eta_U^k = \delta \eta_B^k + \delta \eta_U^k$

u-velocity $\delta u^k = \mathbf{K}_{up}^{k-1} \delta p^k + \delta u_U^k = \delta u_B^k + \delta u_U^k$

v-velocity $\delta v^k = \mathbf{K}_{vp}^{k-1} \delta p^k + \delta v_U^k = \delta v_B^k + \delta v_U^k$

Treat as approximately mutually independent (Derber & Wu, 1998, MWR).

Density $\delta \rho^k = \mathbf{K}_{\rho T}^{k-1} \delta T^k + \mathbf{K}_{\rho S}^{k-1} \delta S^k$

Pressure $\delta p^k = \mathbf{K}_{p\rho} \delta \rho^k + \mathbf{K}_{p\eta} \delta \eta^k$

Components of the balance operator



Salinity balance
(approx. T-S conservation)

$$\delta S_B^k = \gamma^{k-1} \left(\frac{\partial S}{\partial z} \right)_{S=S^{k-1}} \left(\frac{\partial z}{\partial T} \right)_{T=T^{k-1}} \delta T^k$$

SSH balance
(baroclinic)

$$(\nabla \cdot H \nabla) \delta \eta_B^k = -\nabla \cdot \int_{z=-H}^0 \int_{z'=z}^0 (\nabla \delta \rho^k(z') / \rho_0) dz' dz$$

u-velocity balance
(geostrophy with
 β -plane approx. near eq.)

$$\delta u_B^k = -\frac{1}{\rho_0} \left(\frac{W_f}{f} + \frac{W_\beta}{\beta} \frac{1}{a} \frac{\partial}{\partial \varphi} \right) \frac{1}{a} \frac{\partial \delta \tilde{p}^k}{\partial \varphi}$$

v-velocity
(geostrophy, zero at eq.)

$$\delta v_B^k = \frac{1}{\rho_0} \frac{W_f}{f} \frac{1}{a \cos \varphi} \frac{\partial \delta \tilde{p}^k}{\partial \lambda}$$

Density
(linearized eq. of state)

$$\delta \rho^k = \rho_0 \left(-\alpha^{k-1} \delta T^k + \beta^{k-1} (\delta S_B^k + \delta S_U^k) \right)$$

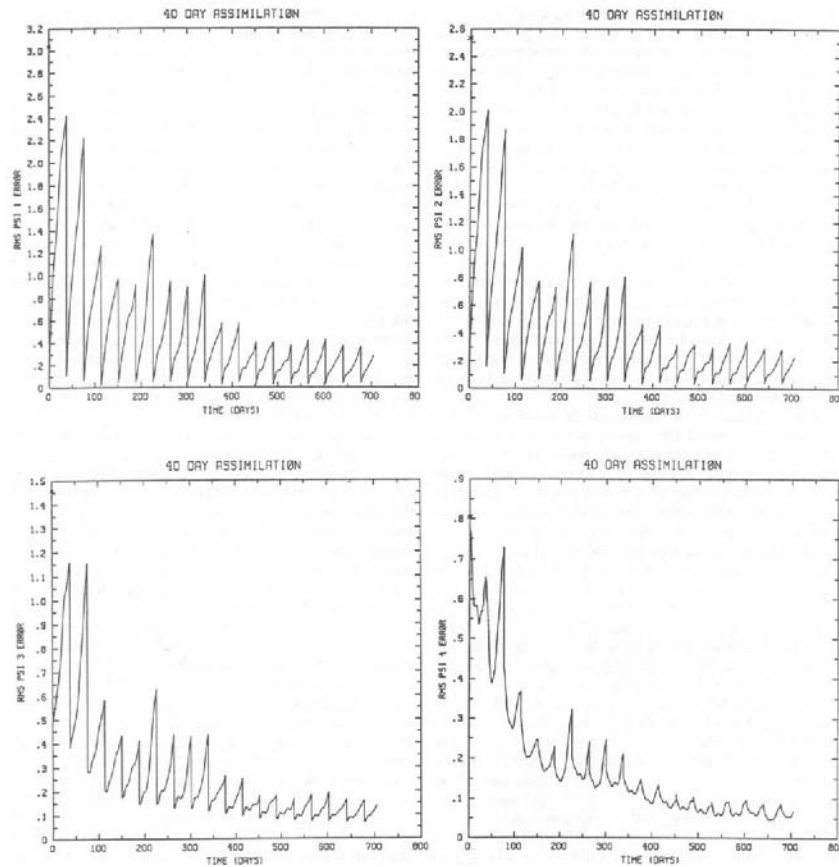
Pressure
(hydrostatic approx.)

$$\delta \tilde{p}^k(z) = \int_{z'=z}^0 \delta \rho^k(z') g dz' + \rho_0 g (\delta \eta_B^k + \delta \eta_U^k)$$

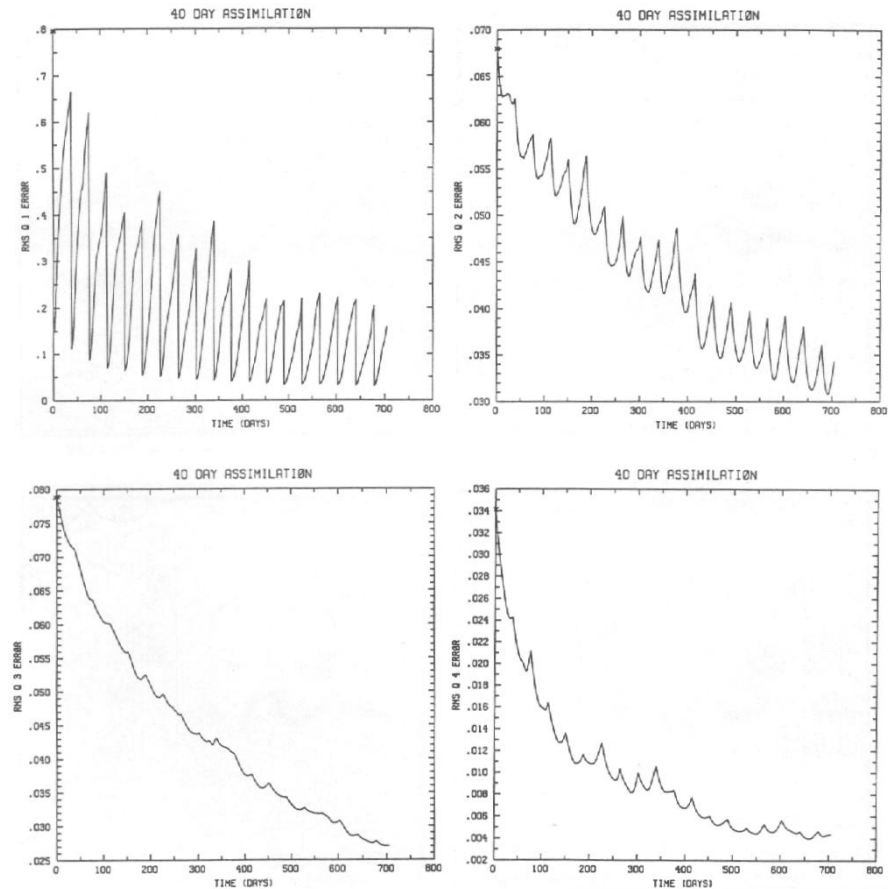
+ β -plane correction

Twin experiment assimilation of ψ_1 every 40 days 4-layer QG box ocean model

$\psi_1 - \psi_4$

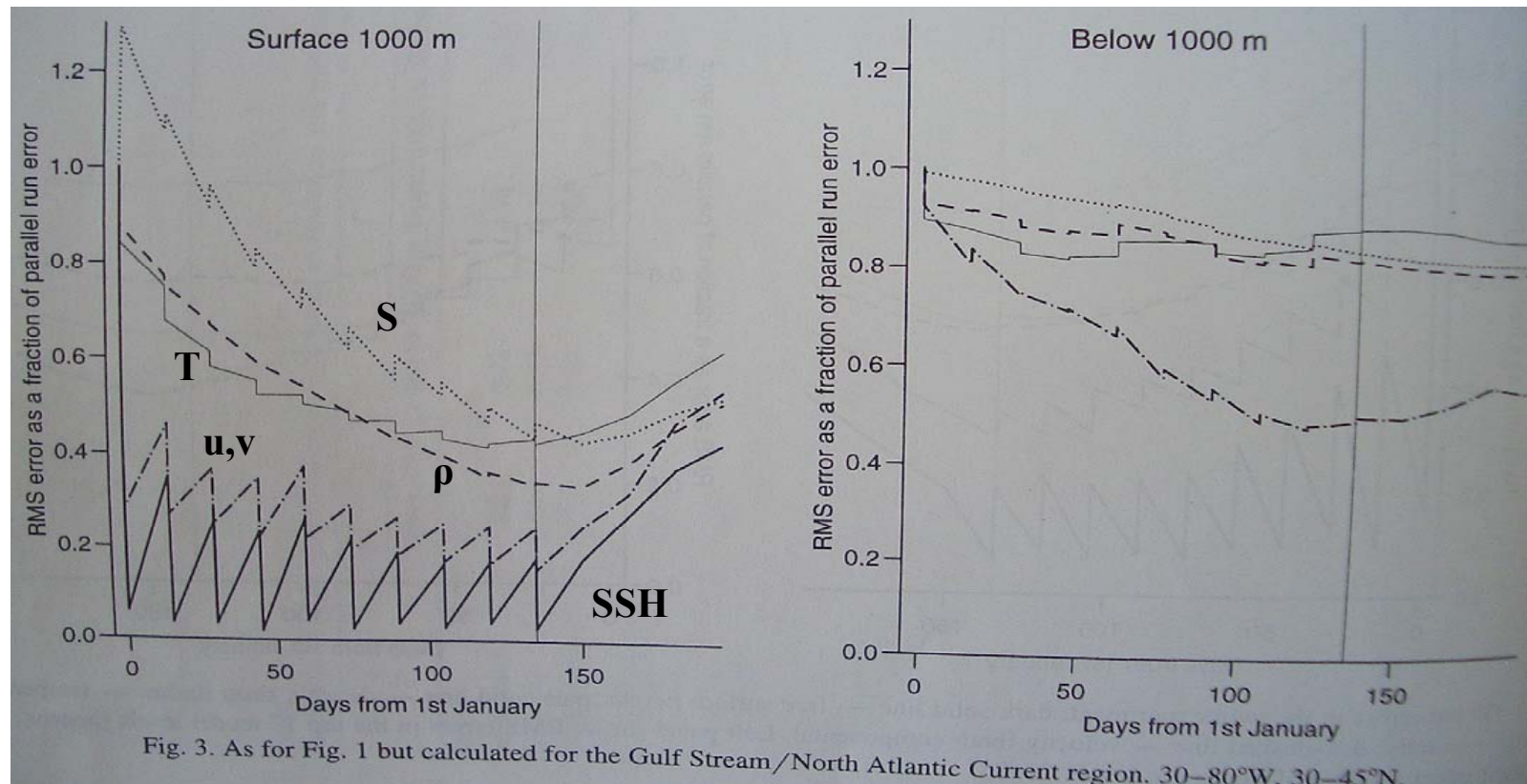


$q_1 - q_4$



Note $q_2 - q_4$ unchanging at assimilation times

Altimeter Twin in OCCAM 36 level PE model assimilating SSH



Fox et al 2001a

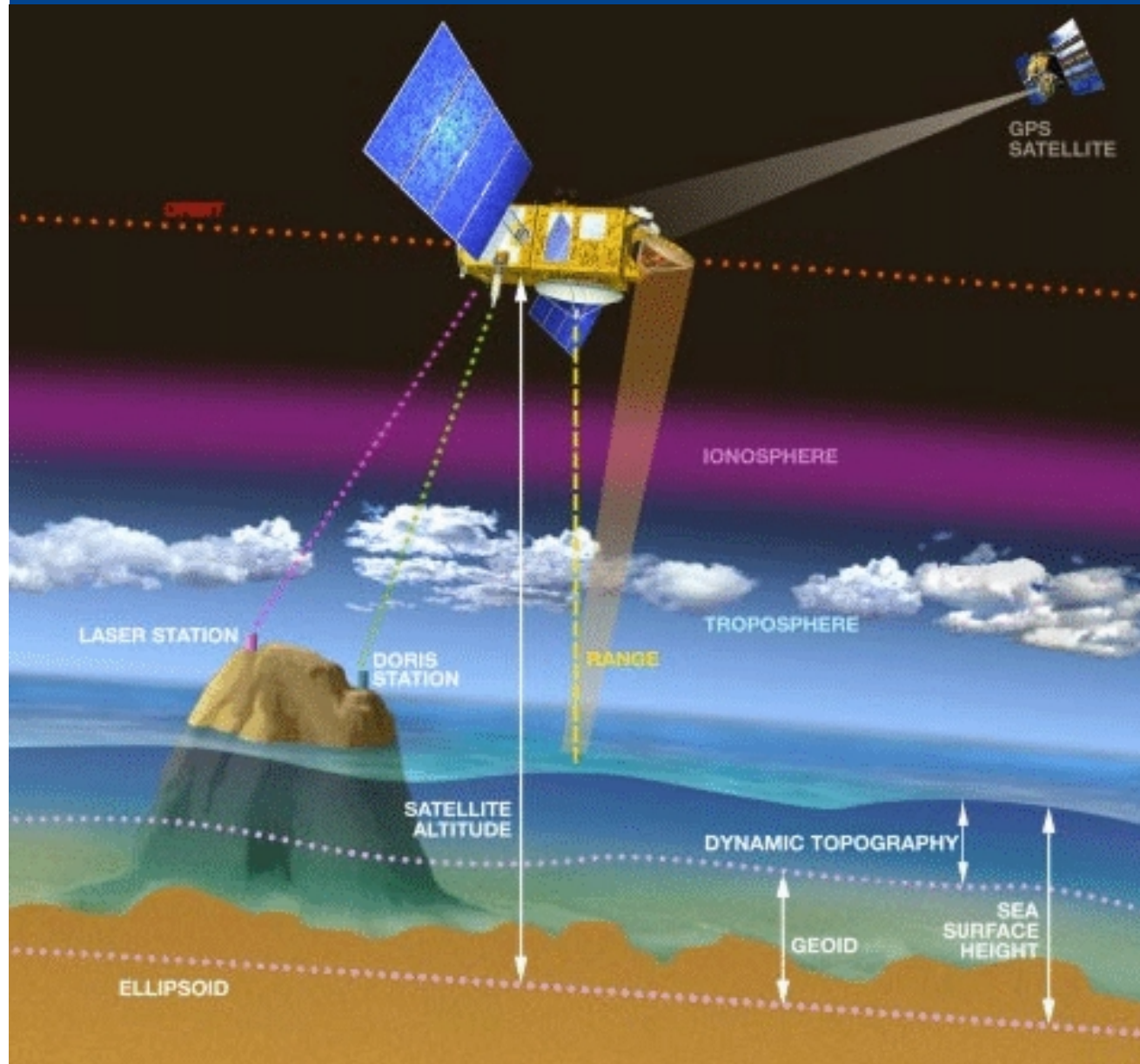
Note that subsurface T,S converge

Perhaps now could use Argo to demonstrate in real ocean?

Two Key problems of Altimeter Assimilation

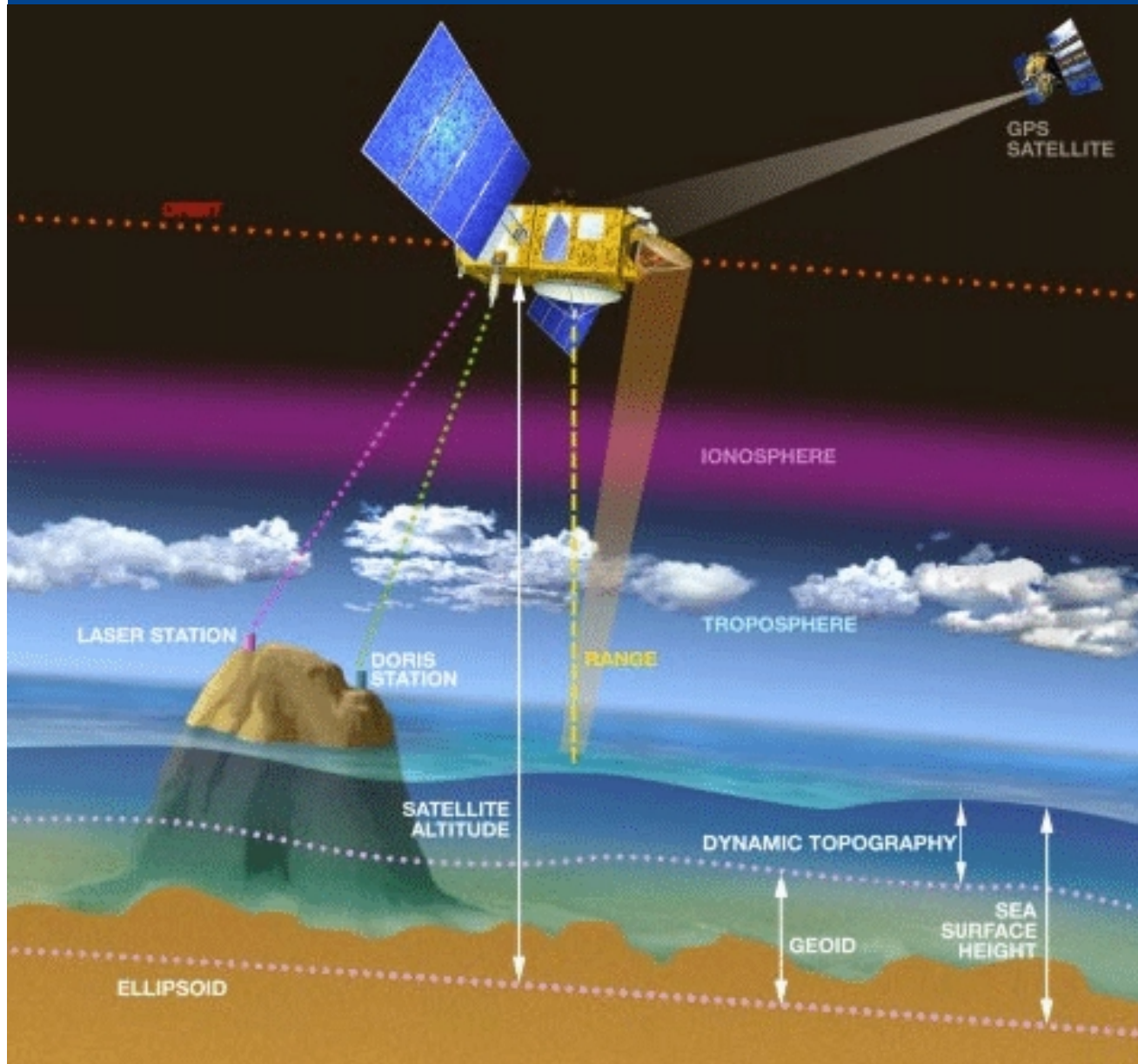
- Projecting the dynamic topography signal below the surface
 - Covariance functions
 - Physically based methods
- How to treat the Mean Dynamic Topography?
 - MDT from elsewhere eg. Ocean model
 - Error characteristics very different from Altimeter anomalies
 - Problem in Observation bias

The Geoid, Altimetry and Ocean Dynamic Topography



- Geoid = surface of constant gravitational potential energy
- Sea level relative to Geoid = **Dynamic Topography (DT)** => Geostrophic currents
- Altimeters measure sea level relative to Earth ellipsoid not Geoid
- Can only use **time-varying** altimetry for oceanography because Geoid is not well known

The Geoid, Altimetry and Ocean Dynamic Topography



Assimilation assumes full DT

$DT = MDT + SSH_anomaly$
where

$MDT = \text{Time mean } DT$

Like to use

$MDT = \text{Mean_SSH} - \text{Geoid}$

In practice

MDT model product

Error characteristics of
SSH_anomaly and MDT
Completely different

$DT = MDT + SSH_anomaly$
MDT error represents
constant **observation bias**

Bias in Data Assimilation

- Dee (2006) Review in QJRMS
- 3D Variational formulation easiest to understand (derivable from Bayesian analysis; Drecourt et al; 2006)

$$2J(\mathbf{x}, \mathbf{b}, \mathbf{c}) = (\mathbf{y} - \mathbf{b} - \mathbf{x})^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{b} - \mathbf{x}) + \quad \text{Minimise } J \text{ wrt } \mathbf{x}, \mathbf{b}, \mathbf{c}$$
$$(\mathbf{x} - \mathbf{x}^f + \mathbf{c})^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}^f + \mathbf{c}) +$$
$$(\mathbf{b} - \mathbf{b}^f)^T \mathbf{O}^{-1} (\mathbf{b} - \mathbf{b}^f) + (\mathbf{b}^T \mathbf{T}^{-1} \mathbf{b} +)$$
$$(\mathbf{c} - \mathbf{c}^f)^T \mathbf{P}^{-1} (\mathbf{c} - \mathbf{c}^f)$$

\mathbf{y} = observation

\mathbf{x} = model state

\mathbf{b} = **observation bias**

\mathbf{c} = **model forecast bias**

Superscript f are forecast values

Observation operators have been omitted

\mathbf{R} = observation error covariance

\mathbf{B} = model background error covariance

\mathbf{O} = observation bias forecast error covariance

\mathbf{T} = **observation bias error covariance**

\mathbf{P} = model forecast bias error covariance

Bias in Data Assimilation

- Solution (Analysed variables ^a)

$$\mathbf{x}^a = (\mathbf{x}^f - \mathbf{c}^f) + \mathbf{K} \{(\mathbf{y} - \mathbf{b}^f) - (\mathbf{x}^f - \mathbf{c}^f)\}$$

$$\mathbf{b}^a = \mathbf{b}^f + \mathbf{F} \{(\mathbf{y} - \mathbf{b}^f) - (\mathbf{x}^f - \mathbf{c}^f)\}$$

$$\mathbf{c}^a = \mathbf{c}^f + \mathbf{G} \{(\mathbf{y} - \mathbf{b}^f) - (\mathbf{x}^f - \mathbf{c}^f)\}$$

$$\mathbf{K} = (\mathbf{B} + \mathbf{P}) [\mathbf{B} + \mathbf{P} + \mathbf{O} + \mathbf{R}]^{-1}$$

$$\mathbf{F} = \mathbf{O} [\mathbf{B} + \mathbf{P} + \mathbf{O} + \mathbf{R}]^{-1}$$

$$\mathbf{G} = \mathbf{P} [\mathbf{B} + \mathbf{P} + \mathbf{O} + \mathbf{R}]^{-1}$$

or
$$\mathbf{x}^a = (\mathbf{x}^f - \mathbf{c}^a) + \mathbf{K}_1 \{(\mathbf{y} - \mathbf{b}^a) - (\mathbf{x}^f - \mathbf{c}^a)\} \quad \mathbf{K}_1 = \mathbf{B} [\mathbf{B} + \mathbf{R}]^{-1}$$

y = observation

x = model state

b = observation bias

c = model forecast bias

R = observation error covariance

B = model background error covariance

O = observation bias forecast error covariance

P = model forecast bias error covariance

- Usual problems are: (i) Knowing the Covariance errors: $\mathbf{O} = \gamma_b \mathbf{T}$; $\mathbf{P} = \gamma_c \mathbf{B}$
(ii) Sequential 3DVar requires bias models:

Can use Persistence $\mathbf{b}^f(t+1) = \mathbf{b}^a(t)$; $\mathbf{c}^f(t+1) = \beta \mathbf{c}^a(t)$ ($\beta = 3$ month decay)

3D-Var cost function with model and obs. bias

$$\begin{aligned} J = & (\mathbf{y} - \mathbf{H}(\mathbf{x} + \mathbf{b}))^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{H}(\mathbf{x} + \mathbf{b})) && \text{Model data misfit} \\ & + (\mathbf{x} - \mathbf{x}^f + \mathbf{c})^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}^f + \mathbf{c}) && \text{Background constraint} \\ & + (\mathbf{b}^o - \mathbf{b})^T \mathbf{T}^{-1} (\mathbf{b}^o - \mathbf{b})^T && \text{Obs bias constraint} \\ & + (\mathbf{b} - \mathbf{b}^f)^T \mathbf{O}^{-1} (\mathbf{b} - \mathbf{b}^f) && \text{Obs bias forecast constraint} \\ & + (\mathbf{c} - \mathbf{c}^f)^T \mathbf{P}^{-1} (\mathbf{c} - \mathbf{c}^f) && \text{Model bias forecast constraint} \end{aligned}$$

\mathbf{x} – model state

\mathbf{y} – observation

\mathbf{R} – observation error covariance

\mathbf{B} – background error covariance

\mathbf{H} – observation operator

\mathbf{b} – observation bias

\mathbf{c} – model bias

\mathbf{T} – observation bias error covariance

\mathbf{O} – obs bias forecast error covariance

\mathbf{P} – model bias forecast error covariance

Method: Analysis equations

$$\mathbf{x}^a = (\mathbf{x}^f - \mathbf{c}^f) + \mathbf{K}_1 \{ \mathbf{y} - \mathbf{H}(\mathbf{L}\mathbf{b}^o + (\mathbf{I} - \mathbf{L})\mathbf{b}^f) - \mathbf{H}(\mathbf{x}^f - \mathbf{c}^f) \} \quad ..$$

$$\mathbf{K}_1 = (\mathbf{B} + \mathbf{P})\mathbf{H}^T \{ \mathbf{H}(\mathbf{B} + \mathbf{P} + \mathbf{L}\mathbf{T})\mathbf{H}^T + \mathbf{R} \}^{-1} \quad \quad \text{State analysis}$$

$$\mathbf{b}^a = \mathbf{H}(\mathbf{L}\mathbf{b}^o + (\mathbf{I} - \mathbf{L})\mathbf{b}^f) + \mathbf{F}\{..\}$$

$$\mathbf{F} = \mathbf{L}\mathbf{T}\mathbf{H}^T \{.....\}$$

Observation bias analysis

$$\mathbf{c}^a = \mathbf{c}^f - \mathbf{G}\{..\}$$

$$\mathbf{G} = \mathbf{P}\mathbf{H}^T \{.....\}$$

Model bias analysis

Method applied to Altimeter assimilation in N Atlantic model at Met Office

R – observation error covariance

B – background error covariance

T – observation bias error covariance

O – obs bias forecast error covariance

P – model bias forecast error covariance

Simplify by assuming

$$\mathbf{O} = \gamma_b \mathbf{T}$$

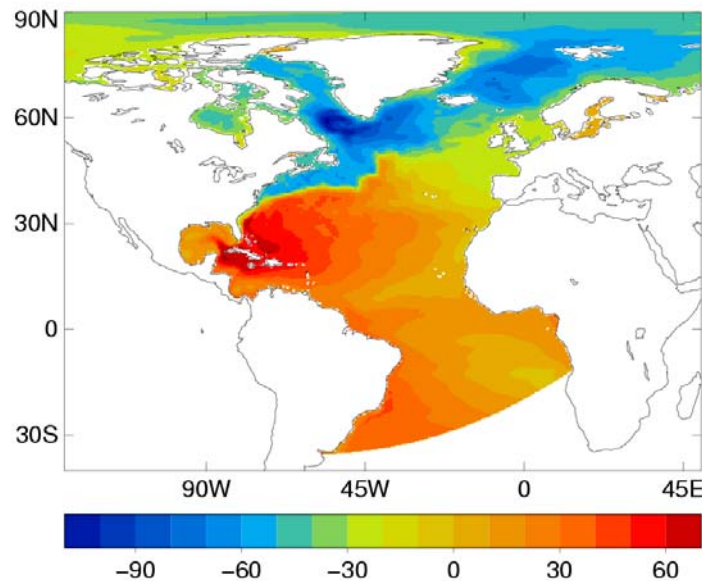
$$\gamma_b = 0.01 \quad (\mathbf{b} \text{ units cm MDT bias})$$

$$\mathbf{P} = \gamma_c \mathbf{B}$$

$$\gamma_c = 10^{-3} \quad (\mathbf{c} \text{ units cm/day Model drift})$$

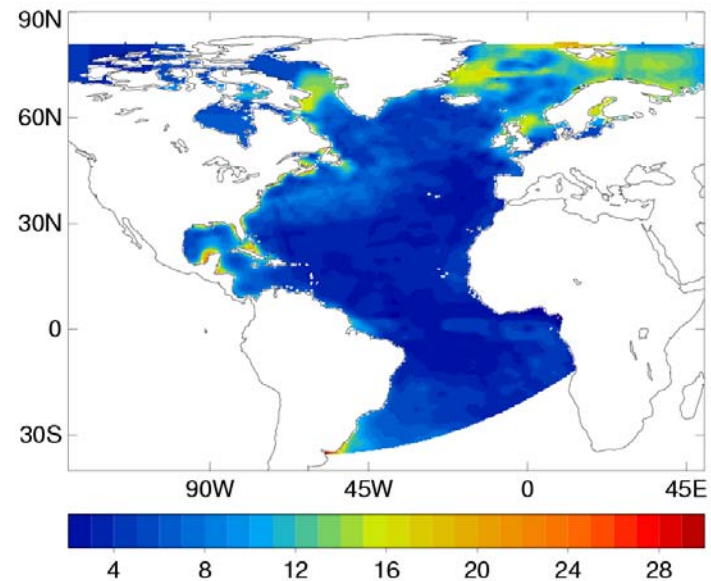
MDT Bias applied to Altimeter assimilation in N Atlantic model at Met Office

Original MDT /cm



Combined model mean,
Singh and Kelly and GOCINA

Original MDT error /cm

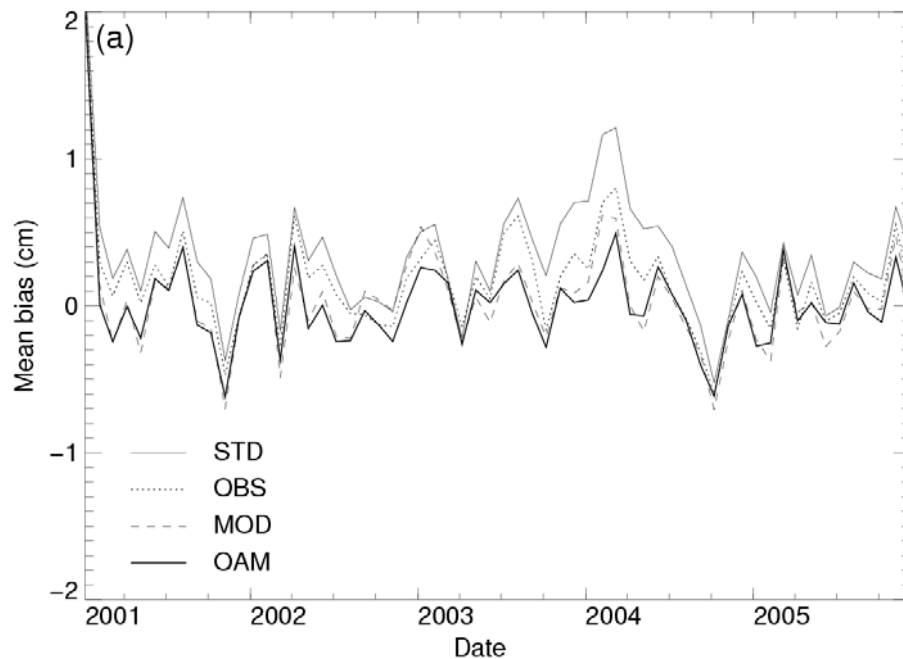


Rio (2005) MDT error
(times 5) – use for T

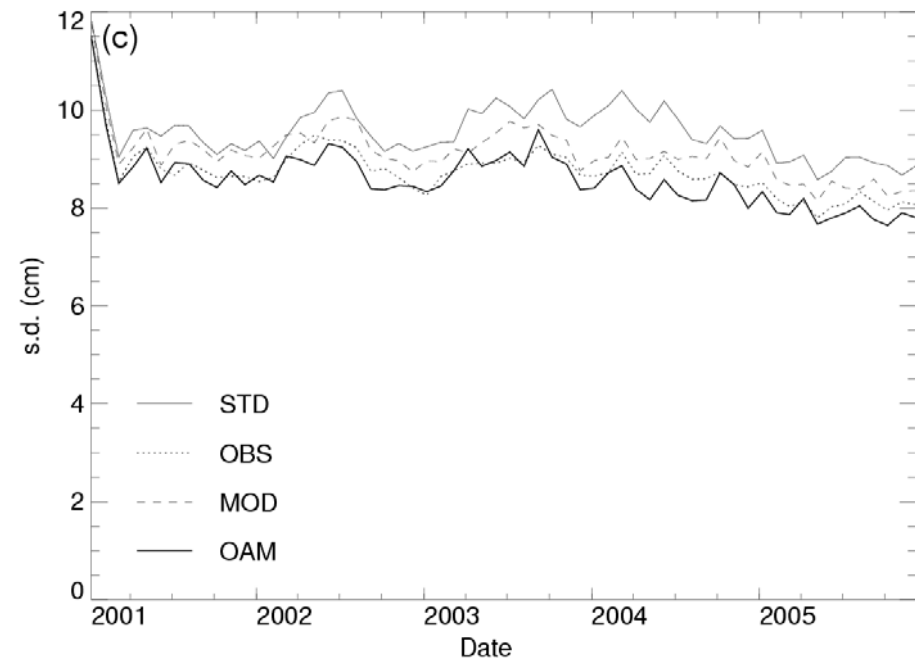
MDT and errors will come from GOCE mission data

Time series of innovations

Mean innovations

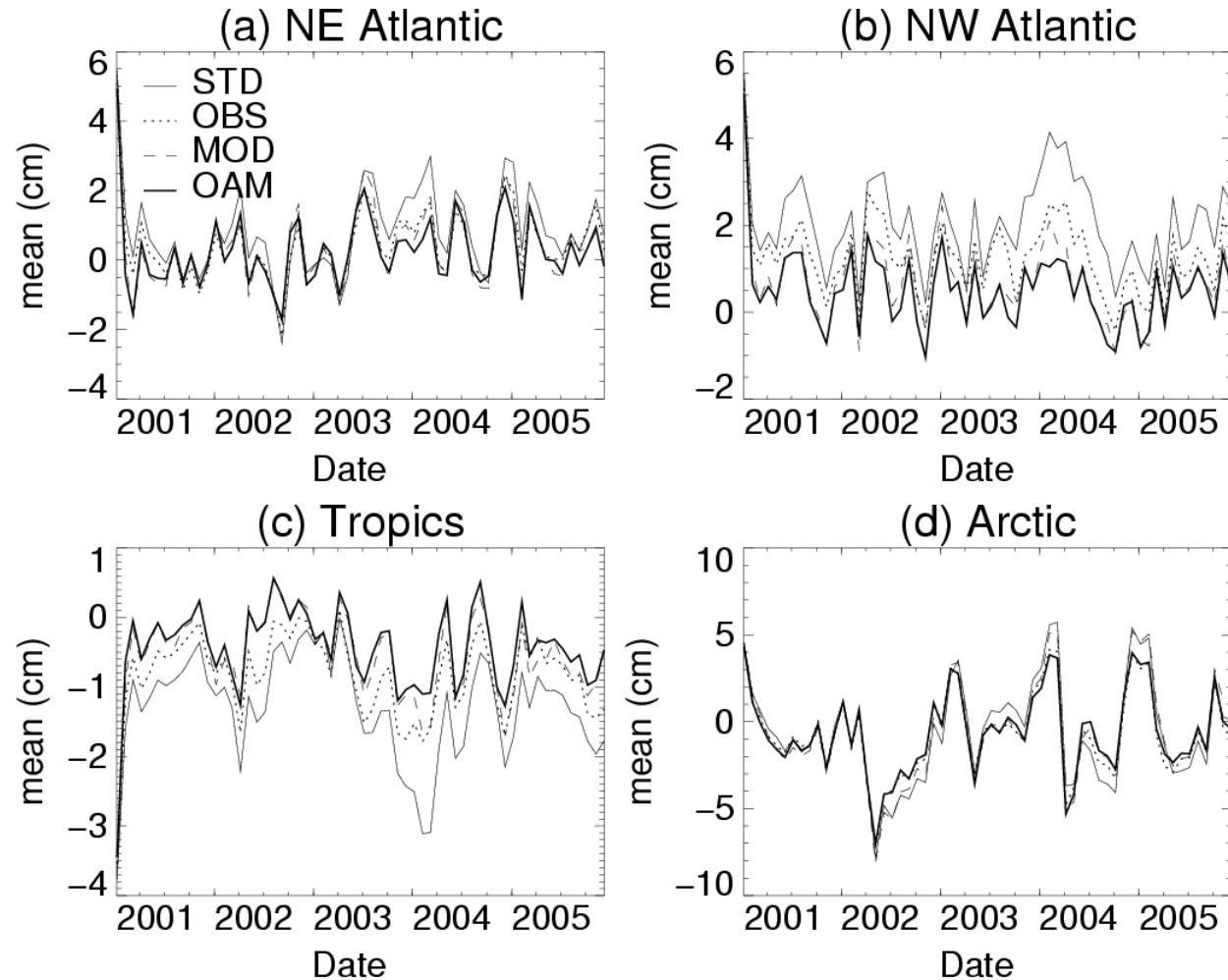


s.d. innovations

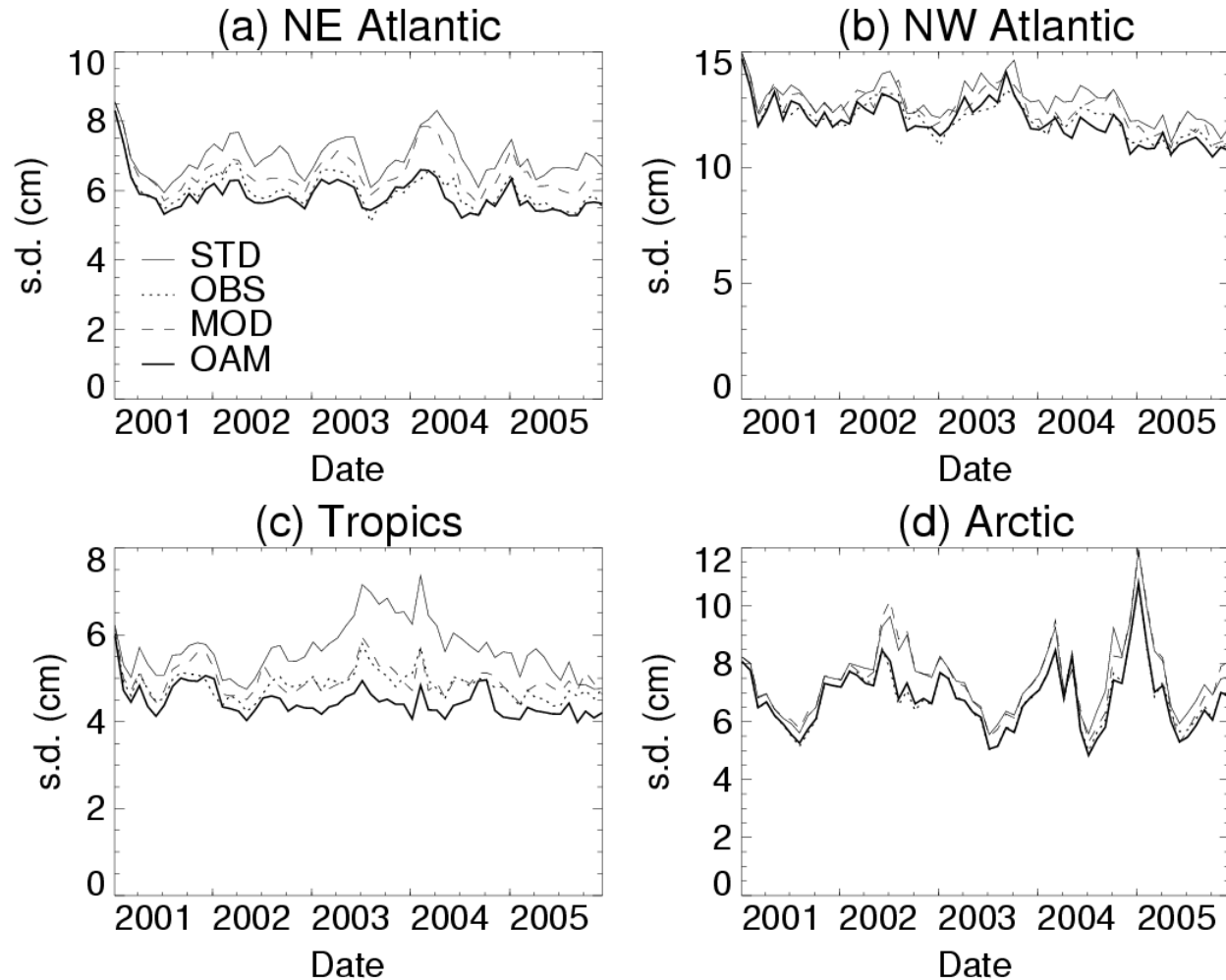


- Time variability and RMS reduced by bias correction
- Obs bias correction most effective in reducing RMS

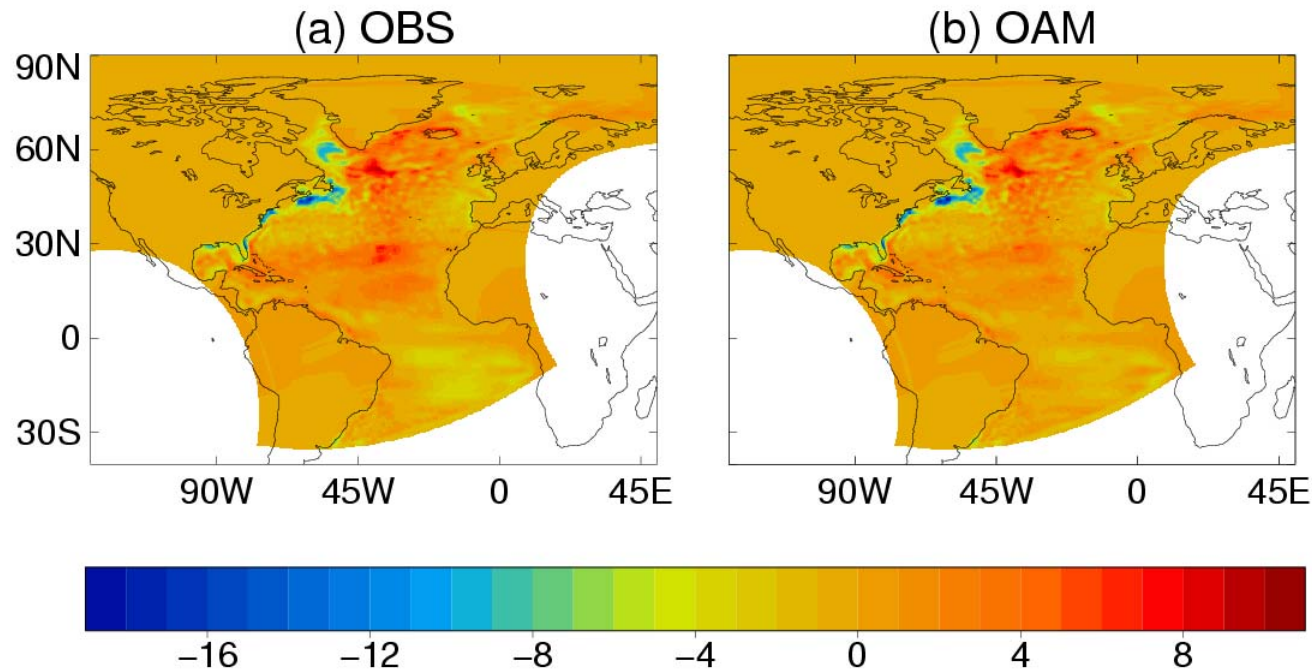
Mean Innovations in areas



Std dev of innovations in areas

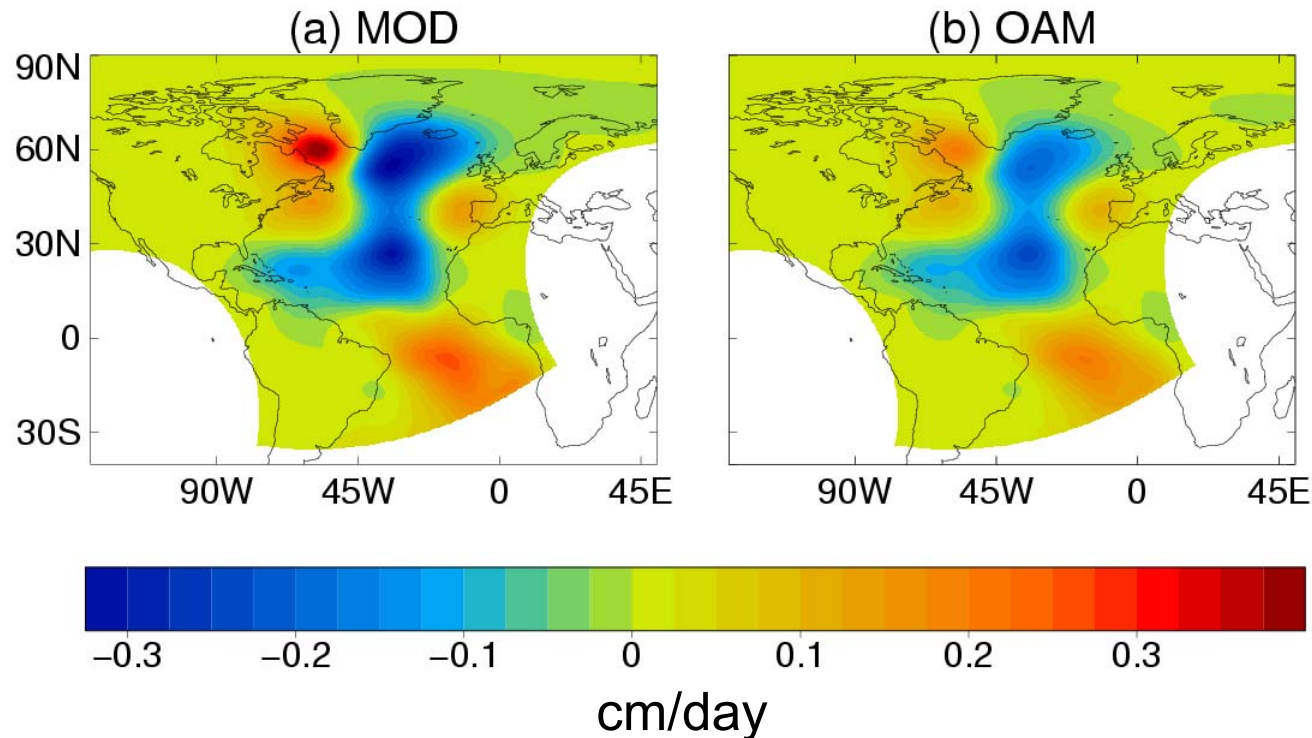


Mean obs bias field (b field)



- MDT lowered north of Gulf Stream, increased in sub-tropical gyre
- Pattern similar for both OBS and OAM. The model bias not significantly affecting the MDT estimate.

Mean model bias field (c field)



- Small mean model bias (units cm/day). Model is positively biased north of Gulf Stream and negatively biased in the sub-tropical gyre.
- Same pattern (with reversed sign) as **b** field (using the same info).

Data Assimilation for Ocean Synthesis/Reanalysis

Aims:

Recover ocean signals relevant to climate change
(1950-present)

Changes in water masses

Changes in Ocean circulation (geostrophic) based on ρ
measurements (eg. thermohaline circulation)

Changes in ocean heat content

Changes in ocean salinity=> hydrological cycle

Infer errors/changes in air-sea fluxes from budgets

Key Data for Ocean Synthesis/Reanalysis

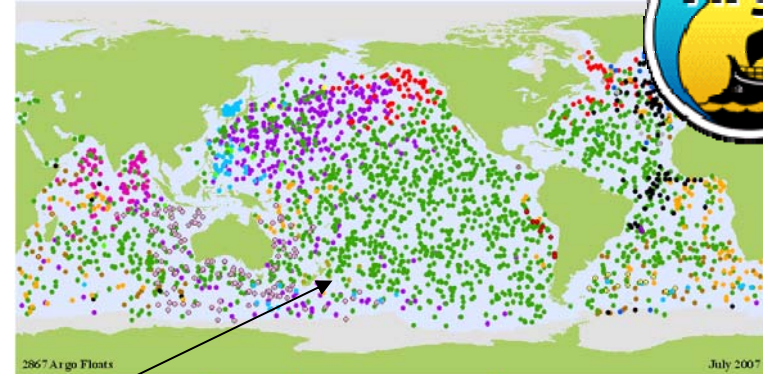
In situ data

T(z) profiles or

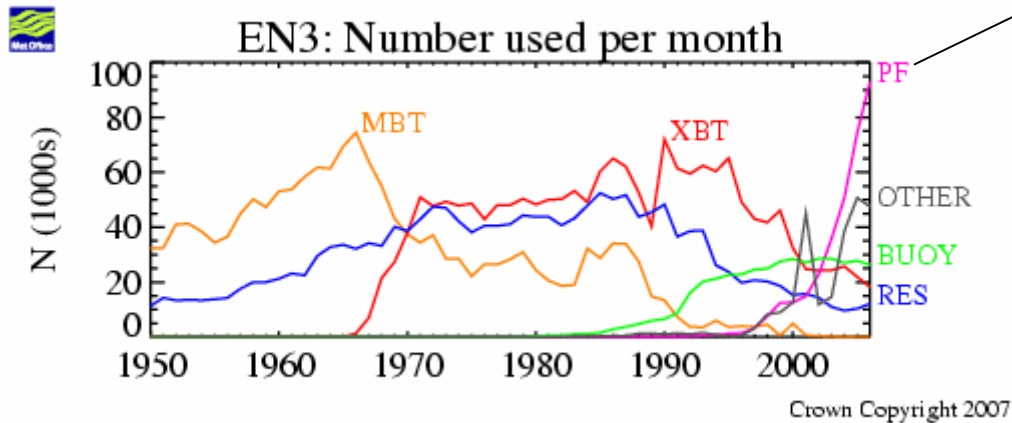
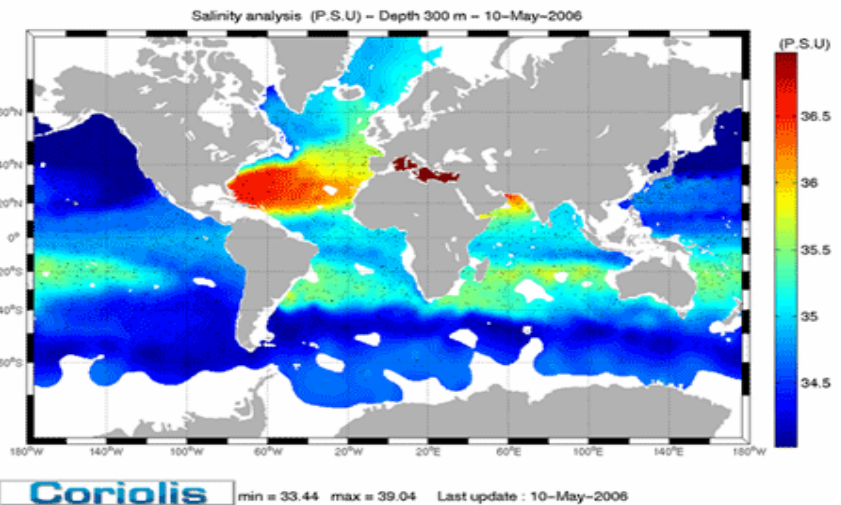
T(z) and S(z) profiles => $\rho(z)$

Instruments, spatial distribution and depth ranges vary through time

In Situ data from Argo PF



2867 Argo Floats July 2007



Met Office Hadley Centre for Climate Change

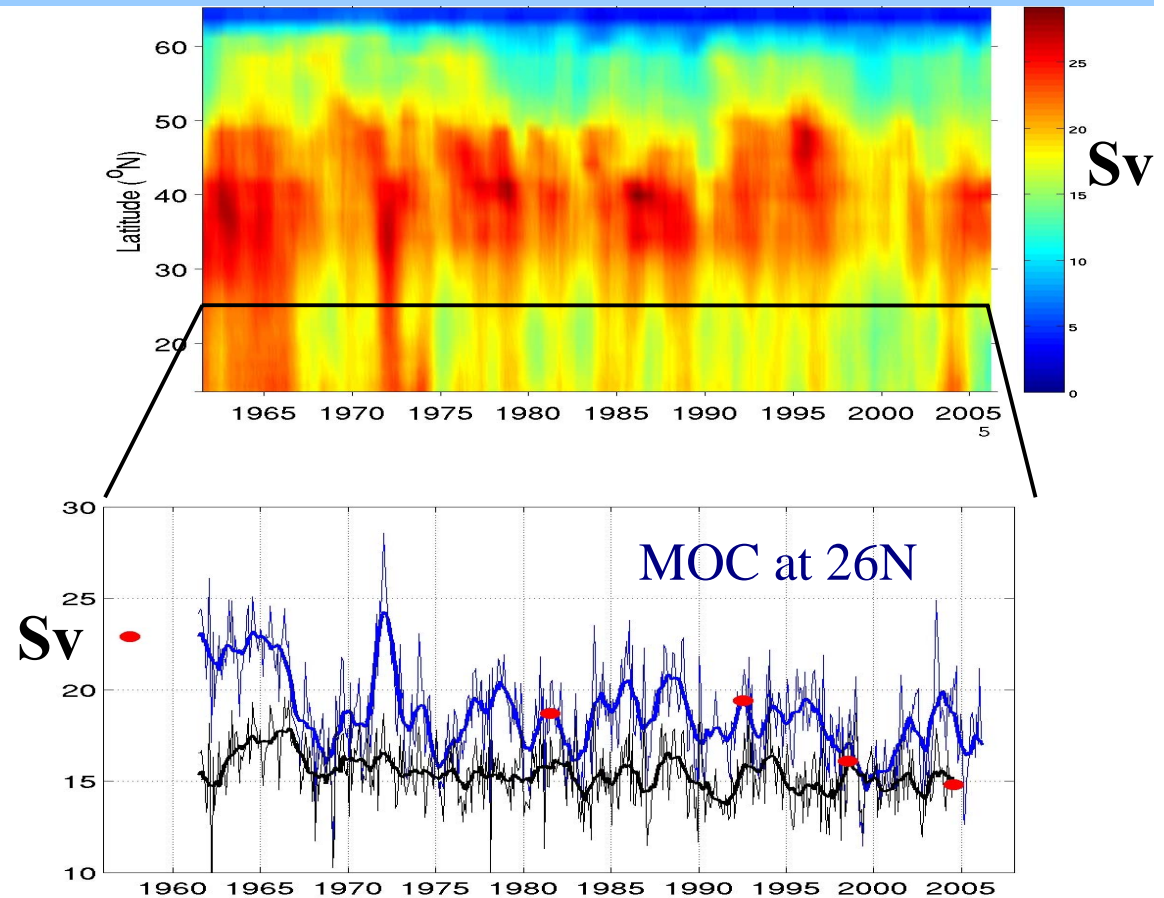
Source: www.metoffice.gov.uk/hadobs

Crown Copyright 2007

ECMWF Ocean Reanalysis 3 (ORA3)

- 47 year ocean reanalysis from ECMWF Seasonal Forecasting System 3
- 1° resolution ocean model with tropical enhancement
- Assimilates T(z) and salinity on isotherms S(T)

Atlantic Meridional Overturning Circulation



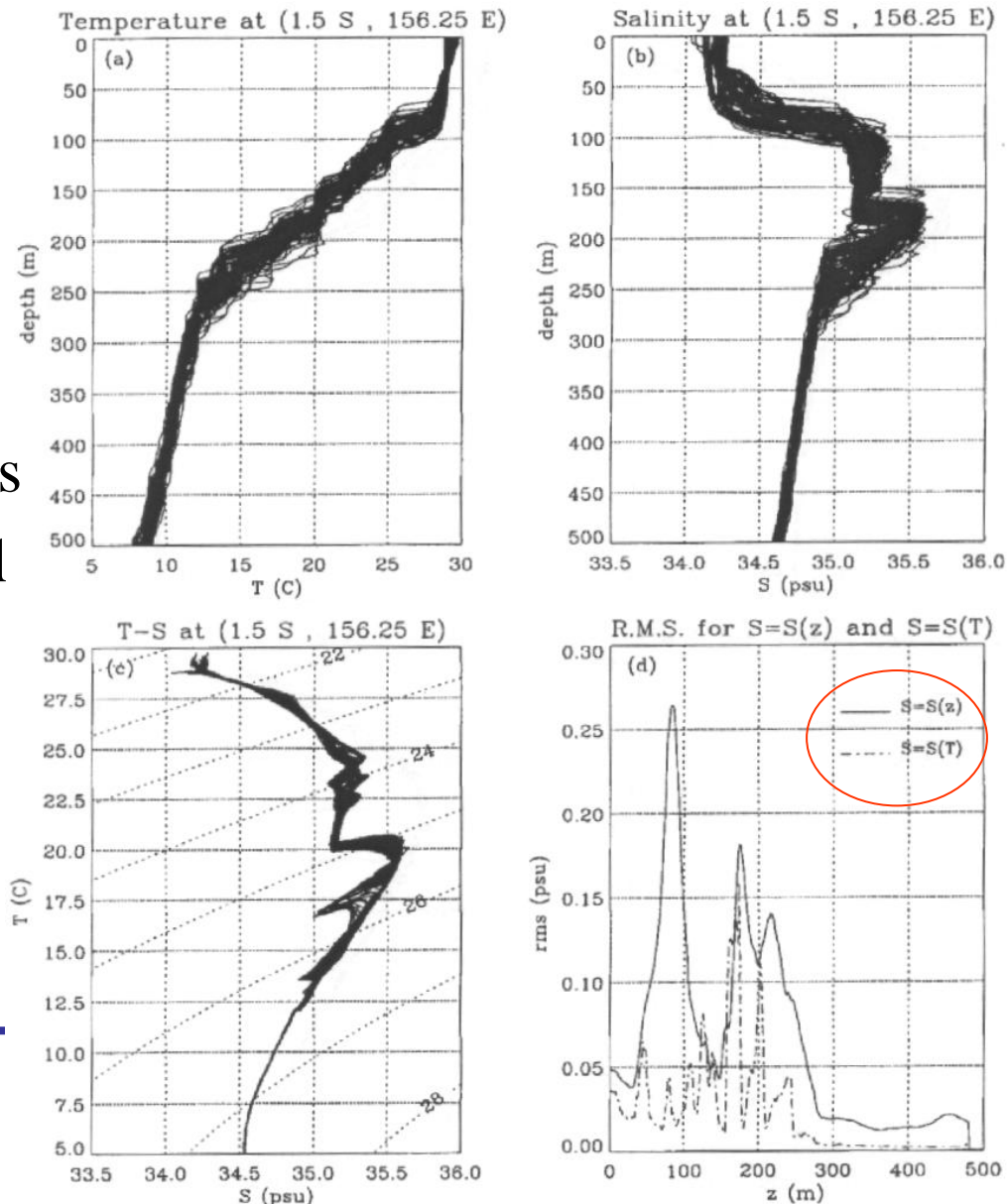
Balmaseda et al 2007 sub.

Dynamic v. thermodynamic variability

104 CTD profiles
over 10 days in
W. Equatorial Pacific

Reduced variance in
 $S(T) \Rightarrow$ water properties
not altered by High-freq
waves

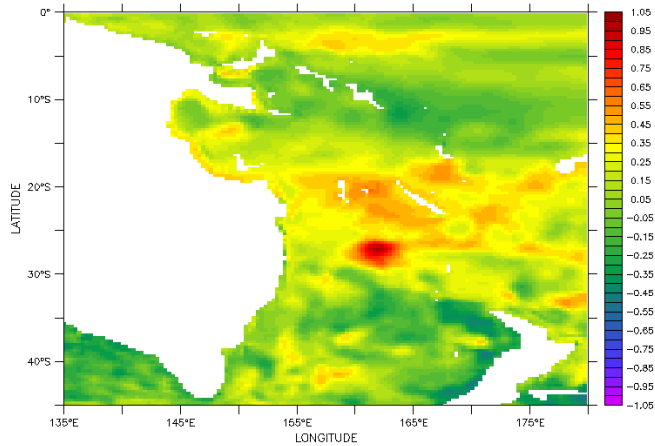
Model **Representivity**
of $S(T)$ better than for
 $S(z)$ or $T(z)$



Troccoli et al
(1999)

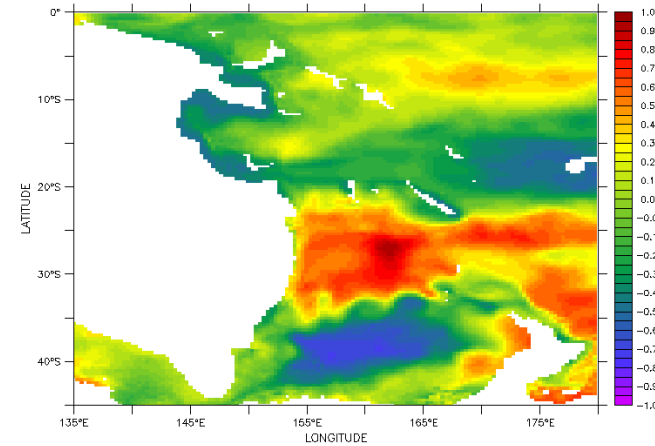
One point Salinity correlation maps HadCEM 1/3 model

$S(z)$



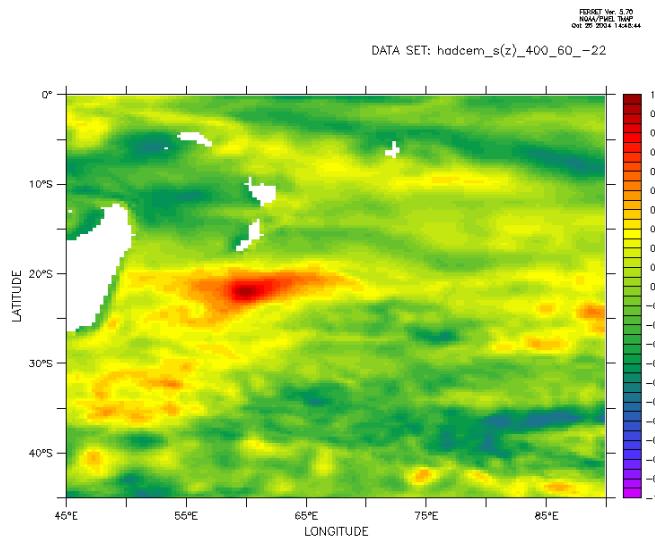
Correlation of salinity on 400m depth surface

$S(T)$



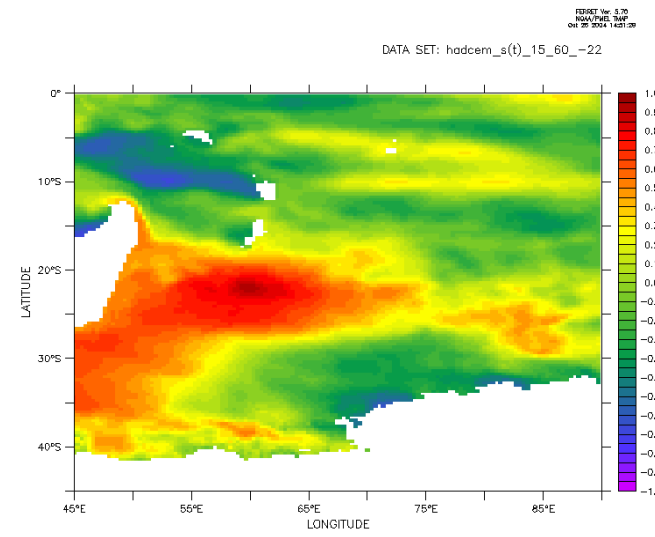
Correlation of salinity on 12C temp surface

**Expect error
Covariances of
 $S(T)$ to be larger
Scale than $S(z)$
=> Useful in
assimilation of
Salinity data,
especially for
Reanalysis**



Correlation of salinity on 400m depth surface

ENVIRONMENTAL SYSTEMS SCIENCE CENTRE



Correlation of salinity on 15C temp surface

ECM

September 2007

Haines et al
(2006)



Generalized observation operator

- Collocate observations on depth, isotherm and isopycnal levels
- By evaluating model-data difference on isotherm or isopycnal levels can better assess errors in water mass properties.

- For isotherms:

- Given $T, S \rightarrow$ Calculate $T(z), S(T)$ for model and observations

$$T'(z) = T_b(z) + \Delta T(z)$$

$$S'(T) = S_b(T) + \Delta S(T) \quad \text{implemented in ECMWF ORA3}$$

- For isopycnals:

- Given $T, S \rightarrow$ Calculate $Z(\rho), \pi(\rho)$ for model and observations

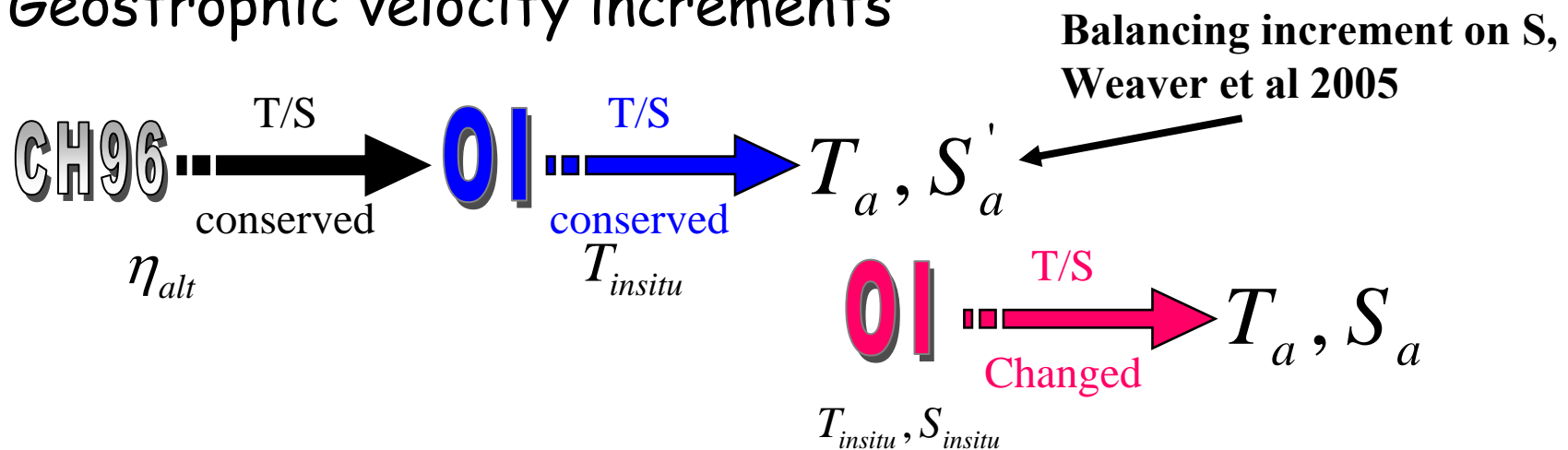
$$Z'(\rho) = Z_b(\rho) + \Delta Z(\rho)$$

$$\pi'(\rho) = \pi_b(\rho) + \Delta\pi(\rho) \quad \text{where } \pi(T, S, \rho) \text{ is "spice"}$$

orthogonal fn. to $\rho(T, S, \rho)$

ECMWF System 3 ocean analysis

- Sequential assimilation (every 10 days)
- In situ and altimeter assimilation
- Geostrophic velocity increments



Second OI using Salinity data to correct the T/S relationship

Assimilation of $S(T)$ not $S(z)$

$$S_a(T_a) = S'_a(T_a) + K'(S_o(T_o) - HS_b(T_o))$$

Note conservation of water masses => Complementary data contributions

Salinity assimilation improves temperature

EqPac

EqAtl

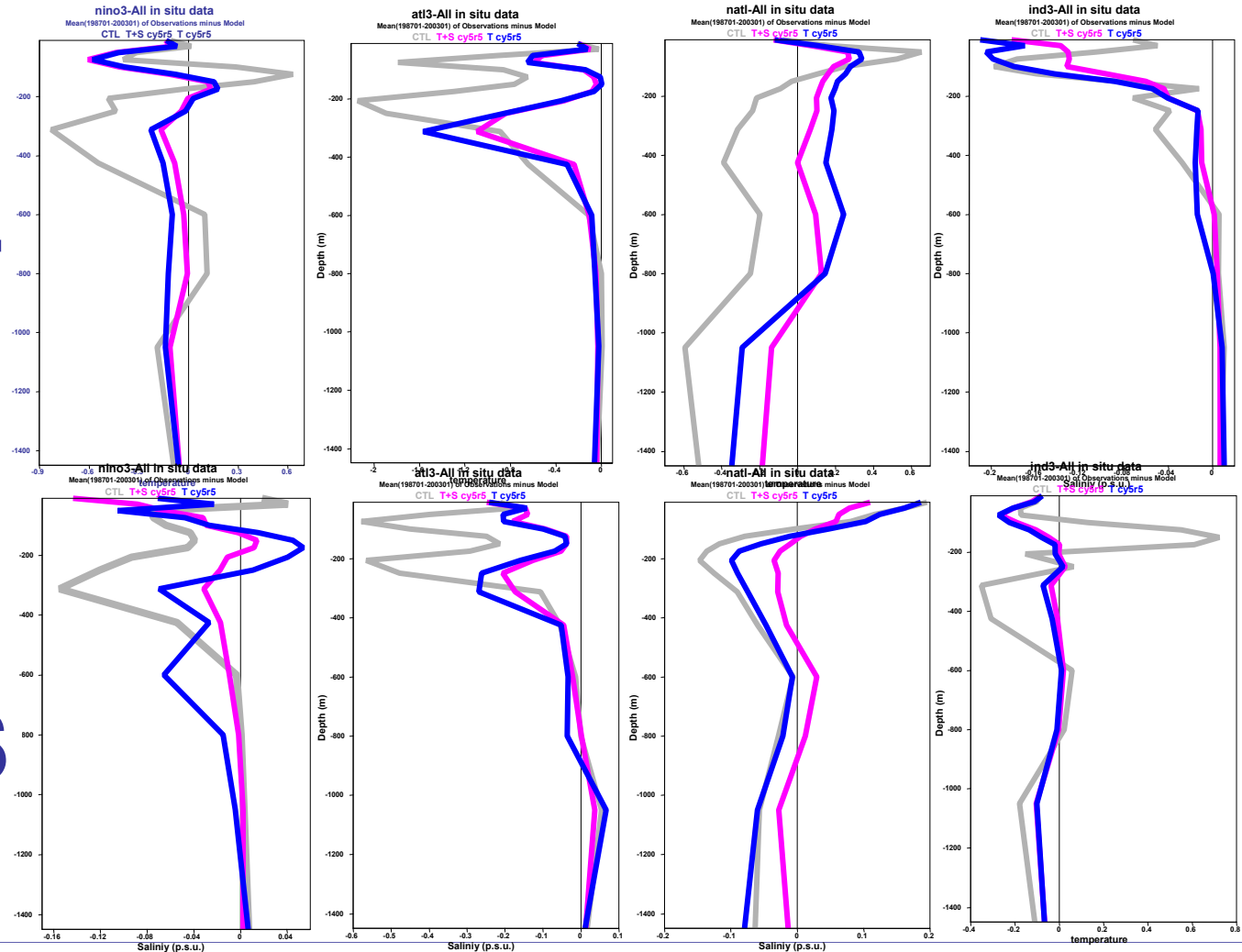
NATL

EqInd

No assim
T assim with
 balancing
 increment ΔS_T
 only
T and S(T)
 assimilation

T

S



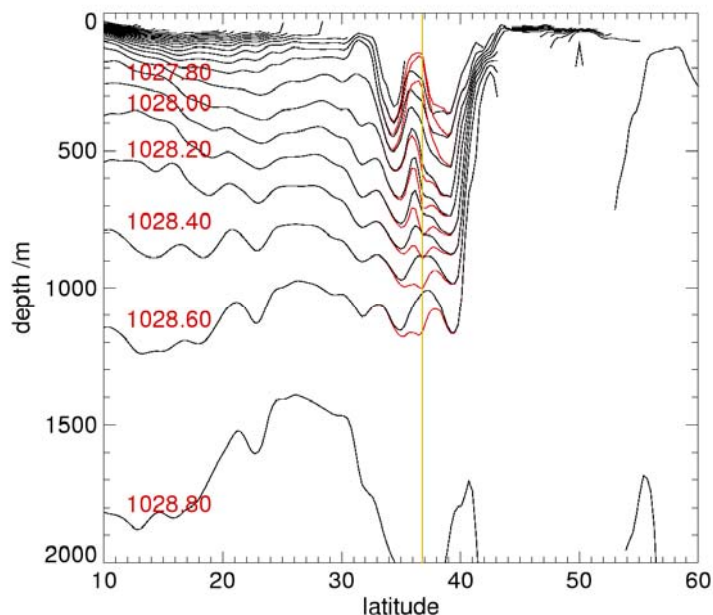
Vidard et al

Mean Observation Minus Background in selected regions for temperature and salinity

Isopycnal assimilation: Assimilation of 1 observation profile

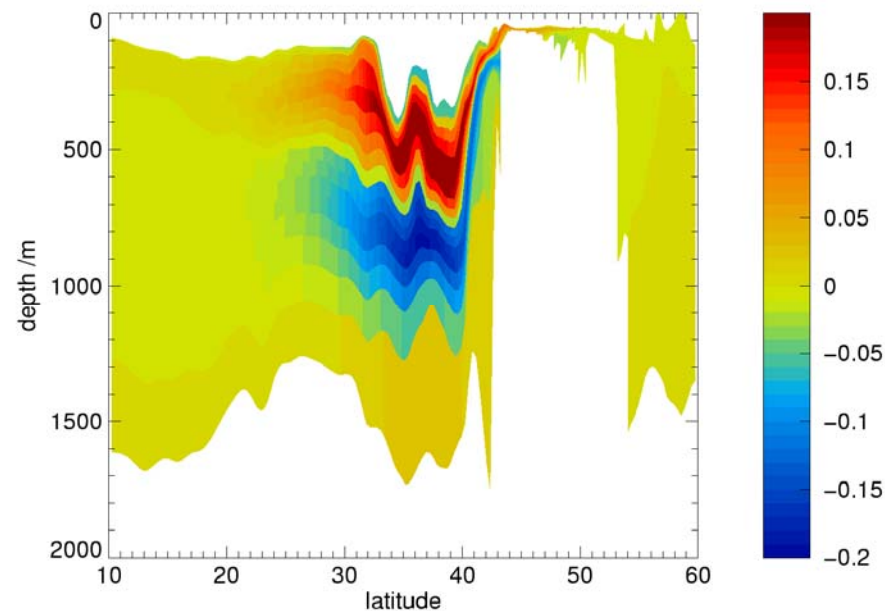
$T(z), S(z) \rightarrow z(\rho), \pi(\rho) \rightarrow \text{Assimilate} \rightarrow T(z), S(z)$

Density level depth $z(\rho)$
before and **after** assimilation



Correlation width 60 km

Spiciness increment $\pi(\rho)$



Correlation width 400 km

Long window 4dVar

Data Assimilation for Coupled-Model Prediction

Aims:

Seasonal Forecasting eg. El Nino

Interannual-decadal forecasting

Based on Coupled Atmosphere-Ocean models

Ocean initial conditions crucial=> ocean assimilation

Prediction based on Ensembles (average Atm. noise)

Coupled assimilation really required to have initial atmosphere-ocean boundary layers consistent

Perhaps other properties should also be assimilated eg. Sea Ice, Snow cover, Soil Moisture?

Seasonal Forecasting

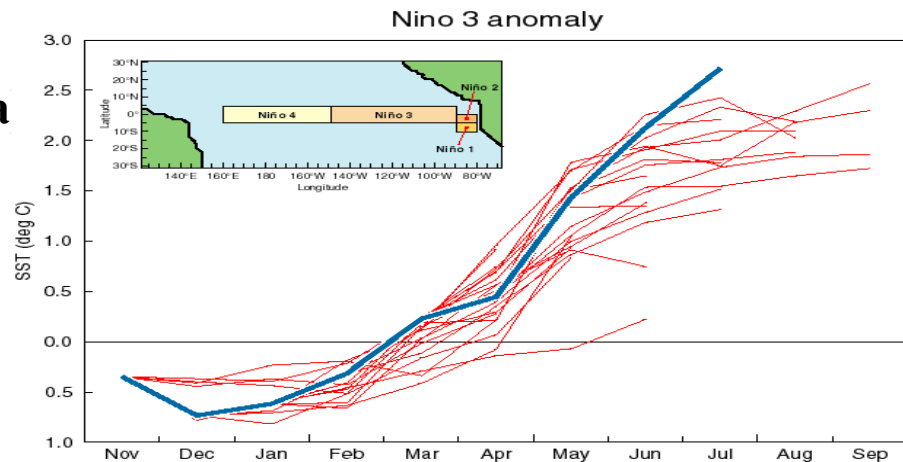
At ECMWF ocean assimilation scheme as for Reanalysis ORA3 (Balmaseda

- Ocean only model run forced with atmospheric ERA-ops and ocean assimilation
- Then coupled to IFS atmosphere for coupled ensemble forecasts

SST shocks common eg. Stockdale 1997

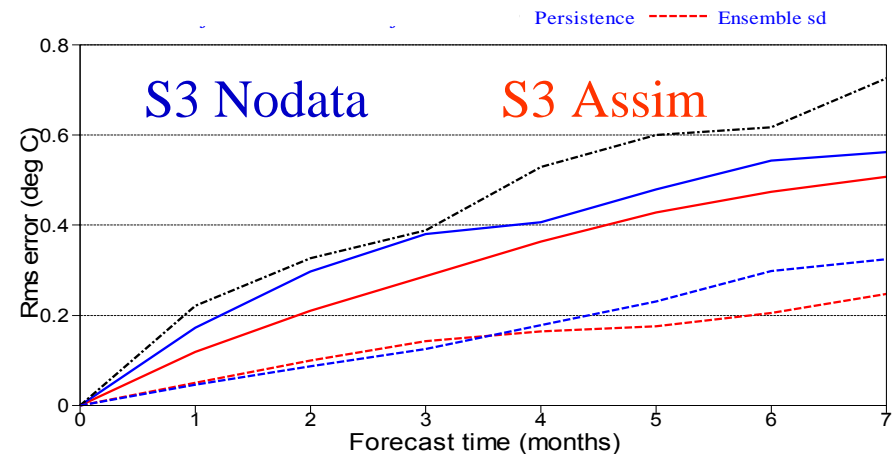
Direct assimilation into coupled system?

- Latif et al. 2004, nudge SST of coupled model: relies on atmos+ocean adjusting
- Coupled 4dVar? => problem with atmospheric noise



NINO4 SST rms errors

76 start dates from 19870101 to 20051001
Ensemble sizes are 3 (esj6) and 3 (esj6)

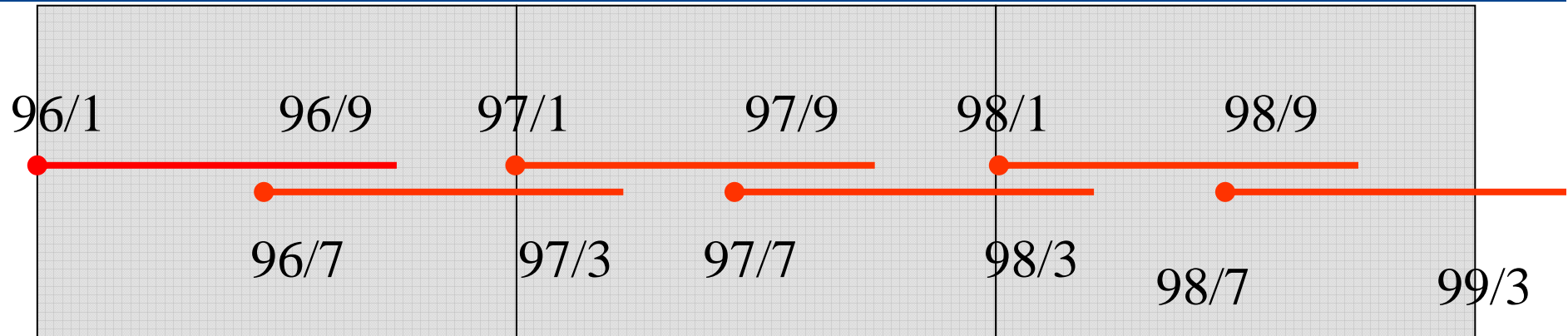


Coupled Data Assimilation at JAMSTEC

thanks to Dr Sugiura and Prof. Awaji

- Assimilation into a **fully coupled GCM**
 - By means of **4D-VAR**
 - Long assimilation window (9 month)
 - Correction of model climatology by parameter estimation
 - Correction of seasonal to interannual trajectory by initialization
 - Atmospheric data are also assimilated
 - Weather mode is treated as noise
- ➔ To be suitable for Seasonal to Interannual state estimation and prediction

CDA Assimilation windows



Control Variables

1. Ocean initial condition
2. Bulk parameters controlling Air-sea fluxes of ; * 97/1 = January of 1997

$$\text{Momentum } \tau = \alpha_D C_D |v| v,$$

$$\text{Sensible heat } H = c_p \alpha_H C_H |v| (\theta_{sfc} - \theta),$$

$$\text{Latent heat } E = \rho \alpha_E C_E |v| (q_{sat} - q),$$

adjustment factors

(x, y, 10daily)

Experimental Settings of Coupled DA

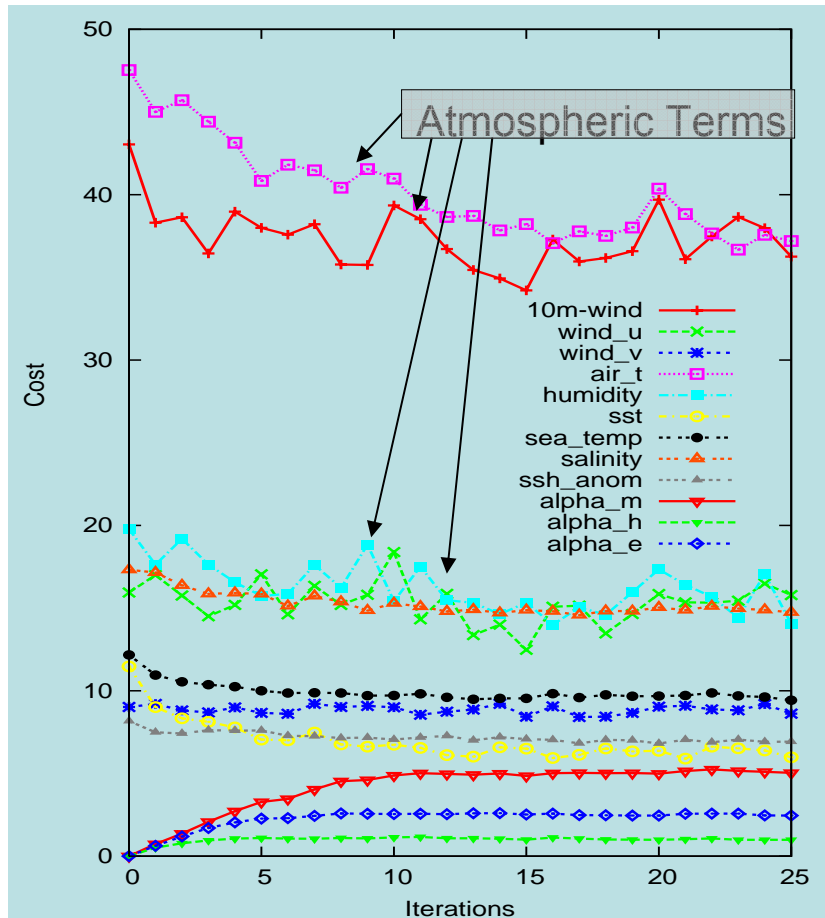
- **Coupled Model (CFES):**
 - T42L24 **AFES** for AGCM
 - 1x1deg L45 **MOM3** for OGCM
 - IARC Sealce model
 - MATSIRO Model for Land
- **Observational Data**
 - Atmosphere:
 - NCEP's **BUFR data** U,V,T,Q (10daily)
 - SSM/I sea wind scalar x ERA40 wind direction (10daily)
 - Ocean:
 - T/P altimeter data(10daily)
 - Reynolds SST (10daily)
 - **WOA data** T,S (monthly)
 - Ocean Data Assimilation Product T,S(monthly)
- **Adjoint Code**
 - **Adjoint** OGCM and **adjoint** AGCM are coupled [Line by line transformation by TAMC,TAF]
 - **Temporal averaging** of forward field for the adjoint integration is applied to smooth the basic field
 - Adjoint AGCM contains **damping terms** to suppress the strong adjoint sensitivity from weather fluctuations.

$$-\frac{\partial \lambda}{\partial t} = \left(\frac{\partial \mathbf{M}}{\partial \mathbf{x}} \right)_{\mathbf{x}=\bar{\mathbf{x}}}^T \lambda - \Gamma \lambda + \mathbf{H}^T \mathbf{R}^{-1} (\mathbf{H} \bar{\mathbf{x}} - \mathbf{y})$$

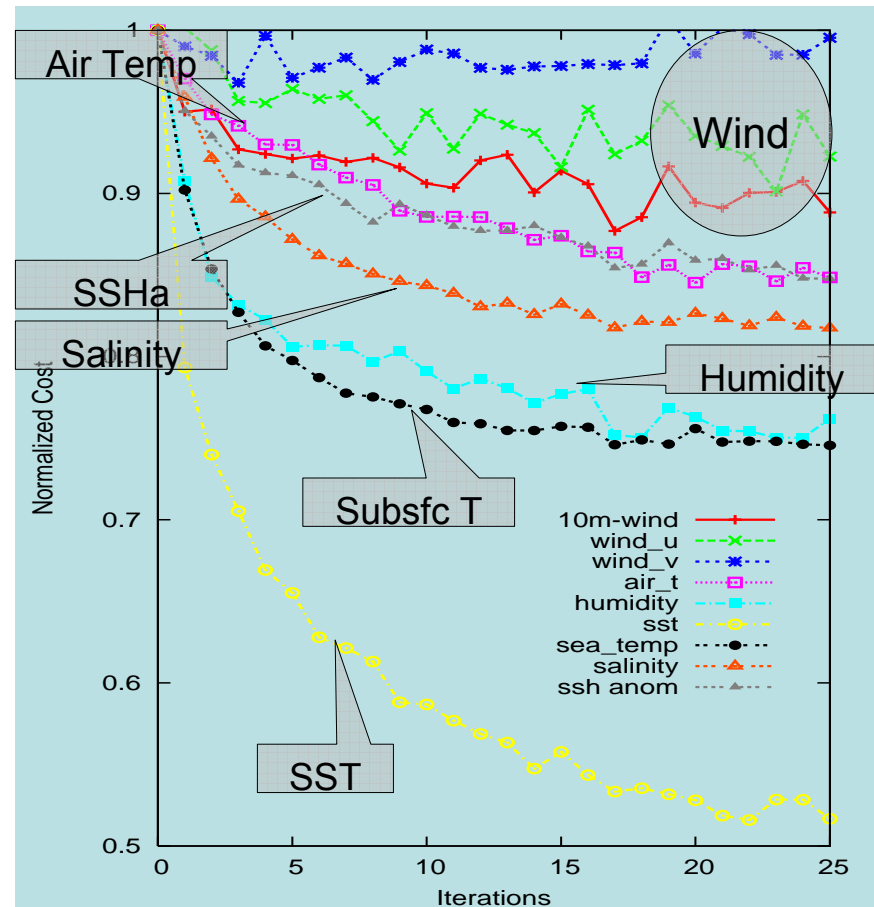
λ : adjoint variables, $\bar{\mathbf{x}}$: temporal average, $-\Gamma \lambda$: damping.

The CDA cost function minimisation

Cost variation for the period from Jul1996

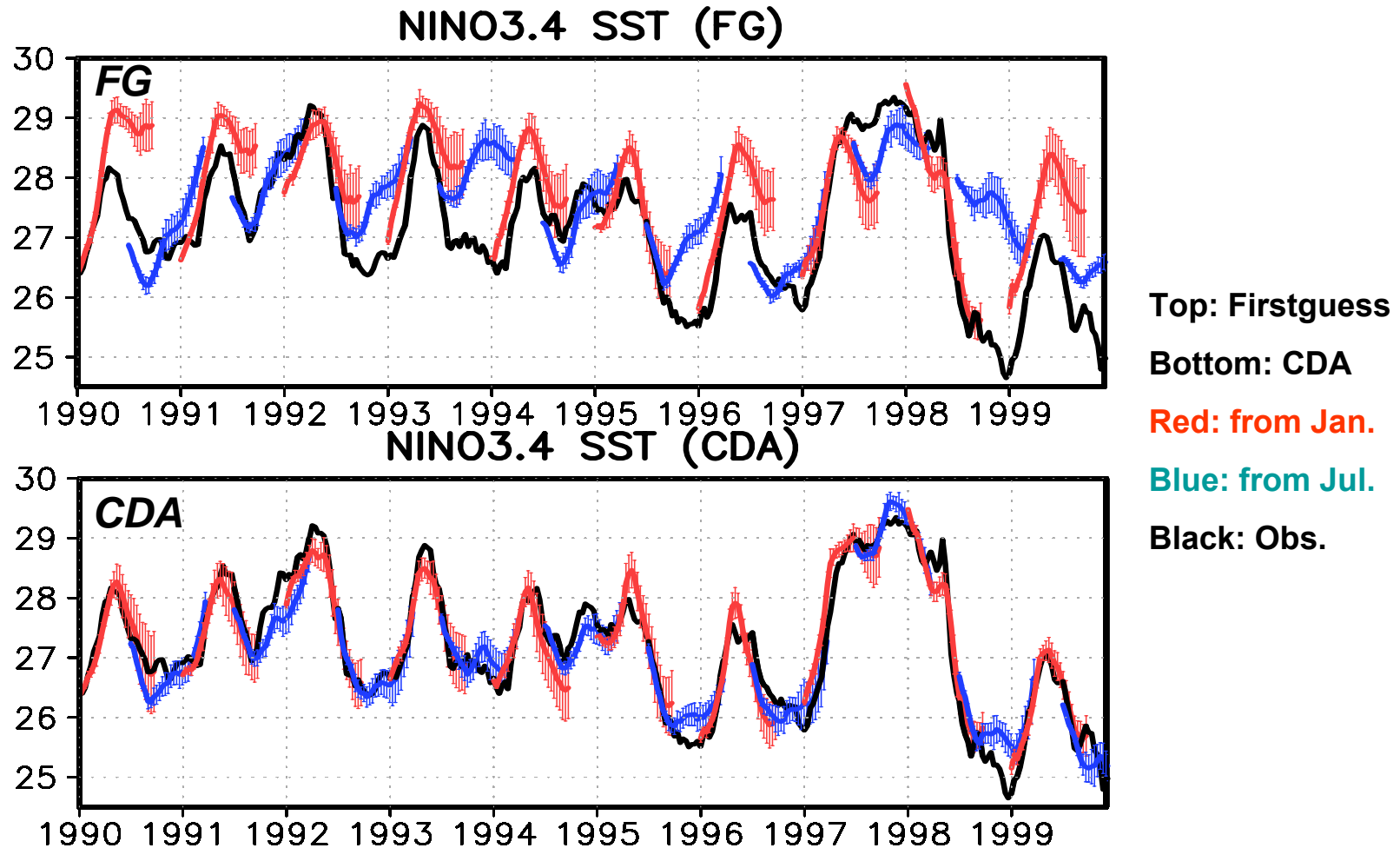


Normalized cost variation in the 1990s



Atmospheric cost terms show some fluctuations with iteration. SST cost significantly reduced.

Coupled DA Seasonal prediction



Error bars are for the spread of ensemble runs with 11-different atmospheric initial conditions. Nino3.4 SST is much more realistic in the CDA analysis field.

Coupled DA Summary

- The **optimizations** of ocean initial condition and of bulk parameters enable us to reproduce coupled field realistically.
 - **Extraction of coupled/climate mode** works to some extent by temporal averaging of forward fields and simple damping terms in adjoint code which is shown by the reduction of the cost values for coupled field.
 - Regarding El Nino, the departures from observation do not grow in the 9-month assimilation windows which verifies that our CDA works properly as a **smoother**.
- This system is also useful for **prediction**.
 - **Bulk parameter adjustment** will be useful to represent properly the climatological mean state by the Coupled GCM.
 - Optimal **ocean initial condition** fit to the coupled model useful for Seasonal-Interannual prediction because it contains proper tendency information thanks to the 4d-Var and hence **Reduces Shocks**.

Hadley Centre Decadal Prediction (DePreSys)

HadCM3 coupled model

Assimilation: ANOMALY

- Atm. nudged to ERA15/40
- Ocean nudged to **filtered ocean T, S gridded anal. from HadCM3 Covariances** all the time running in coupled mode

Hindcast ensembles (4-9) generated every 3-6 months through 1979-2005

Skill in SST, OHC and global SAT assessed out to 9 years ahead

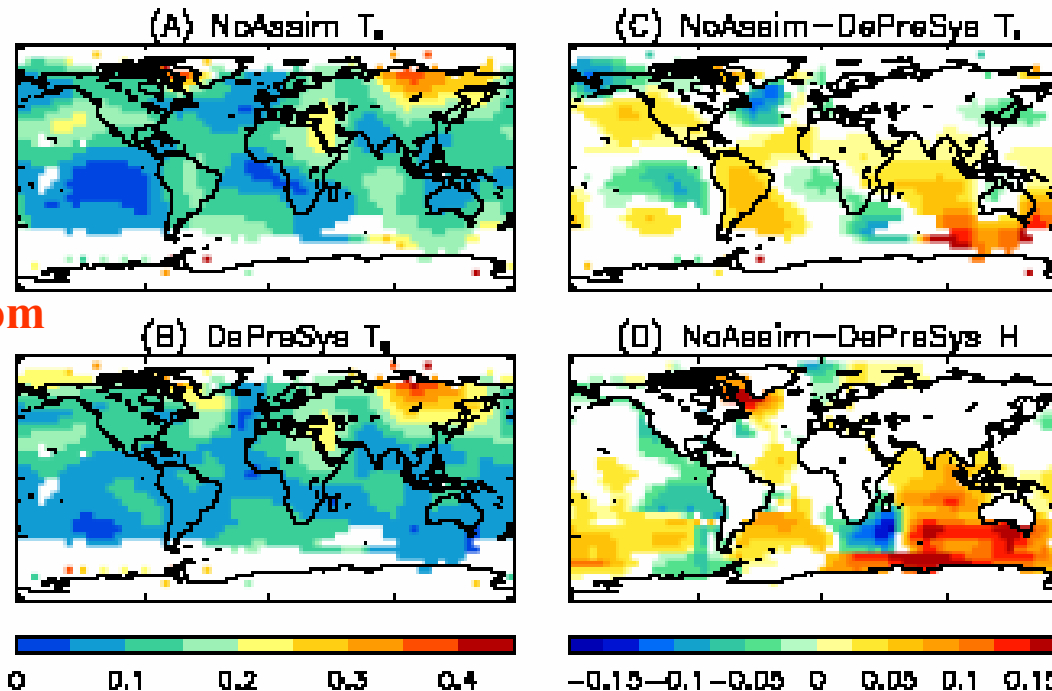


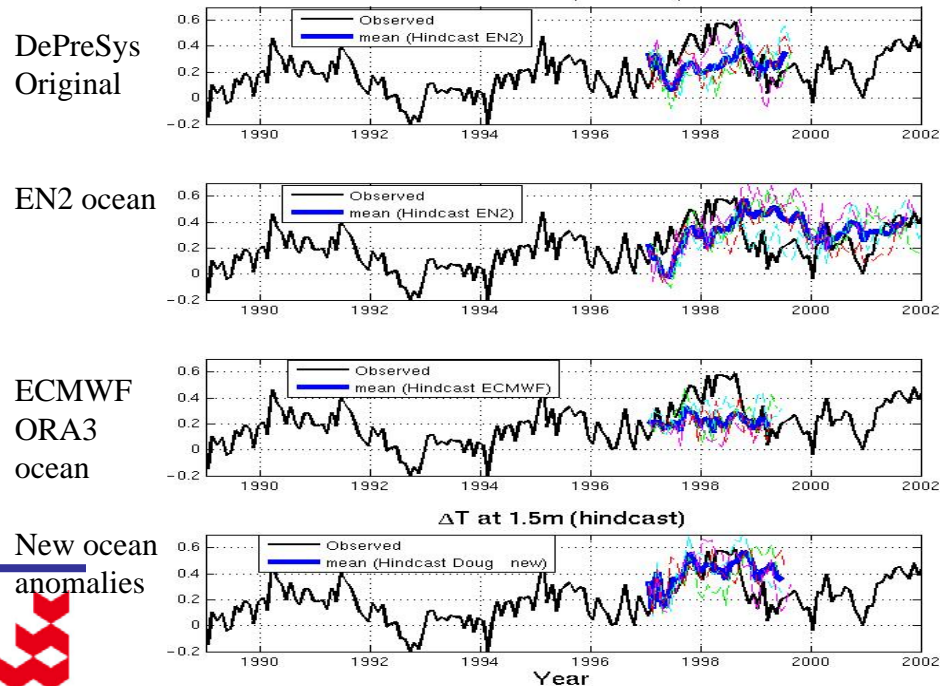
Figure 3: Impact of initial conditions on regional hindcast skill. (A) RMSE of 9-year mean T_s anomalies (relative to 1979-2001) for the ensemble-mean NoAssim hindcasts, verified against observations from HadCRUT2v (36–38). (B) As A but for DePreSys. (C) NoAssim minus DePreSys RMSE of 9-year mean T_s . Differences are only shown where they are significant at the 5% level (18). (D) As C but for 9-year mean H anomalies (relative to 1941-1996). In all panels, each 5° latitude by 5° longitude pixel represents the RMSE for predictions of T_s spatially averaged over the 35° latitude by 35° longitude box centred on that pixel.

Smith et al 2007 Science

Sensitivity of DePreSys system to Ocean Assimilation

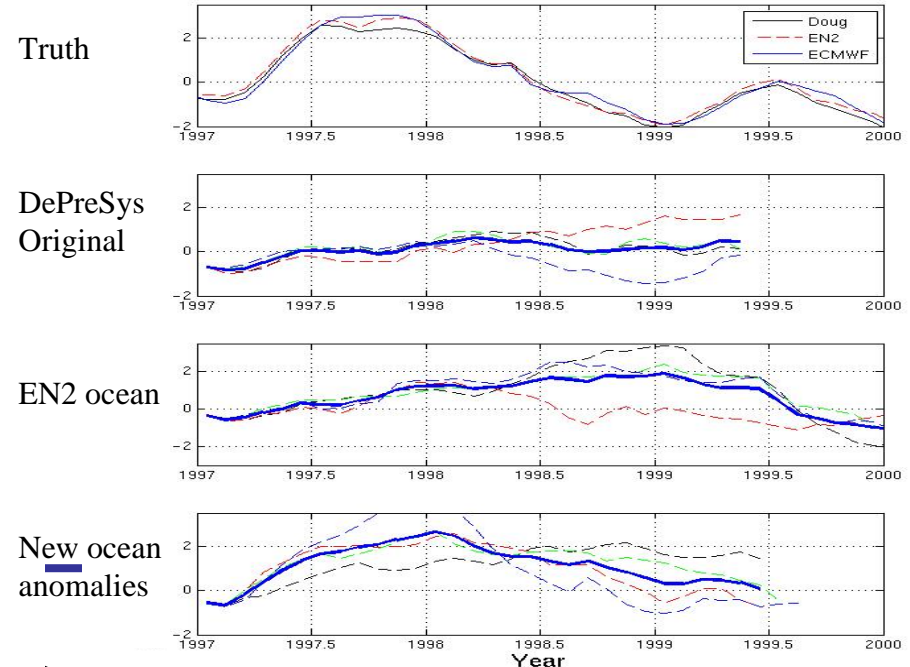
- DePreSys system implemented on set of NERC compute Clusters (GCEP project)
- Figures show Global surface air temperature and Nino3.4 hindcasts from Jan 1997 during the great 1997 ENSO
- Changing ocean initial conditions can give big increases in skill predicting both strength and timing of 1997 ENSO
- Will this carry over to skill statistics for interannual timescales?

Global Surface Air Temperature (STA) anomaly



ensemble_xabc_anomaly_v03e2.m

NINO 3.4 anomaly



Ensemble runs started from Jan 1997



Ocean DA Challenges

- To make most effective use of altimeter data in combination with new geoid data; ESA-GOCE mission
- Demonstrate effective combination of Argo and Altimeter data through DA and make critical OSE assessments
- Ocean reanalysis for climate? Can this be done more effectively than atmospheric reanalyses, eg. using slow thermodynamic timescales in the ocean? => CLIVAR-GSOP (Global Synthesis and Observations Panel)
- Initialising coupled atm.-ocean models for seasonal-decadal ensemble prediction
 - Huge implications if coupled predictions other than for ENSO can be demonstrated
- Many other ocean DA challenges not covered eg. coastal / biological / medium range NWP