



Diagnostics
MJR 1

ECMWF Annual Seminar 2008

Understanding the local and global impacts of model physics changes

Mark Rodwell
Work with Thomas Jung

4 September 2008

Thanks to: ...

Motivation

The real world and GCMs are complex systems ...

- Can use hierarchy of simpler models to understand processes and develop parametrizations.

But ...

- The fully complex system may behave differently. For example due to interactions.
- It is the fully complex system that is used to produce the forecast!

Hence ...

- There is a need to develop diagnostics that help us understand the physics, dynamics and interactions within the fully complex system.



Talk Outline

- **Annual cycle of the global circulation**
 - Systematic errors in seasonal integrations
 - Introduction to the case study: aerosol change
 - Statistically significant global changes
- **Understanding the local physics**
 - Analysis Increments and Initial Tendencies
 - Perturbed physics example: reducing climate change uncertainty
- **Understanding the tropic-wide response**
 - Tropical waves
 - Coupling with convection
- **Understanding the extra-tropical response**
 - The tropical control of the divergent wind
 - Balances in the vorticity equation
 - Extra-tropical physics and PV

Pedagogical!

See Rodwell & Jung (2008)

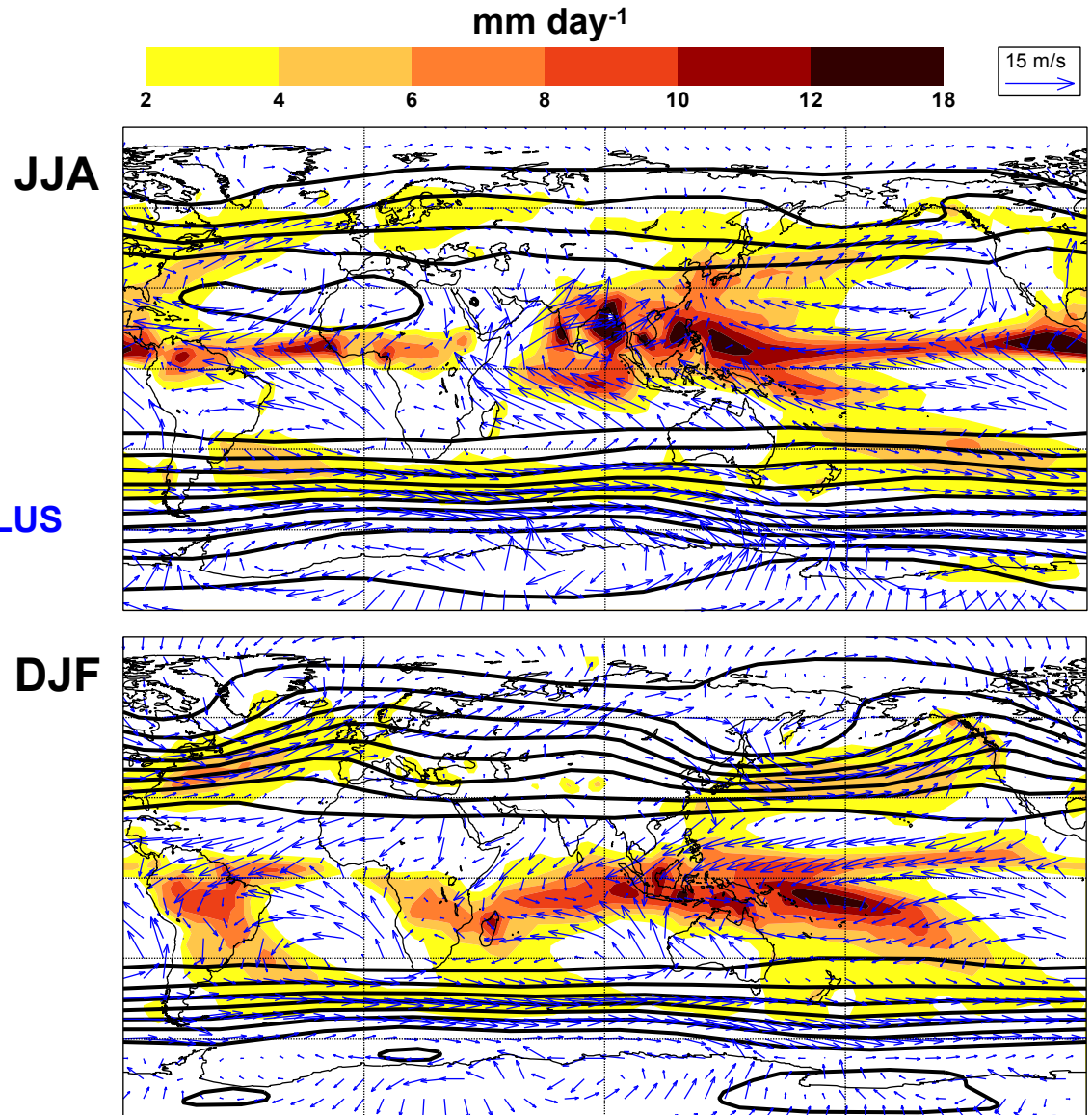


Diagnostics
MJR 4

Annual Cycle of the Global Circulation

Mean Annual Cycle: Precipitation, \underline{V}_{925} & Z_{500}

- INTER-TROPICAL CONVERGENCE ZONE
- MONSOONS
 - SEASONAL CYCLE OF RAINS
 - CONVECTIVE HEATING
- SUBTROPICAL ANTICYCLONES
 - DUALITY WITH MONSOON HEATING
 - RADIATIVELY IMPORTANT STRATOCUMULUS
 - DEEP CONVECTION (SPCZ ETC)
- EXTRATROPICAL STORMTRACKS
 - STRONG VORTICITY GRADIENTS
 - SENSITIVITY TO TROPICAL FORCING



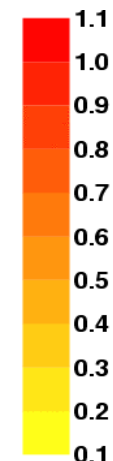
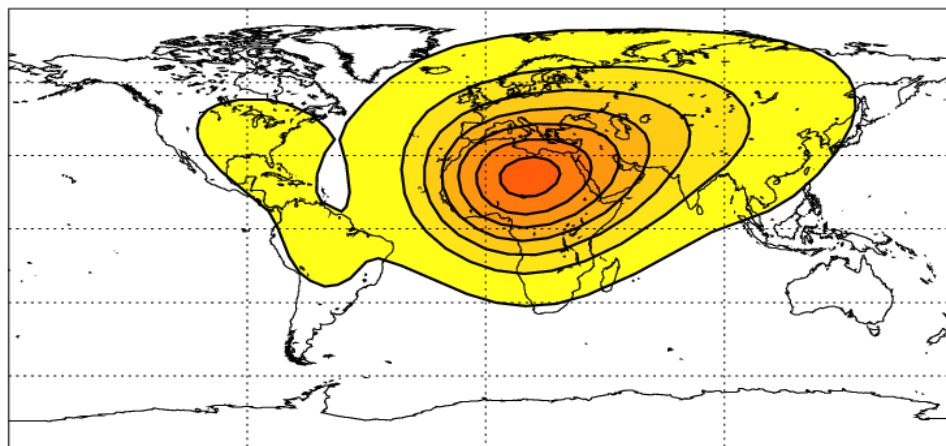
Precipitation: Xie-Arkin 1979/80 – 1998/99

\underline{V}_{925} : ERA40 1962-01

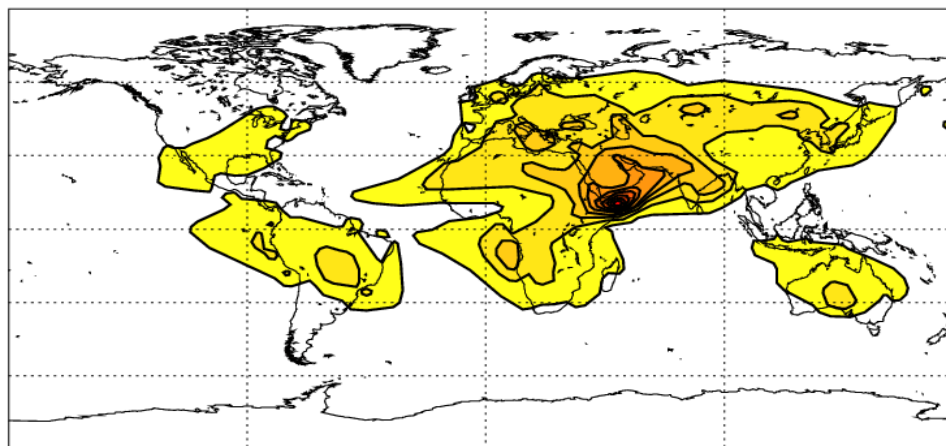
Z_{500} : ERA40 1962-01, CI=10 dam

Old and New Aerosol Optical Thickness

OLD
(NO ANNUAL CYCLE)



NEW
(JULY)



**OPTICAL
DEPTH d AT
550nm**

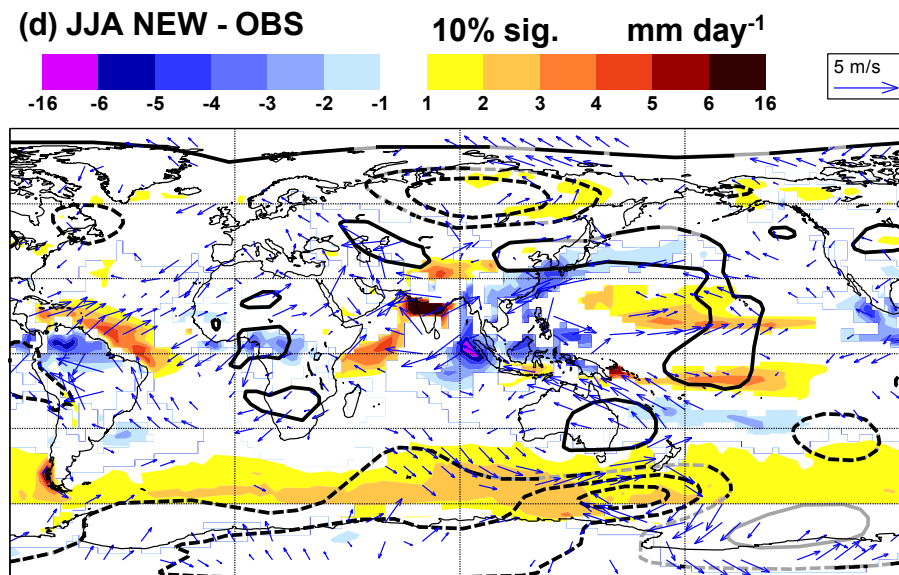
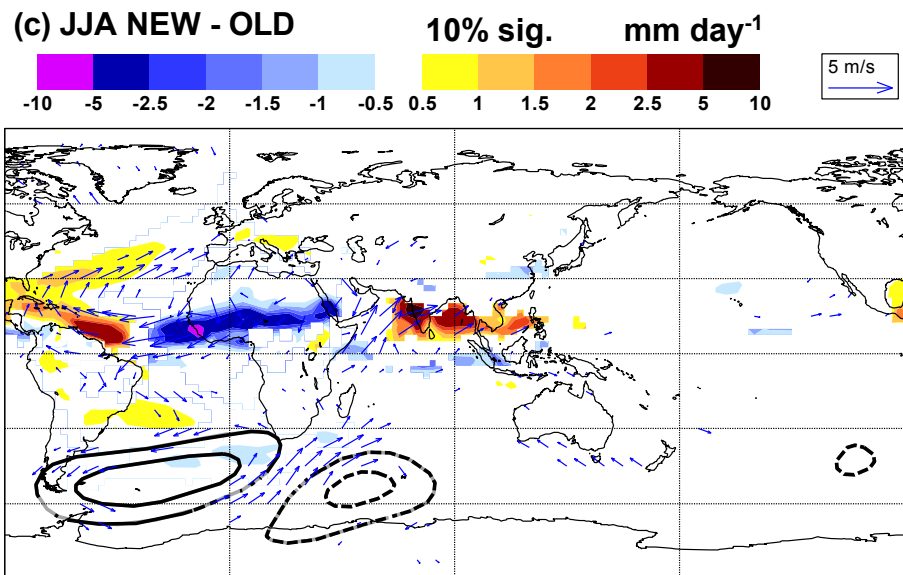
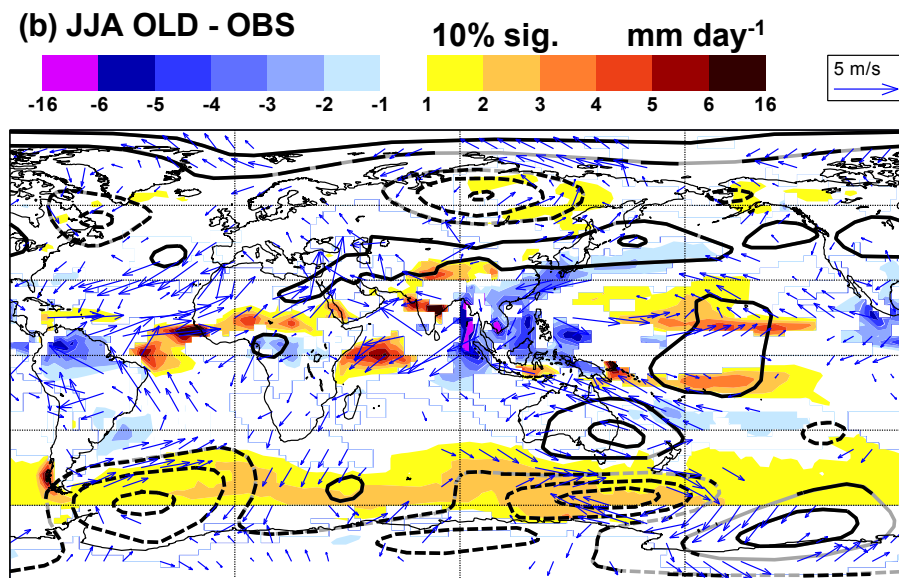
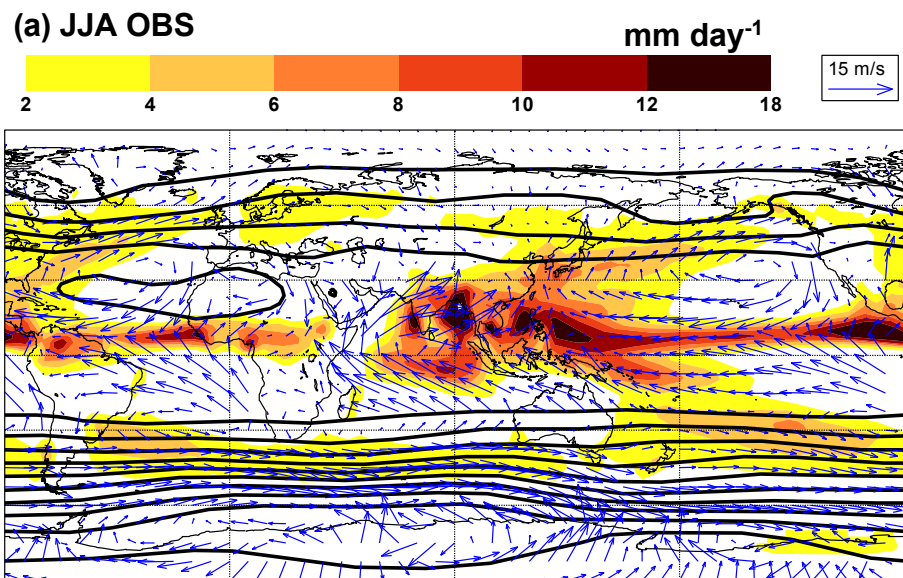
**ATTENUATION
FACTOR = e^{-d}**

**SINGLE
SCATTERING
ALBEDO FOR
DESERT
AEROSOL ≈ 0.9**

- **SOIL DUST IS IMPORTANT**
- **SOIL DUST ABSORBS AS WELL AS SCATTERS**

Old: C26R1 (Tanre et al. 1984), New: C26R3 (Tegen et al. 1997).

June – August Precipitation, v925 and Z500



Precip: Xie-Arkin 1980–1999. v925, Z500: ERA40 1962-01, (a) 10, (b)-(d) 2 dam. 26R3 seasonal data for the same period



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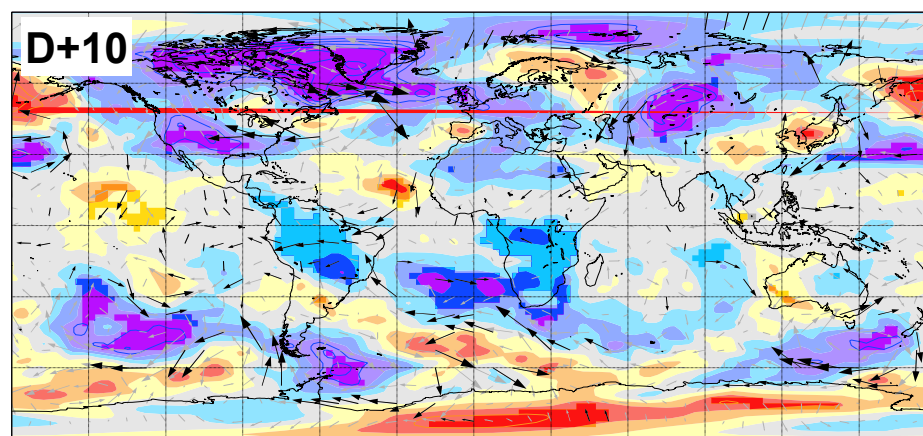
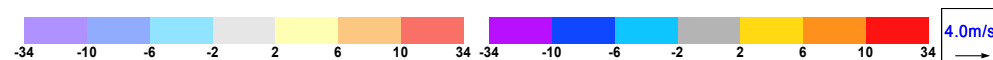
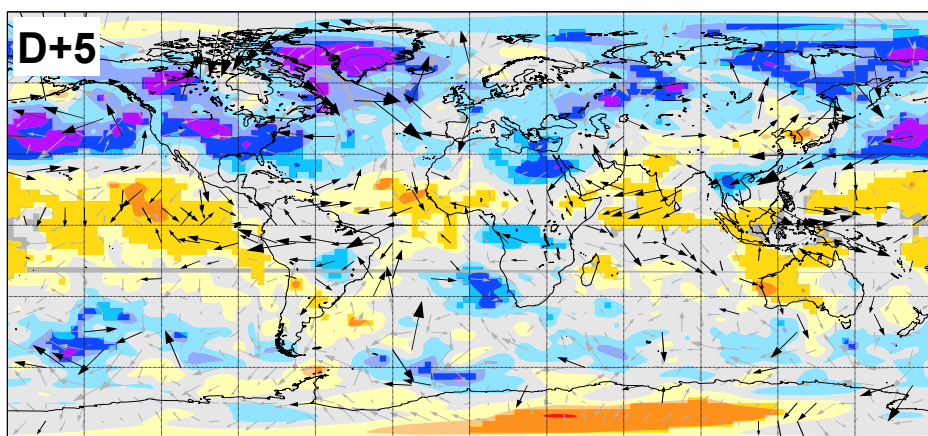
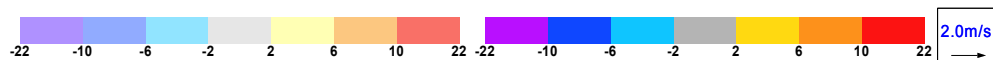
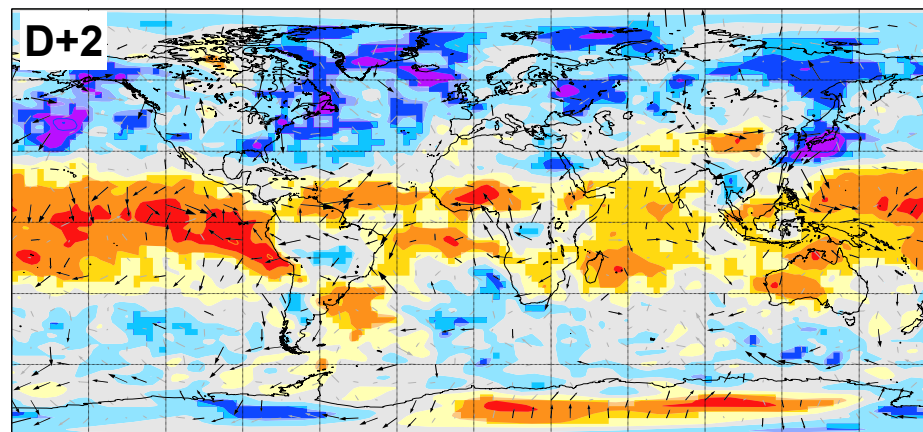
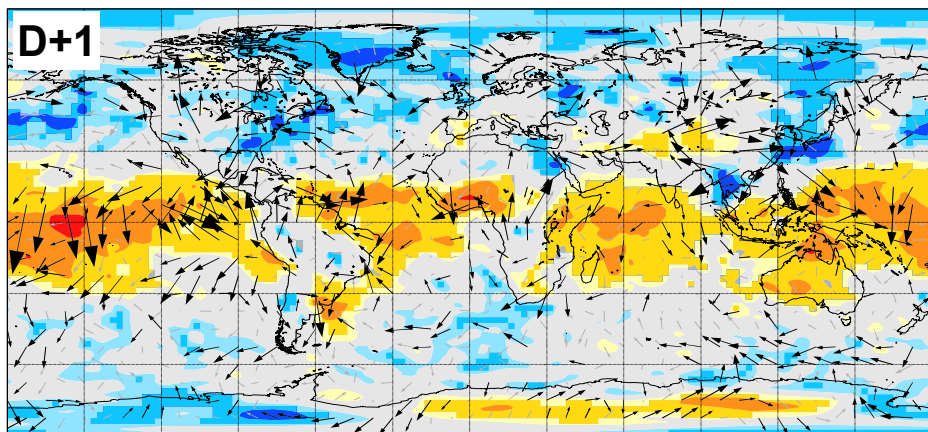
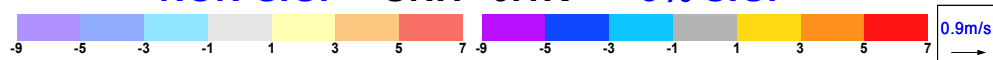
Understanding the Local Physics



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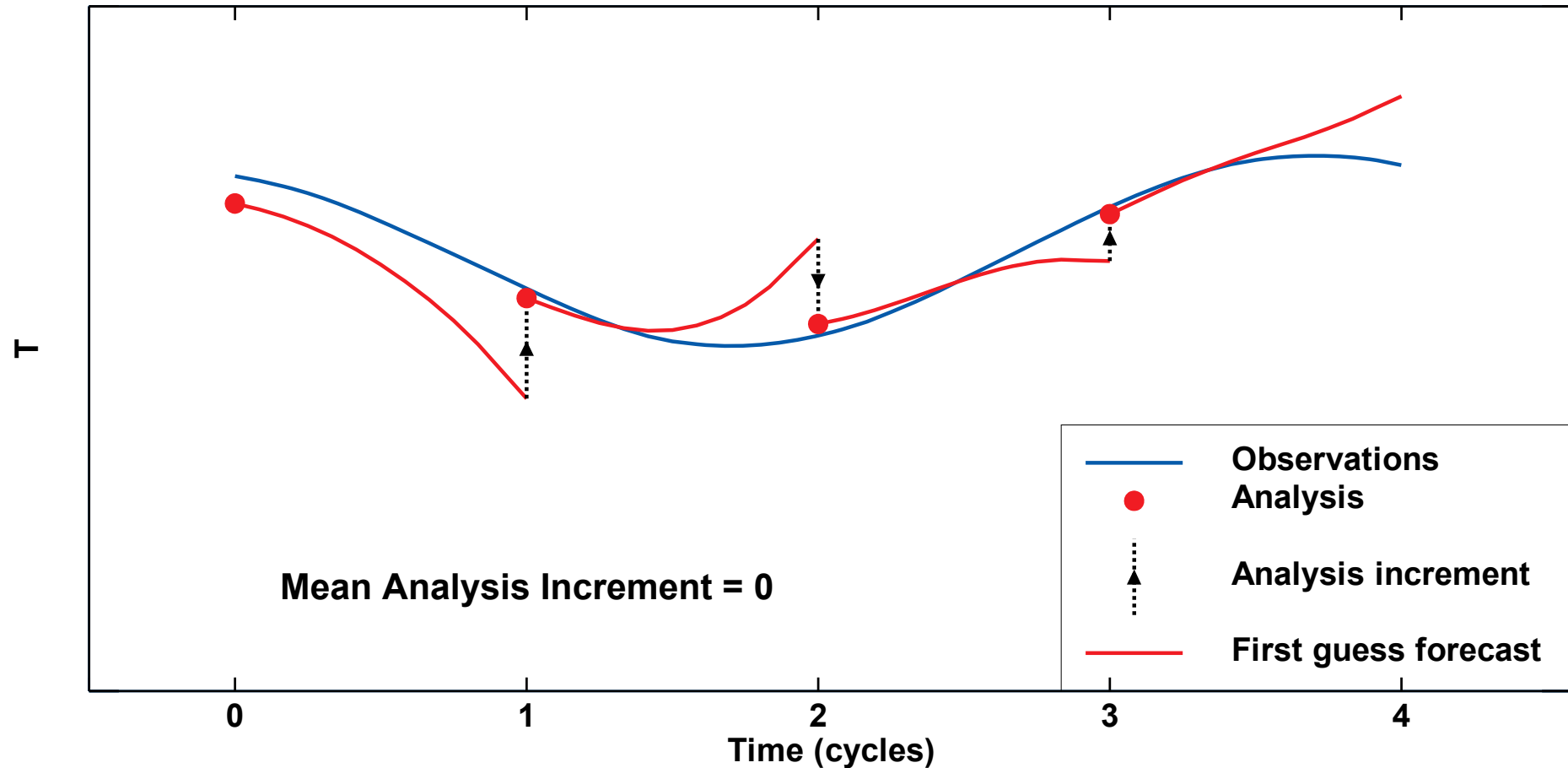
DJF T500 Medium-range Mean Forecast Error

NON-SIG. UNIT=0.1K 5% SIG.



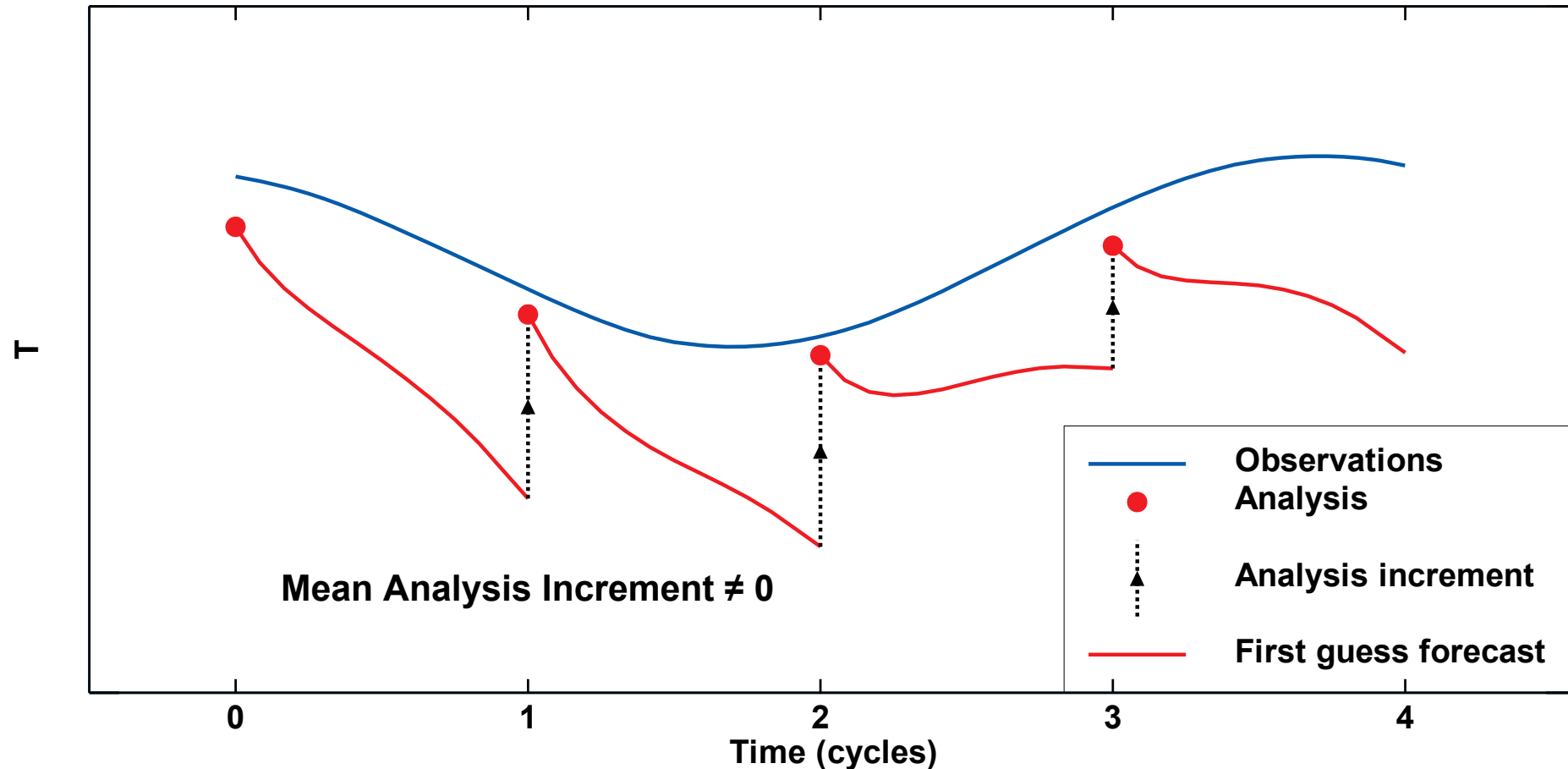
Based on DJF 2006/7 operational analyses and forecasts. Significant values (5% level) in deep colours.

Data Assimilation Cycle: Perfect Model



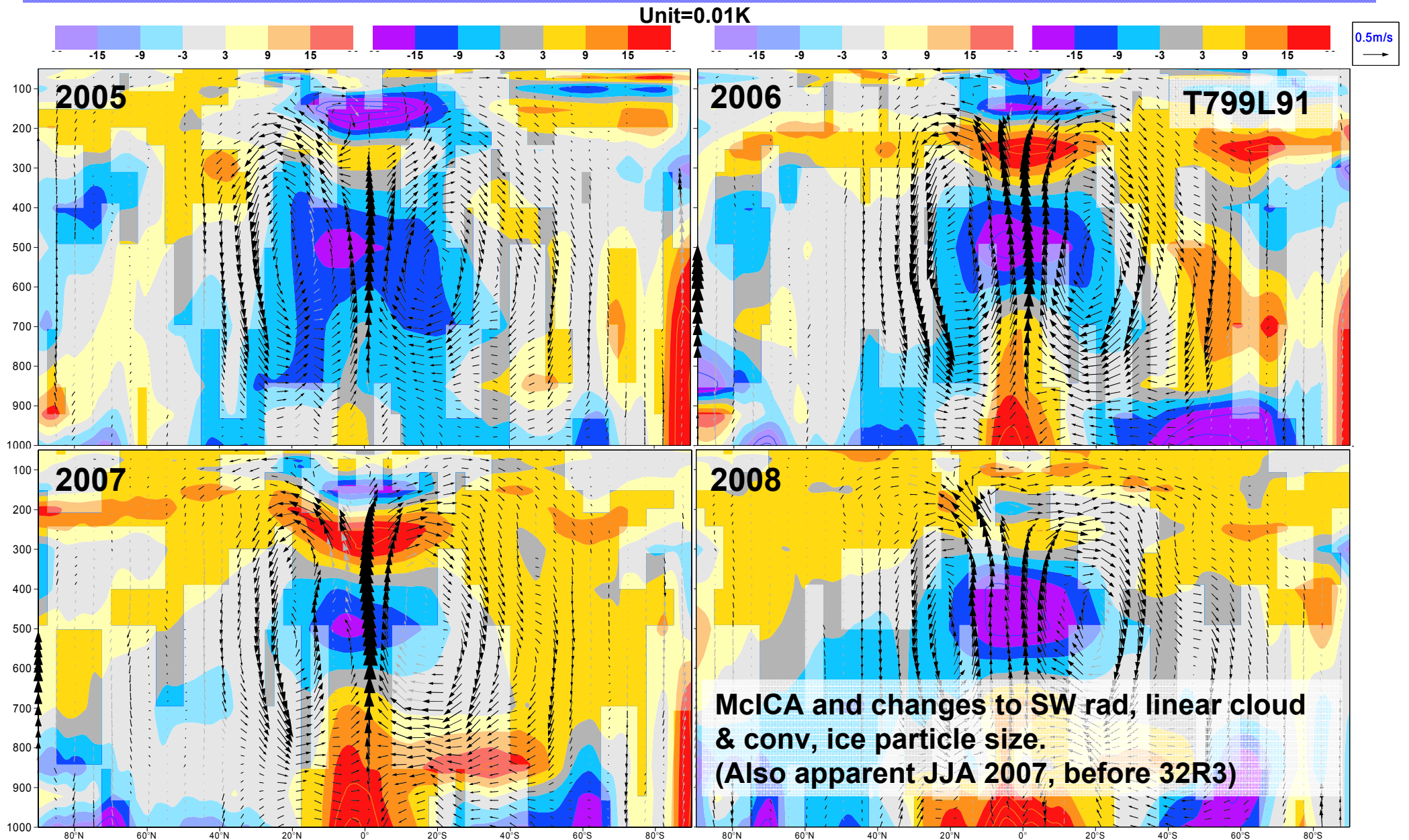
(Imperfect, unbiased observations)

Data Assimilation Cycle: Imperfect Model

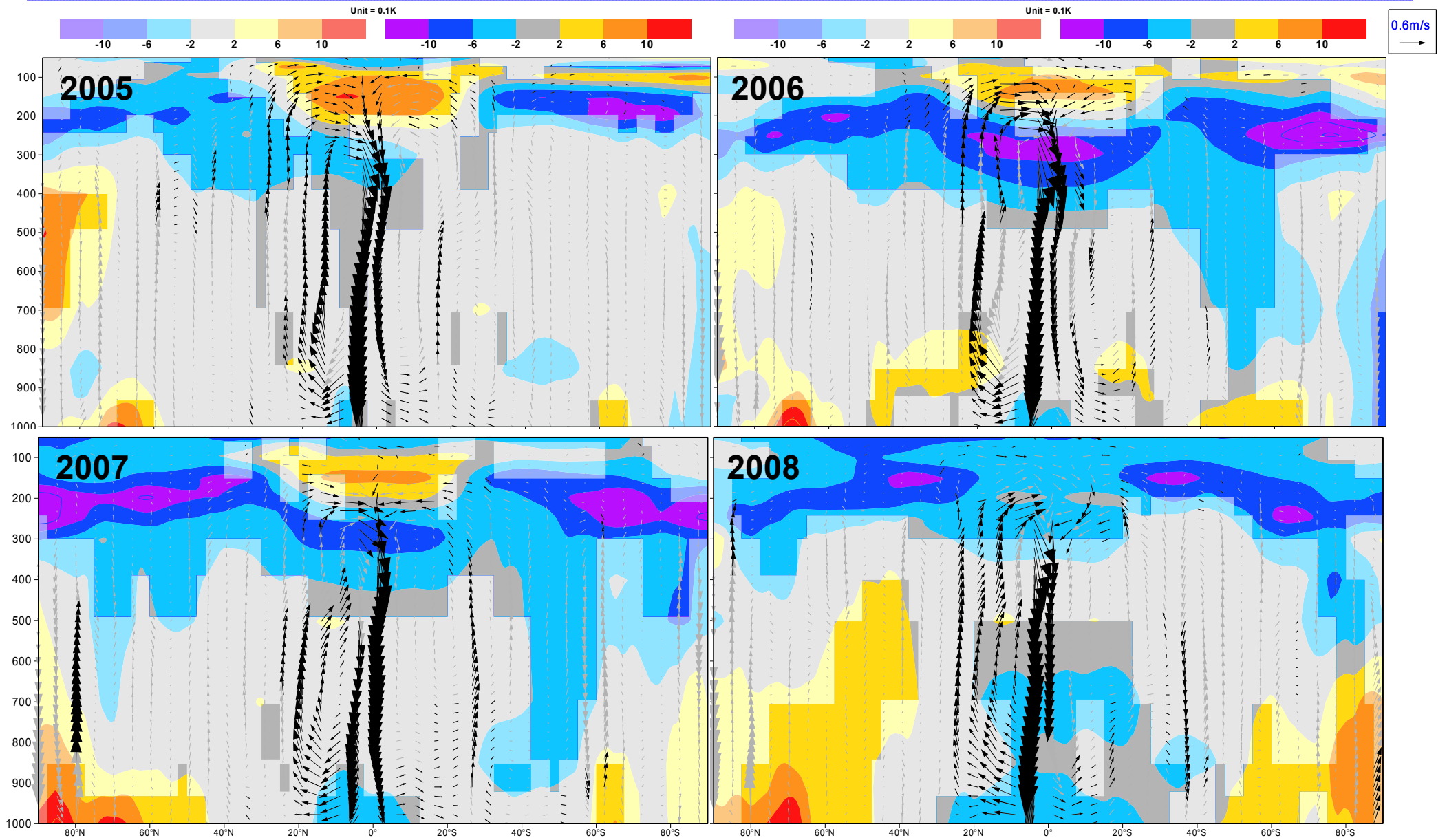


- Mean Analysis Increment = Mean Net Initial Tendency ("I.T." in, e.g., $K\text{cycle}^{-1}$)
- = Mean Convective I.T. + Mean Radiative I.T. + ... + Mean Dynamical I.T.
(summed over all processes in the model)

MAM Mean Analysis Increments: T and (v,w)



MAM Mean Forecast Error D+5: T and (v,w)



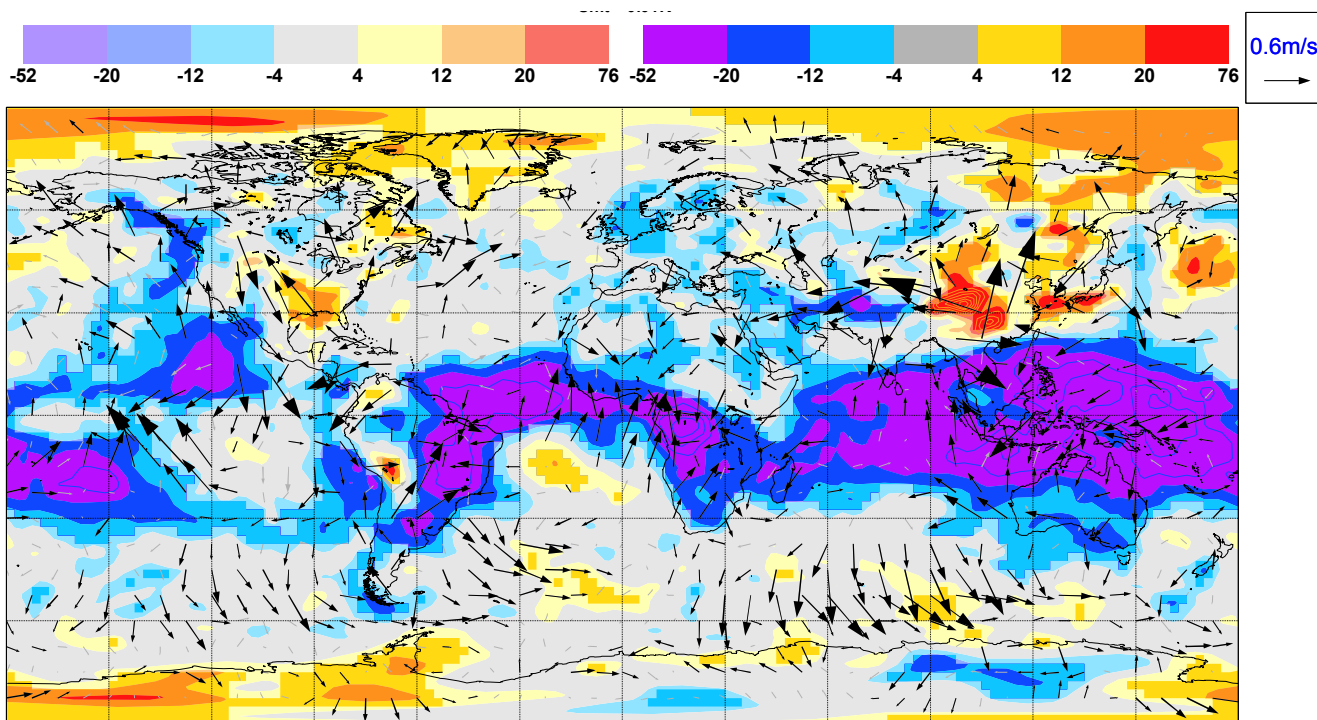


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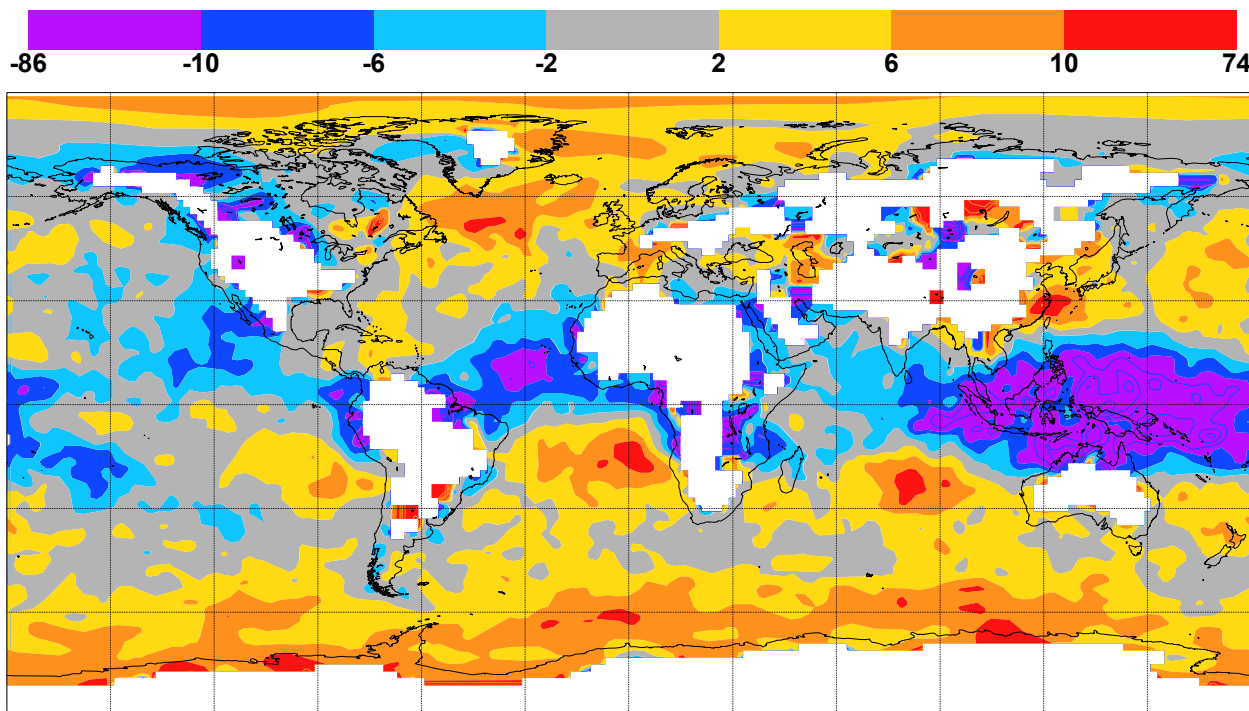
Confronting models with observations

T500 Analysis Increment

UNIT=0.01K



UNIT=0.01K



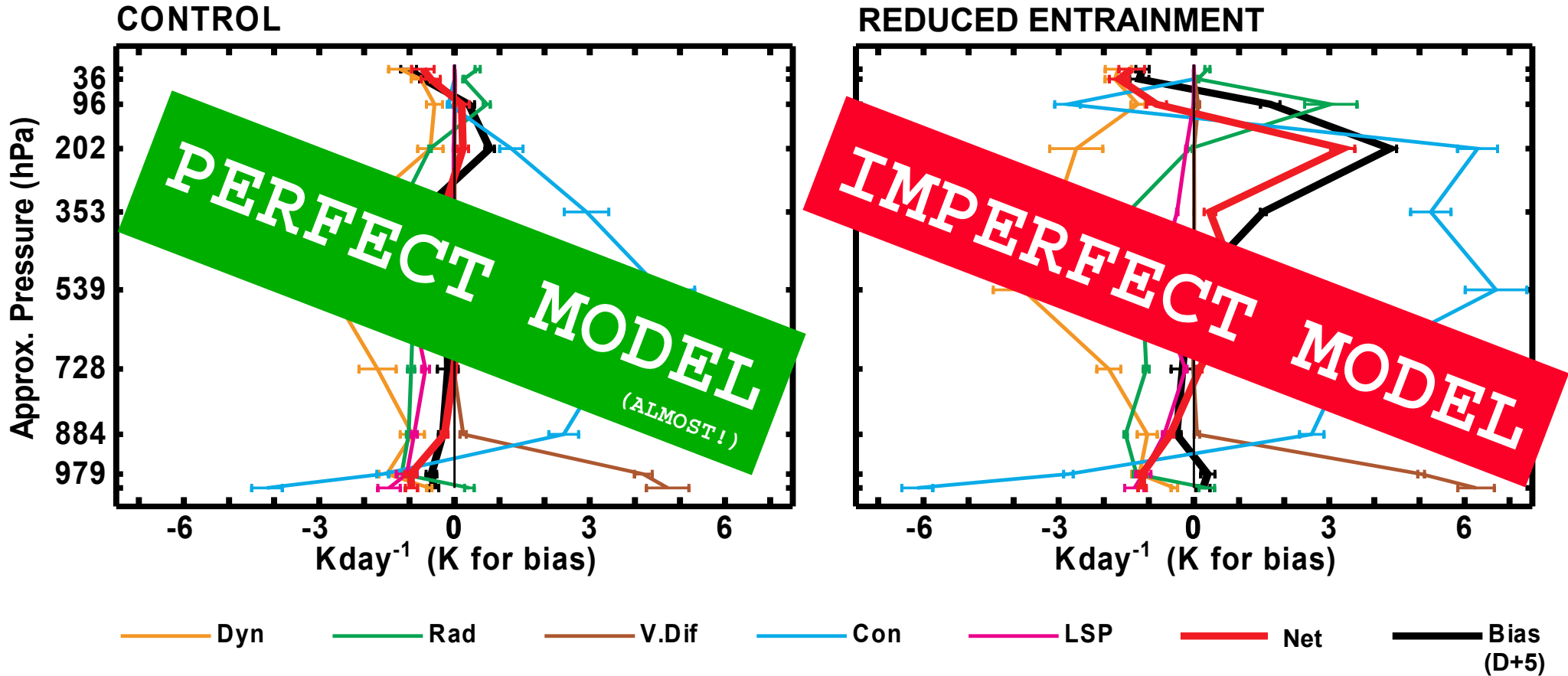
See Rodwell & Jung, ECMWF
Newsletter Autumn 2008

Observed – First Guess
Brightness Temperature
AIRS ch 215 (~T500)

DJF 2007/8



Amazon Initial Process Tendencies

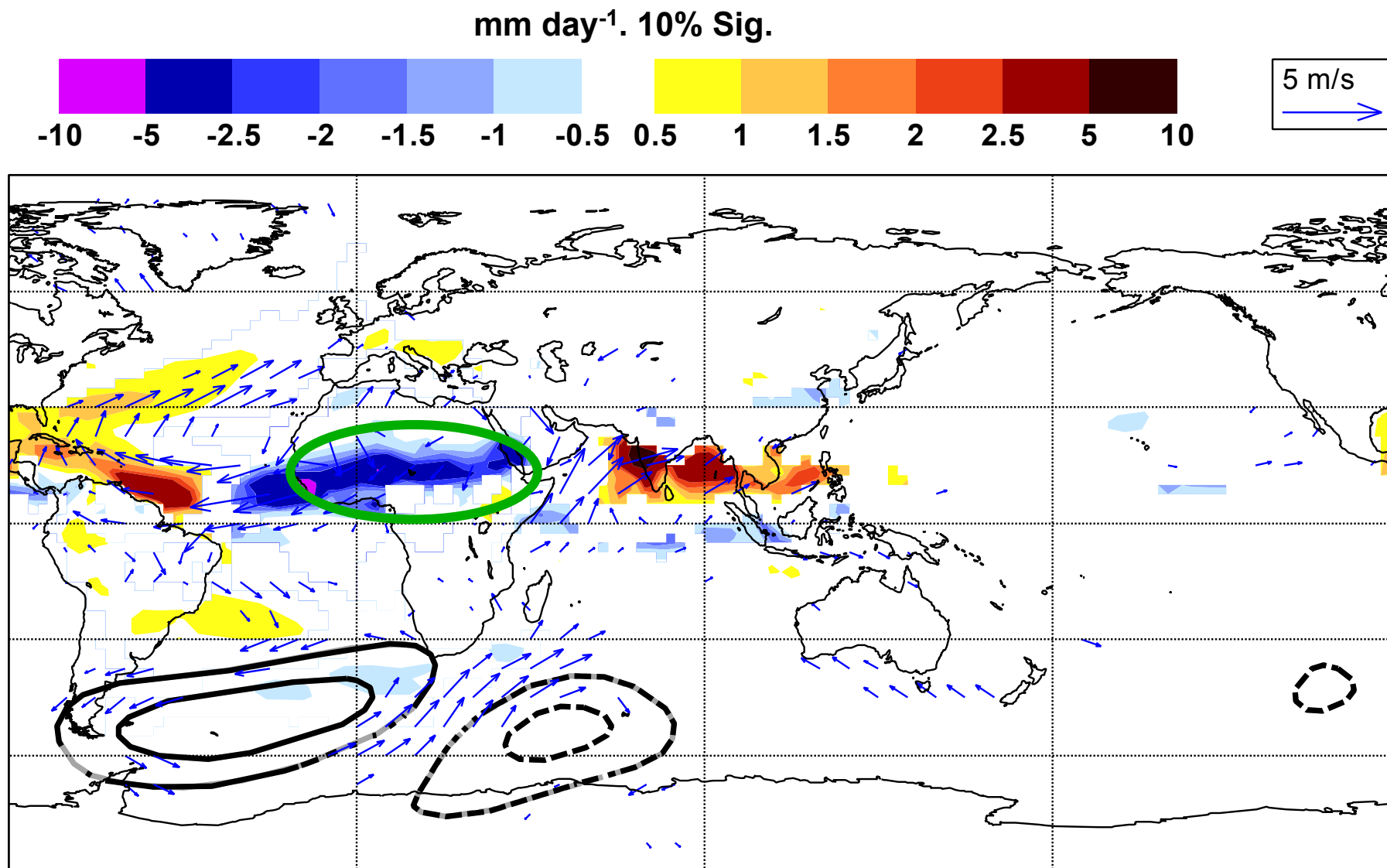


**PROCESS TENDENCIES
BALANCE WELL – LEADING TO
A SMALL NET TENDENCY**

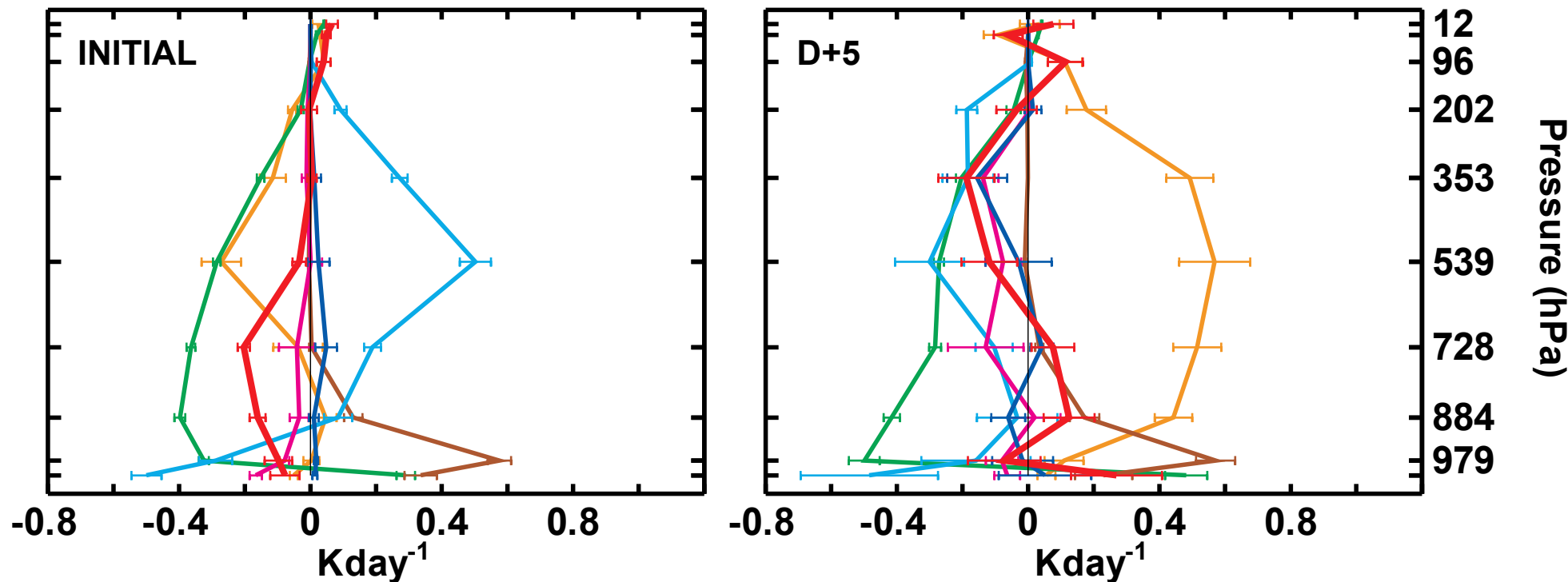
**IMBALANCE LEADS TO LARGE
NET TENDENCIES – INDICATIVE
OF PHYSICS ERROR**

Amazon = [300°E-320°E, 20°S-0°N]. Mean of 31 days X 4 forecasts per day X 12 timesteps per forecast (January 2005). 70% confidence intervals are based on daily means. CONTROL model = 29R1,T159,L60,1800S.

JJA Precipitation, ν_{925} and Z500. New-Old



North Africa Jul 2004 T Tendencies (New-Old)



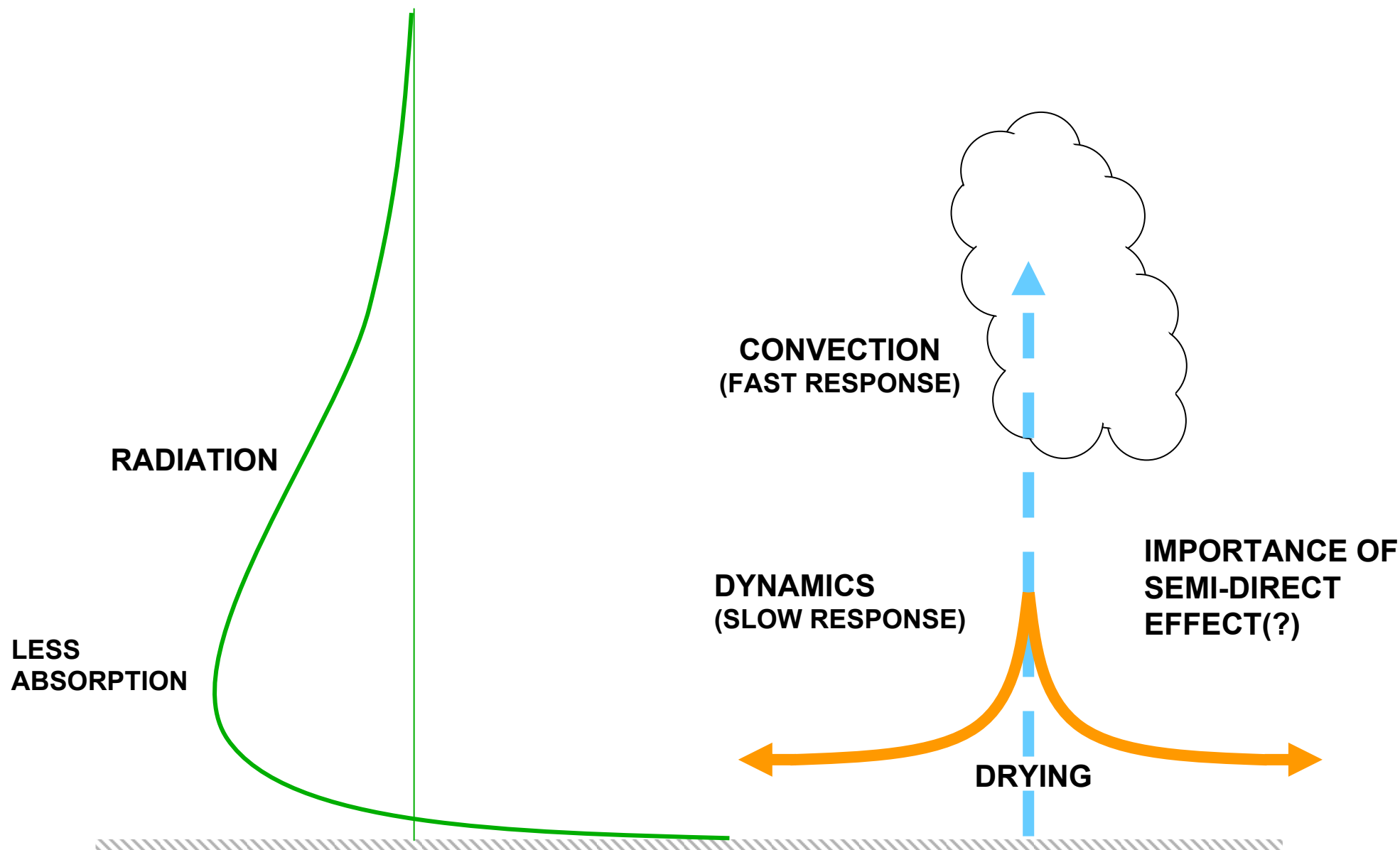
— Dyn
 — Rad
 — V.Dif
 — Con
 — LSP
 — Tot

**RADIATION CHANGES
DESTABILISE PROFILE AND
LEAD TO MORE CONVECTION ...**

**... BUT ULTIMATELY LEAD TO
MORE DESCENT AND LESS
OVERALL PRECIPITATION**

North Africa = $[5^{\circ}\text{N}-15^{\circ}\text{N}, 20^{\circ}\text{W}-40^{\circ}\text{E}]$. Mean of 31 days X 4 forecasts per day X 12 timesteps per forecast.
70% confidence intervals are based on daily means. CONTROL model = 29R1,T159,L60,1800S.

Local Response to Aerosol Reduction

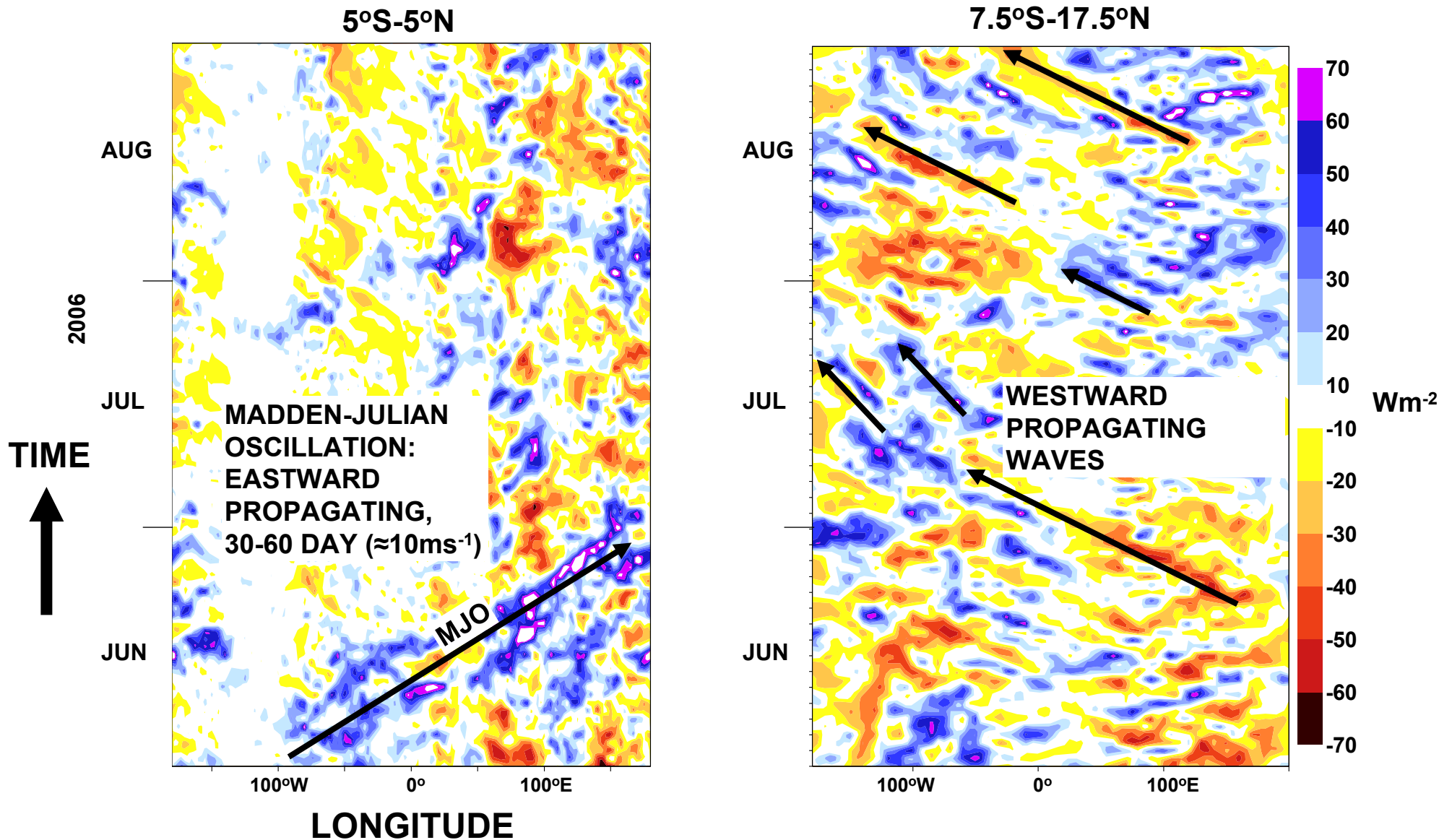




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Understanding the Tropic-wide Response

Tropical Waves: Outgoing Long-wave Radiation

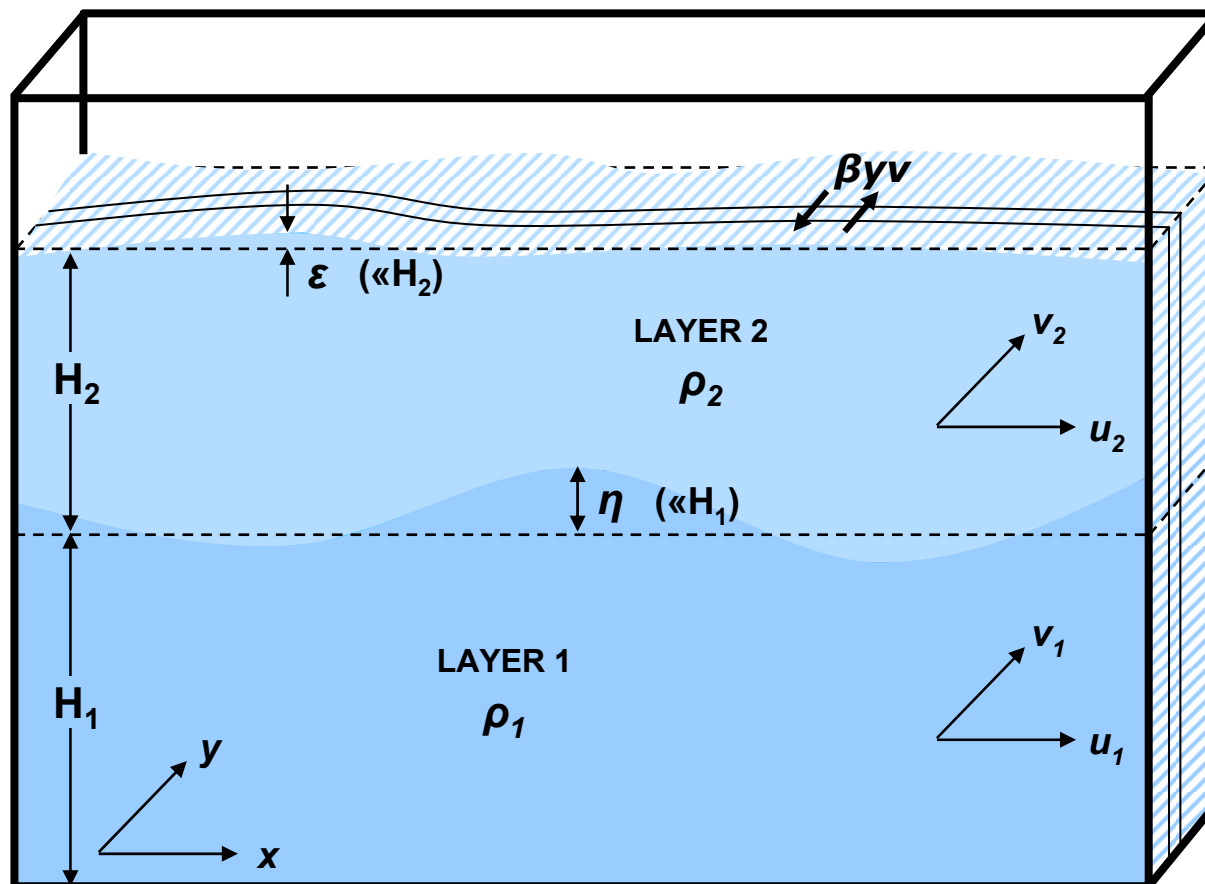


Plots from Thomas Jung. OLR data from NOAA



Shallow Water Equations on the β -plane

(Here, for understanding tropical atmospheric waves)



Baroclinic mode:

$$\varepsilon \ll \eta \quad \begin{aligned} u &\equiv u_1 - u_2 \\ v &\equiv v_1 - v_2 \end{aligned}$$

Momentum:

$$\frac{\partial u}{\partial t} - \beta y v + g' \frac{\partial \eta}{\partial x} \approx 0$$

$$\frac{\partial v}{\partial t} + \beta y u + g' \frac{\partial \eta}{\partial y} \approx 0$$

Continuity:

$$\left(\frac{1}{H_1} + \frac{1}{H_2} \right) \frac{\partial \eta}{\partial t} + \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \approx 0$$

Solving for v:

$$\frac{\partial}{\partial t} \left\{ \frac{\partial^2 \mathbf{v}}{\partial t^2} + \beta^2 y^2 \mathbf{v} - c_e^2 \left(\frac{\partial^2 \mathbf{v}}{\partial x^2} + \frac{\partial^2 \mathbf{v}}{\partial y^2} \right) \right\} - c_e^2 \beta \frac{\partial \mathbf{v}}{\partial x} = 0$$

$$g' \equiv g \left(1 - \frac{\rho_2}{\rho_1} \right) \quad \text{"reduced gravity"}$$

$$c_e^2 \equiv g' \frac{H_1 H_2}{H_1 + H_2} \equiv g H_e \quad c_e \approx 20 \text{ to } 80 \text{ms}^{-2}$$

c_e is the propagation speed of a barotropic gravity wave in single layer of depth H_e .

Free Equatorial Waves

$V=0$:

$$u = u_0 e^{-y^2/2} e^{ik(x-c_e t)}$$

East propagating **Kelvin Wave**

- Non-dispersive
- In geostrophic balance

$V \neq 0$:

$$v = \hat{v}(y) e^{i(kx - \omega t)}$$

Substitute into equation for v

Structures

(Meridional structures are solutions to Schrodinger's simple harmonic oscillator)

$$\hat{v}(y) = \begin{bmatrix} 1 \\ 2y \\ 4y^2 - 1 \\ 8y^3 - 12y \\ \vdots \\ H_n(y) \end{bmatrix} e^{-y^2/2}$$

Hermite Polynomials: $H_n(y)$

- Each successive polynomial has one more node
- Modes alternate asymmetric / symmetric about equator

Dispersion

(How phase speed is related to spatial scale)

$$\left(\frac{\omega^2}{c_e^2} - k^2 - \frac{\beta k}{\omega} \right) = (2n+1) \frac{\beta}{c_e}$$

$(n = 0, 1, 2, \dots)$

For $n \neq 0$: 3 values of ω for each k

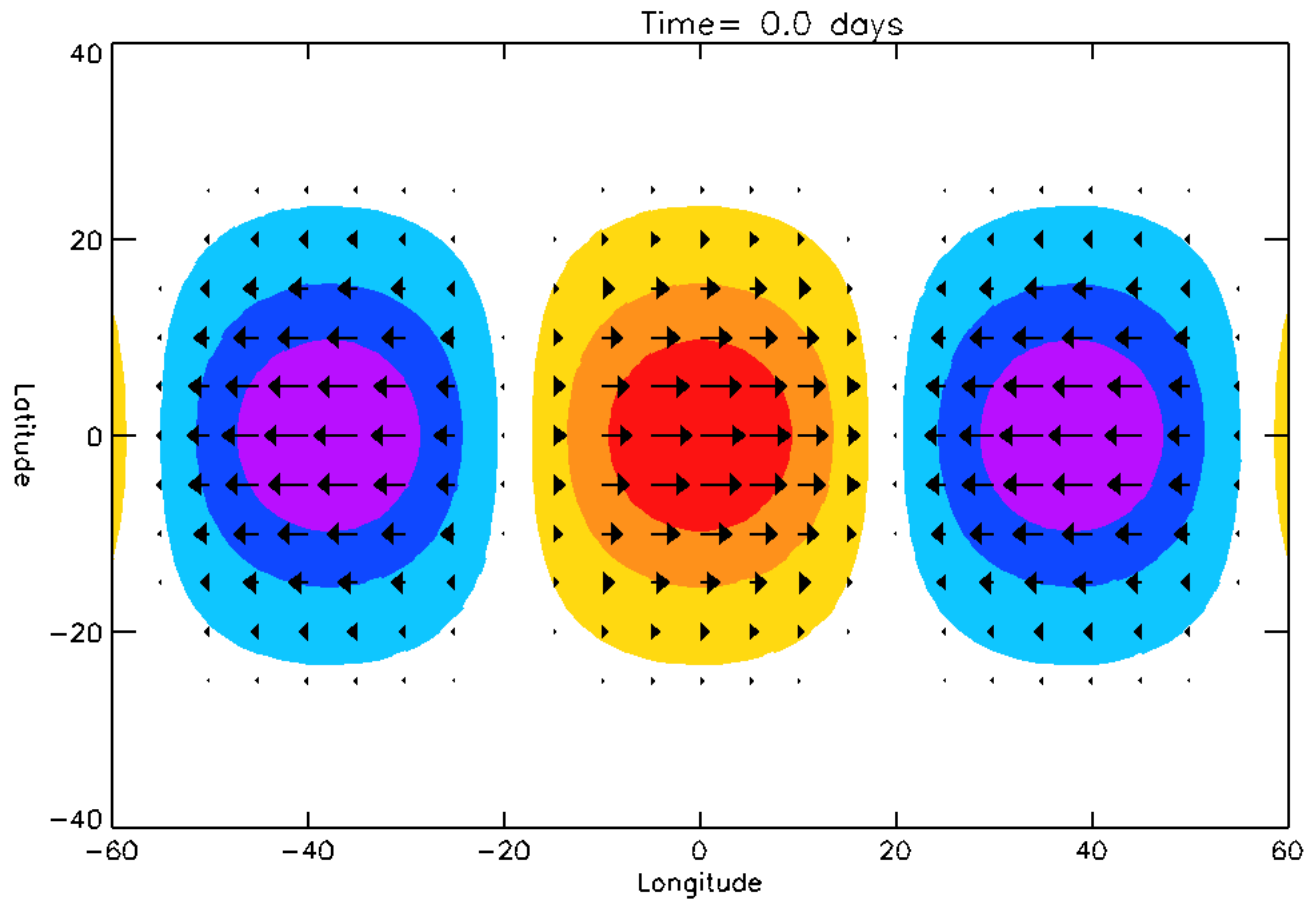
- West propagating **Rossby Wave**
- E & W propagating **Gravity Wave**

For $n=0$: 2 values of ω for each k

- E & W prop. **Mixed Rossby-Gravity**

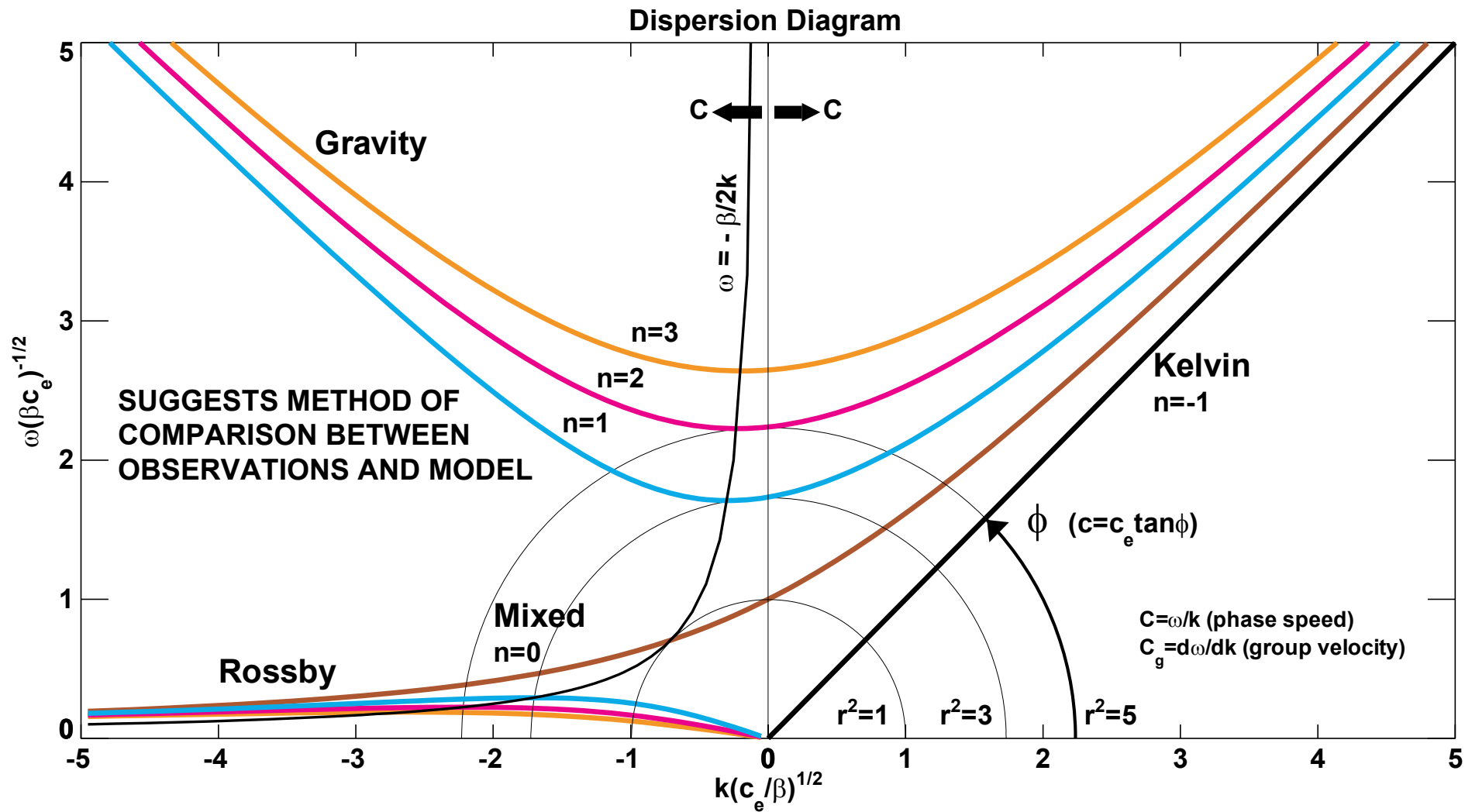
y has been non-dimensionalised by the factor $(\beta/c_e)^{1/2}$

Wave Spotting

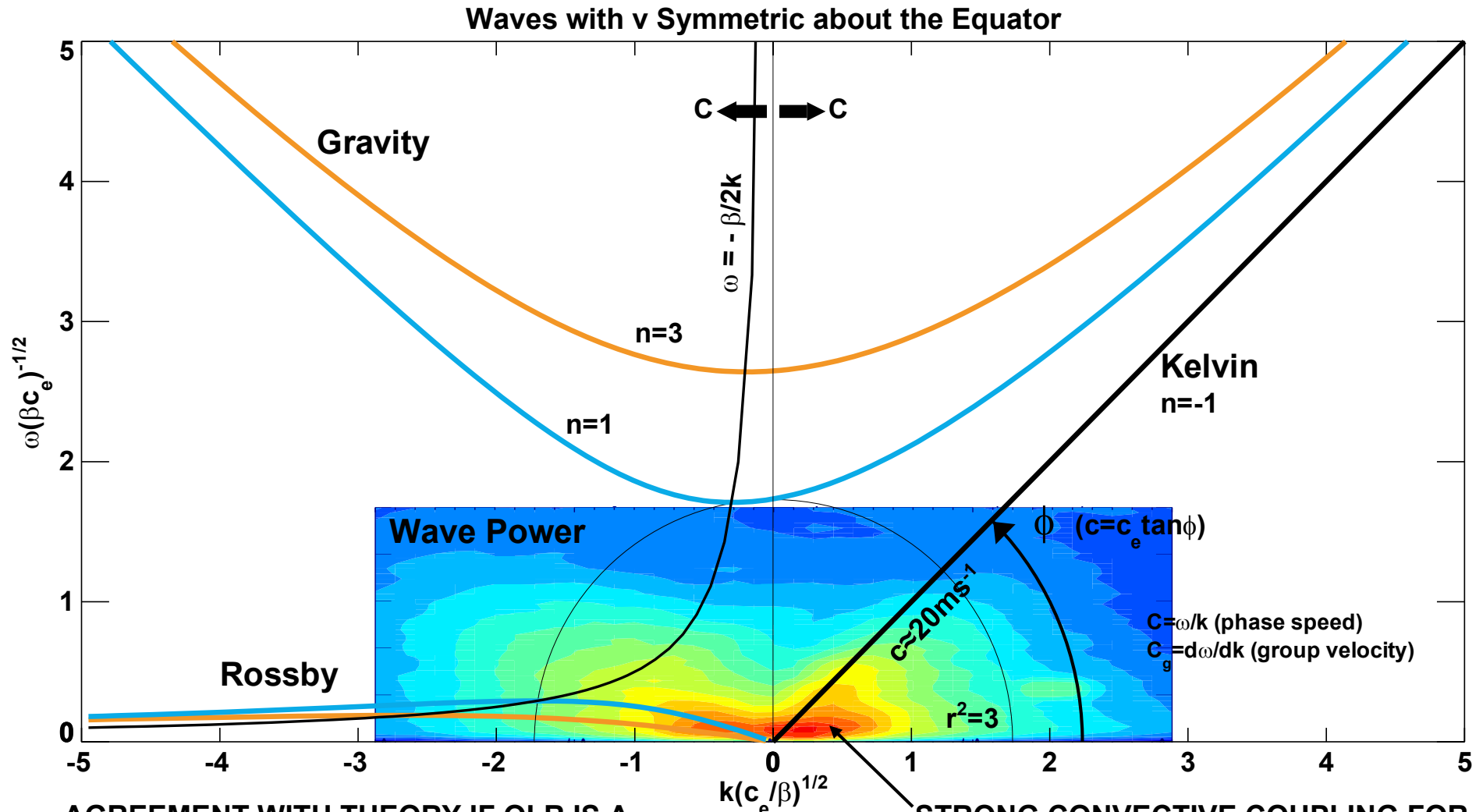


Colours show height perturbation (red positive, blue negative), arrows show lower-level winds

Interpretation of Free Equatorial Waves



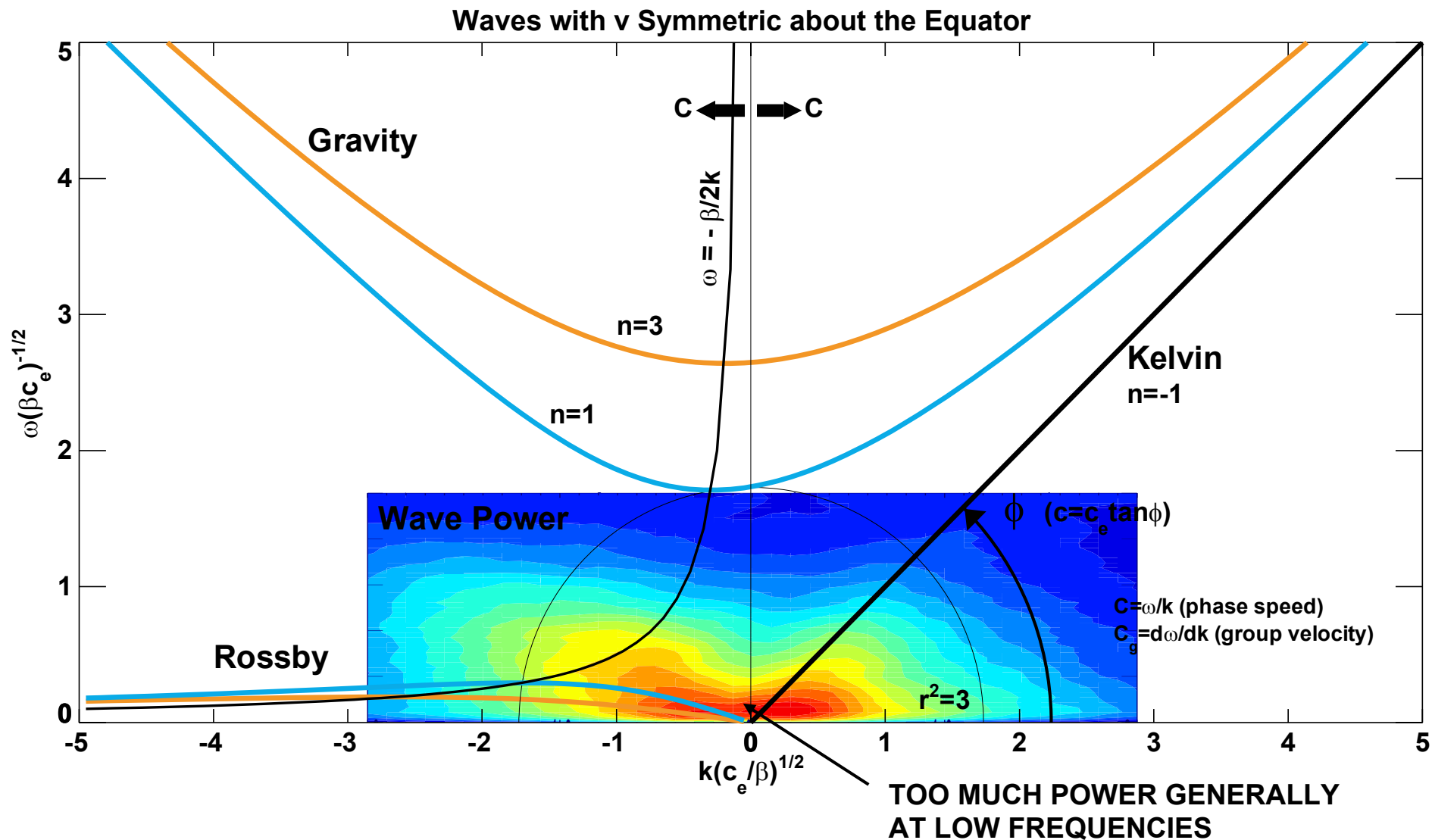
Symmetric waves. Observed OLR (NOAA)



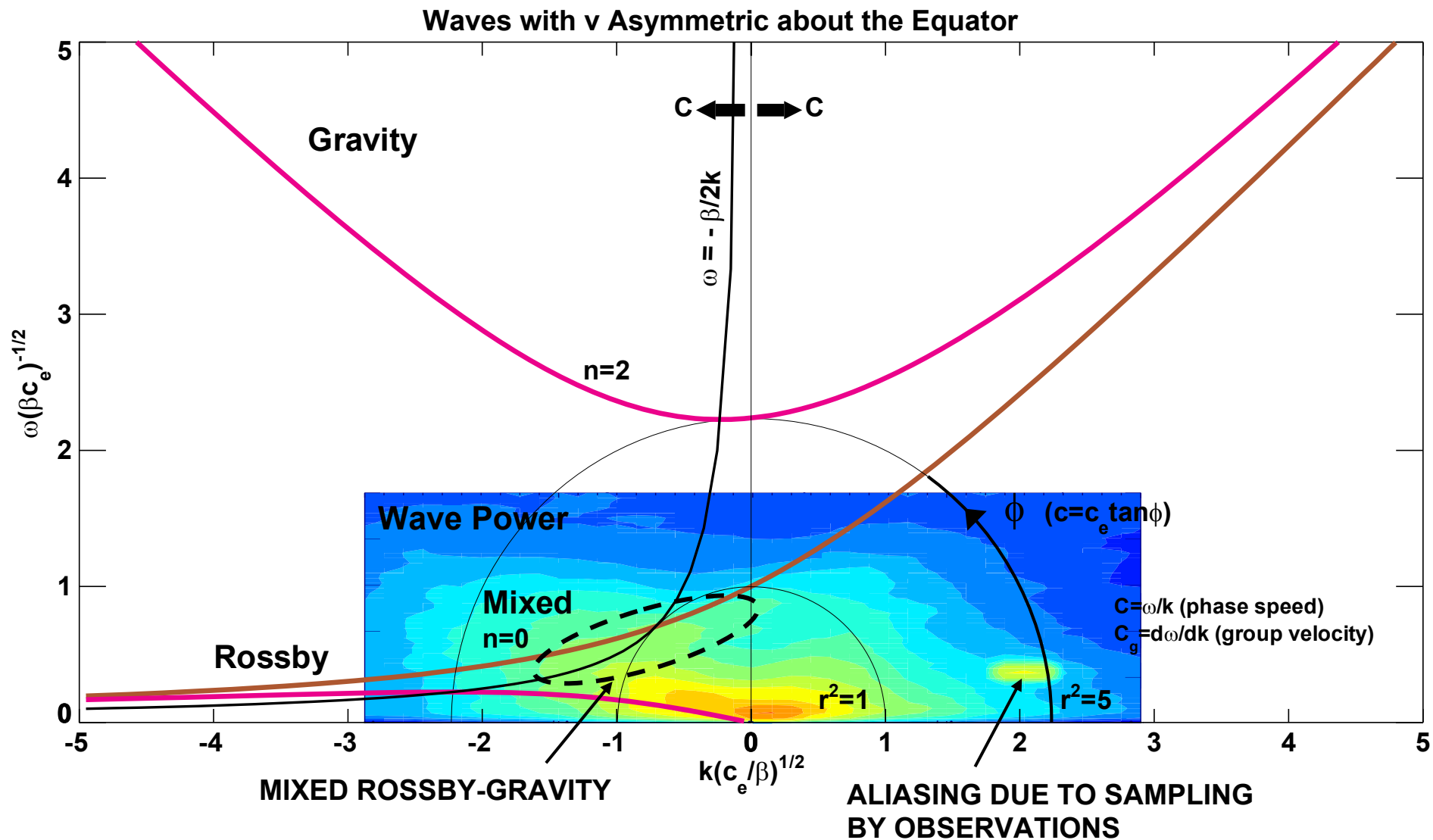
AGREEMENT WITH THEORY IF OLR IS A "SLAVE" TO THE FREE WAVES, LINEARITY ETC.

STRONG CONVECTIVE COUPLING FOR MJO AS IT DOESN'T LIE ON ANY LINE(?)

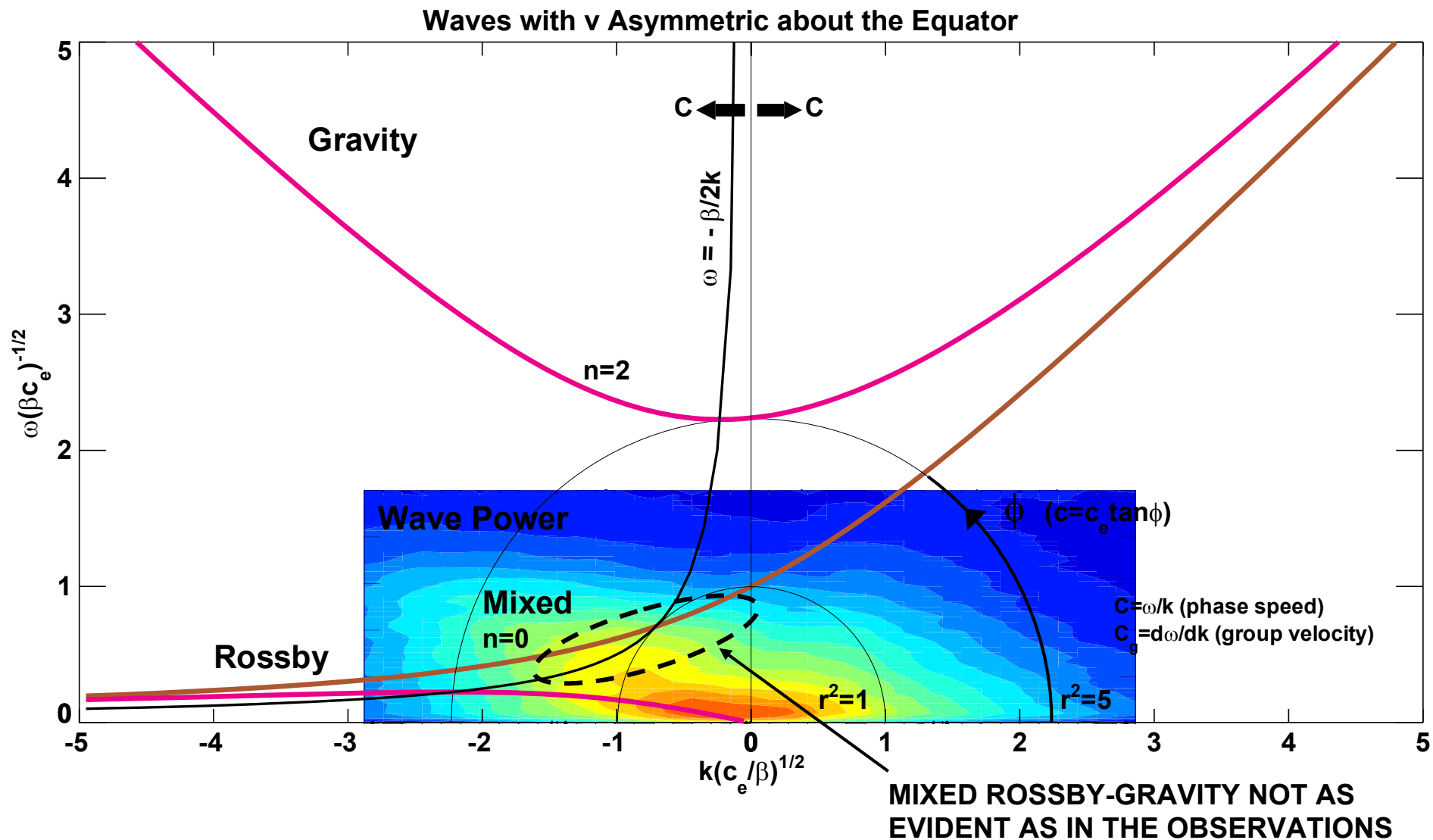
Symmetric waves. Simulated OLR (ECMWF)



Asymmetric waves. Observed OLR (NOAA)



Asymmetric waves. Simulated OLR (ECMWF)



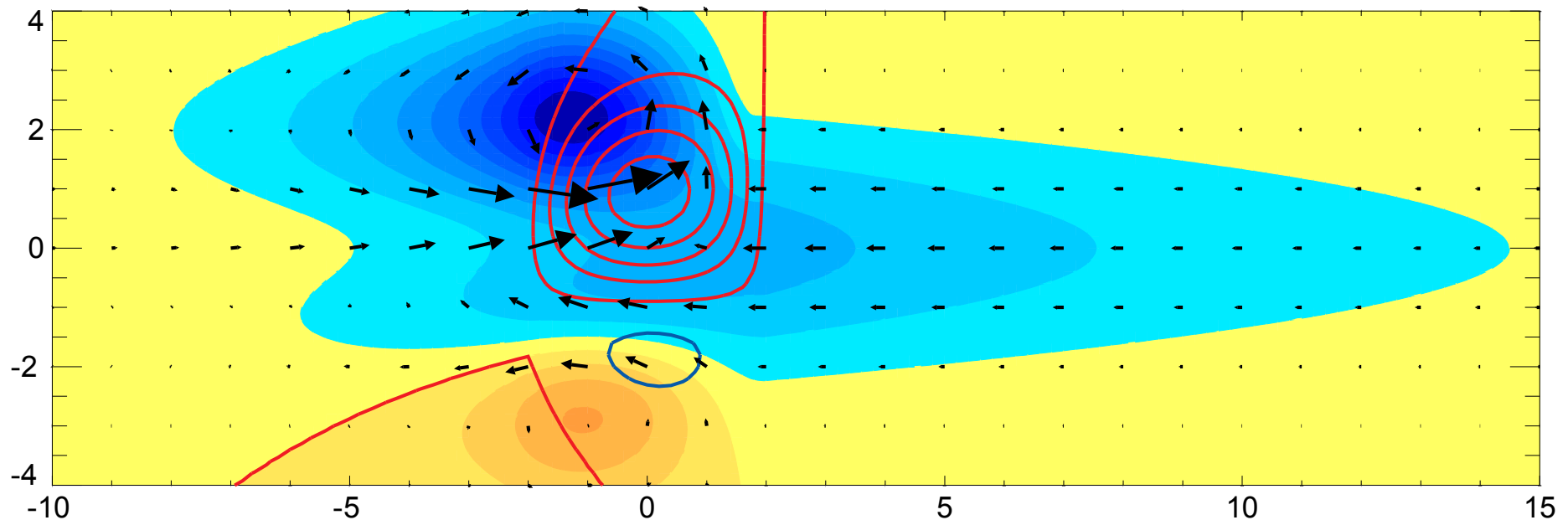
Gill's steady solution to monsoon heating

**DAMPING/HEATING TERMS TAKE THE PLACE OF
THE TIME DERIVATIVES**

EXPLICITLY SOLVE FOR THE X-DEPENDENCE

**GOOD AGREEMENT WITH THE AEROSOL
CHANGE RESULTS (OPPOSITE SIGN):**

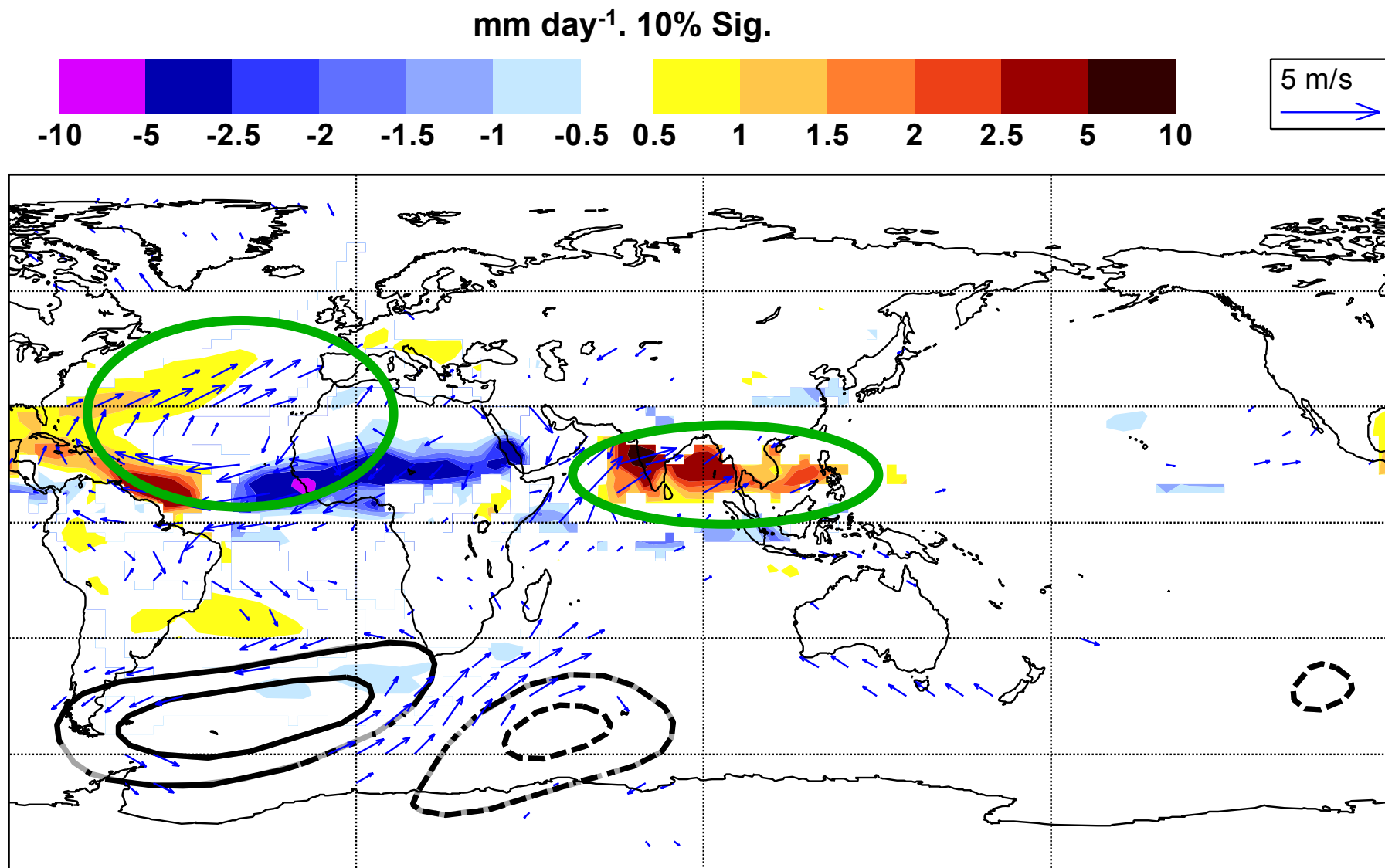
- **NORTH ATLANTIC SUBTROPICAL ANTICYCLONE**
- **CONVECTIVE COUPLING IN KELVIN WAVE REGIME**



Colours show perturbation pressure, vectors show velocity field for lower level, contours show vertical motion (blue = -0.1, red = 0.0, 0.3, 0.6, ...)

Following Gill (1980). See also Matsuno (1966)

JJA Precipitation, ν_{925} and Z500. New-Old





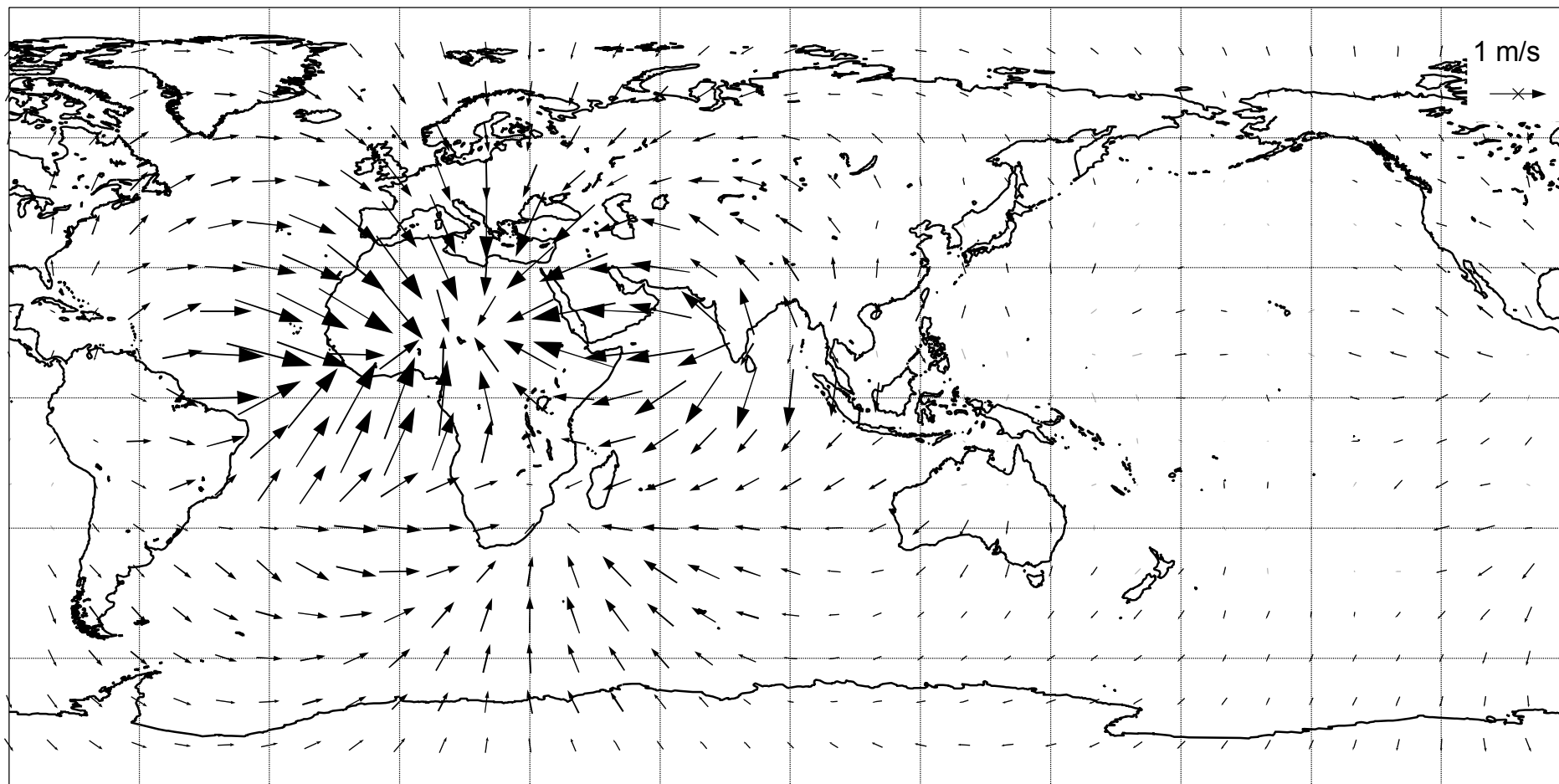
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Understanding the Extra-tropical Response



Diagnostics
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Upper Troposphere Divergent Wind Anomaly



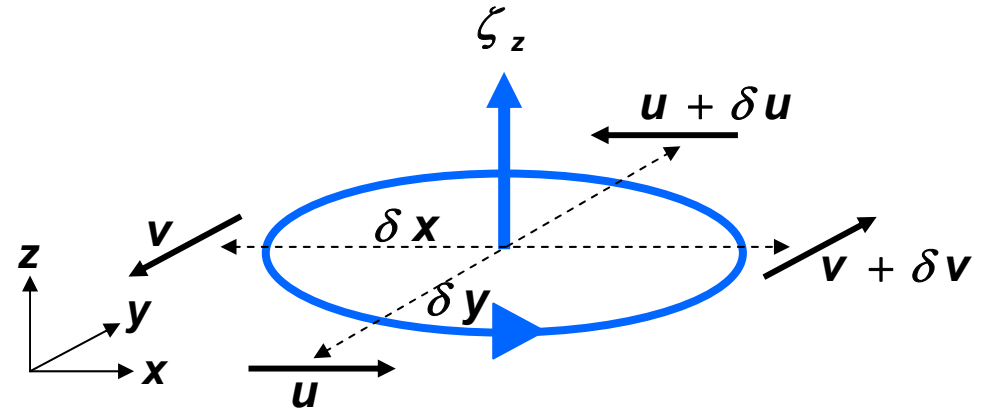
New minus Old aerosol. Anomaly is integrated between 100 and 300 hPa

The Vorticity Equation

Motivation (2D flow) :

$$\zeta_z = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \quad (\equiv \hat{\mathbf{k}} \cdot \nabla_z \times \mathbf{v})$$

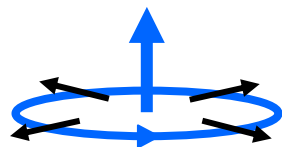
$\hat{\mathbf{k}}$ is the unit "vertical" vector and
 $\nabla_z \times$ is the horizontal curl operator



Curl of the 3D momentum equation in absolute frame of reference:

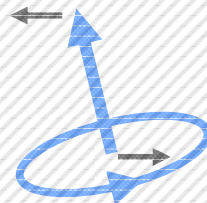
$$\frac{d \underline{\zeta}}{dt} = - \underline{\zeta} (\underline{\nabla} \cdot \underline{\mathbf{u}}) + (\underline{\zeta} \cdot \underline{\nabla}) \underline{\mathbf{u}} + \frac{1}{\rho^2} \underline{\nabla} \rho \times \underline{\nabla} p + \underline{\nabla} \times \underline{\mathbf{F}}_u$$

Lagrangian
tendency
in absolute
vorticity



Divergence

Tilting



Baroclinic



Friction



NEGLECT THESE TERMS

Barotropic Vorticity Equation

- Making the shallow atmosphere approximations and assuming barotropic, frictionless, horizontal flow

$$\begin{aligned} \frac{\partial \zeta}{\partial t} + \underline{\mathbf{v}}_{\psi} \cdot \nabla \zeta &= - \nabla \cdot (\underline{\mathbf{v}}_{\chi} \zeta) \\ &= - \zeta \nabla \cdot \underline{\mathbf{v}}_{\chi} - \underline{\mathbf{v}}_{\chi} \cdot \nabla \zeta \end{aligned}$$

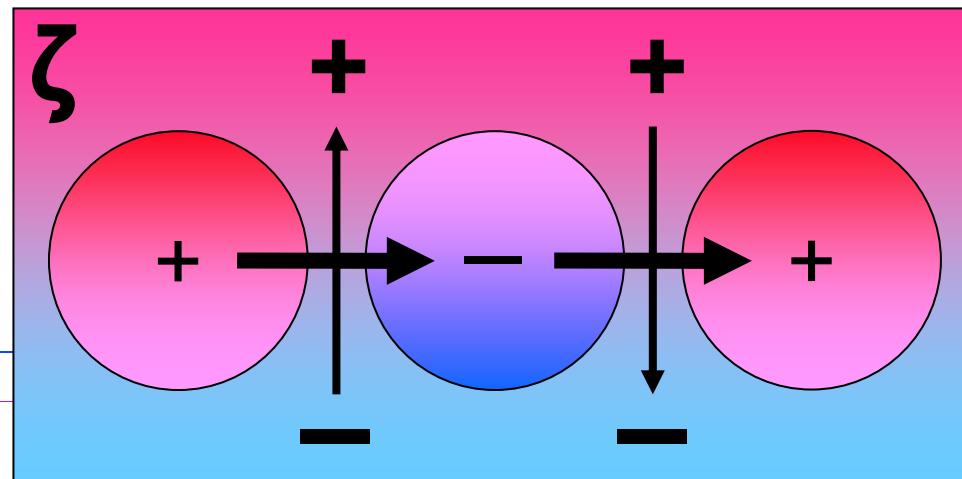
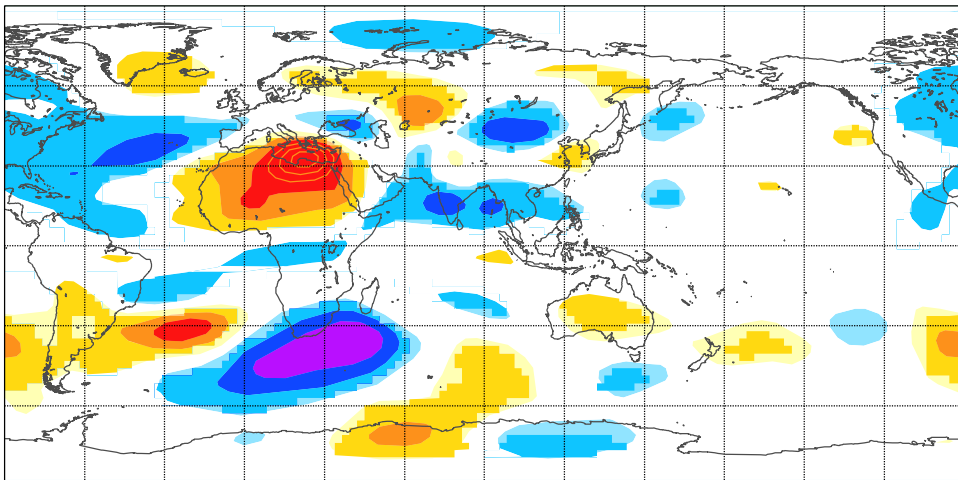
"Rossby Wave Source"

- Application to simple models: Sardeshmukh and Hoskins (1988).
- For use in complex GCMs, it is found here to be useful to vertically integrate this equation between 100 and 300 hPa.
- Is the extra-tropical mean response a linear stationary-wave solution?

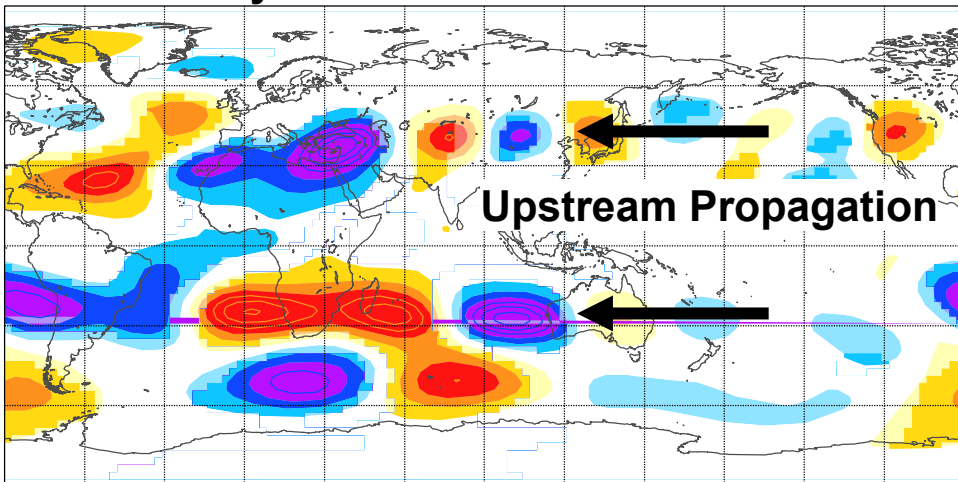
$$\underline{\mathbf{v}}'_{\psi} \cdot \nabla \bar{\zeta} + \bar{\underline{\mathbf{v}}}_{\psi} \cdot \nabla \zeta' \approx - \bar{\zeta} \nabla \cdot \underline{\mathbf{v}}'_{\chi} - \underline{\mathbf{v}}'_{\chi} \cdot \nabla \bar{\zeta} \quad (?)$$

JJA Balance in Vorticity Equation New-Old

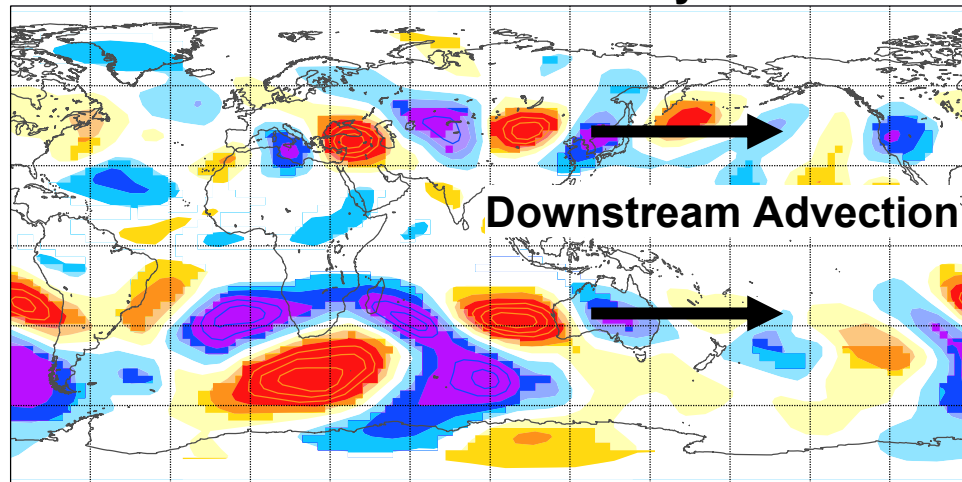
Rossby Wave Source



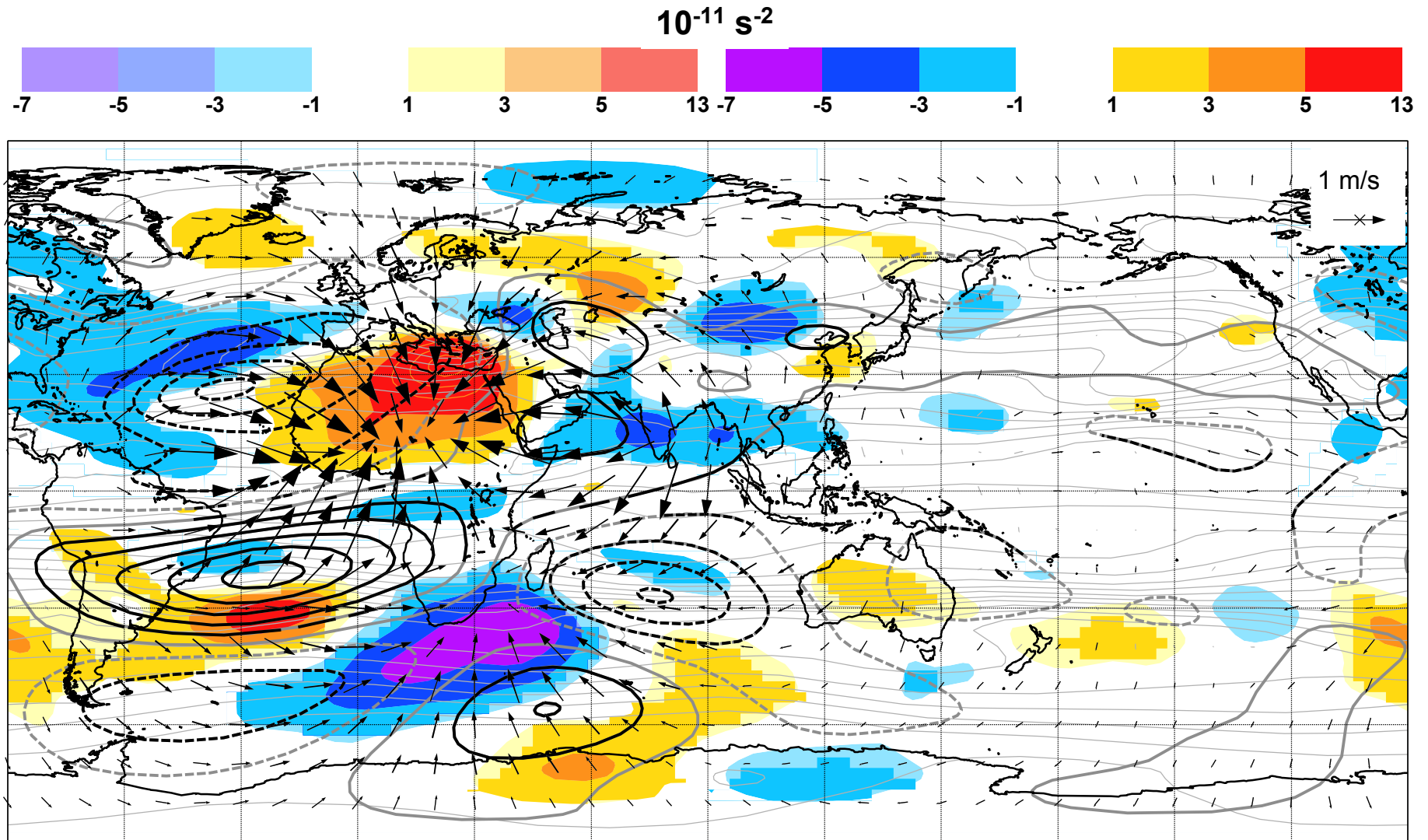
Advection by Anomalous Rotational Wind



Advection of Anomalous Vorticity

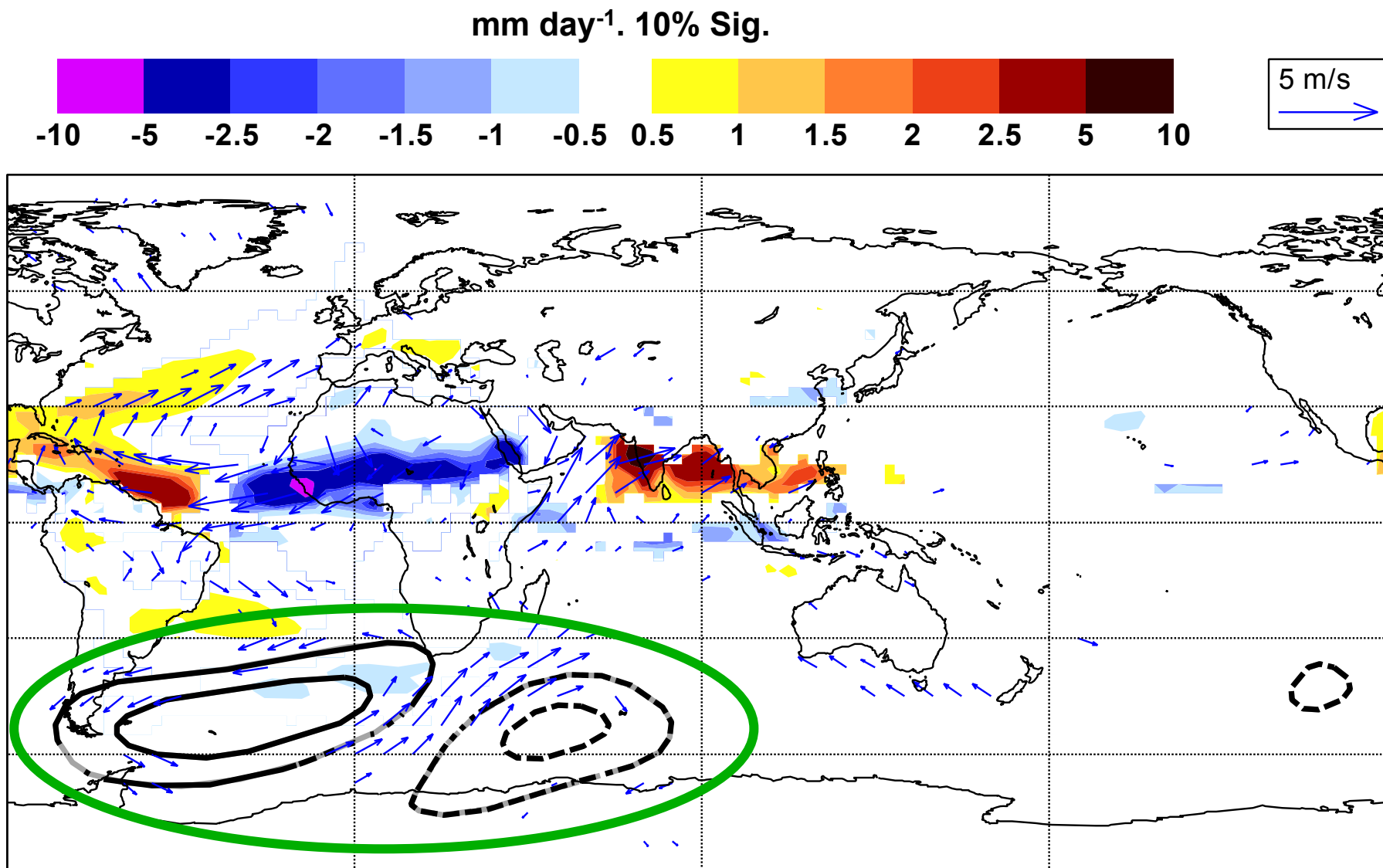


JJA New-Old RWS, \underline{v}_x , Ψ and mean ζ



Rossby wave paths agree beautifully with those predicted by Hoskins and Ambrizzi (1995)

JJA Precipitation, ν_{925} and Z500. New-Old

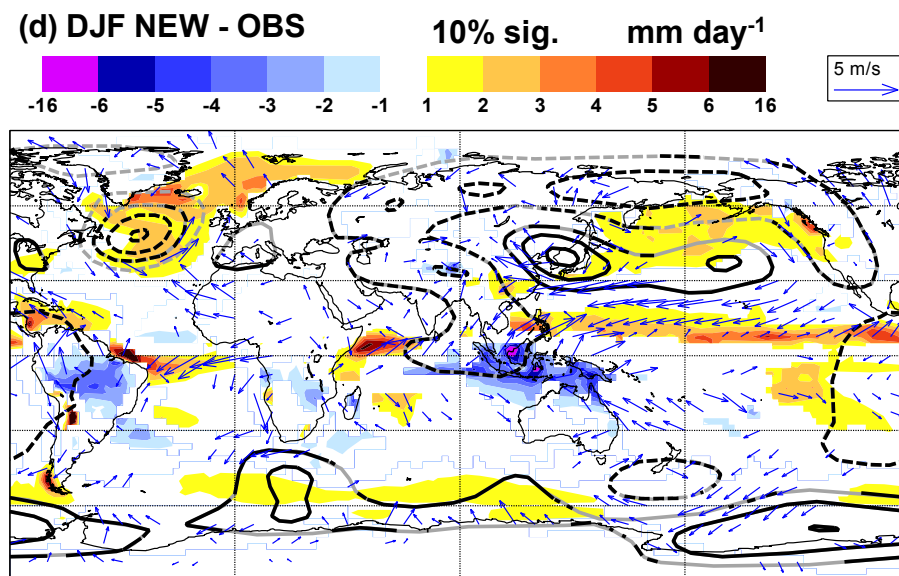
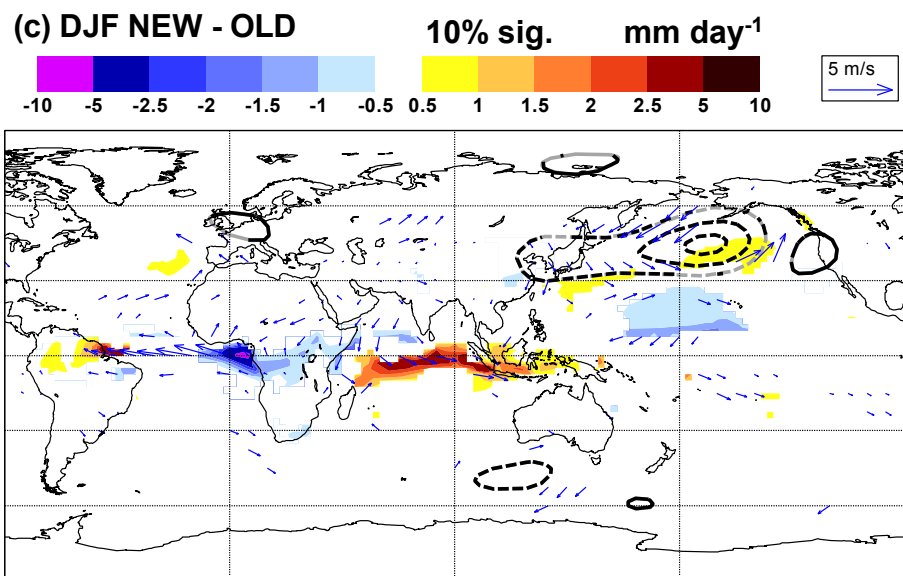
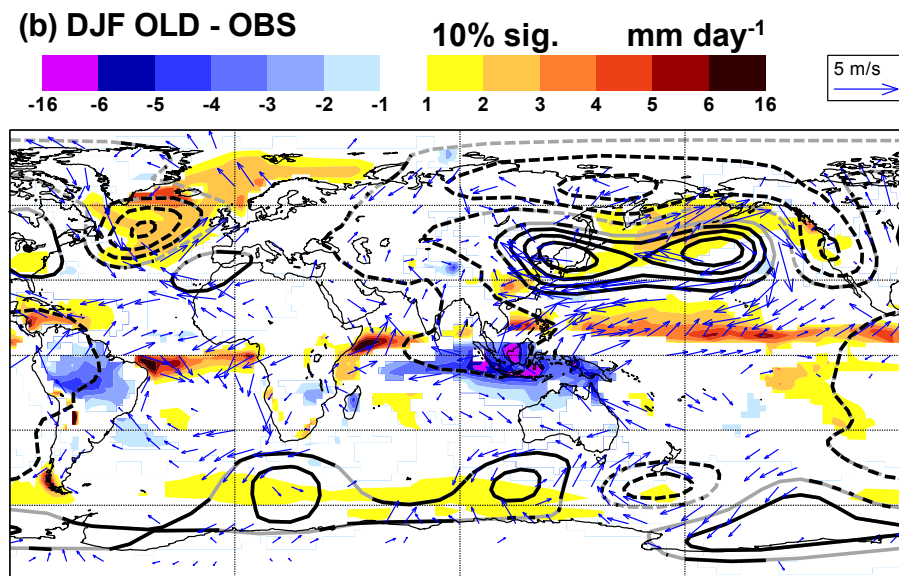
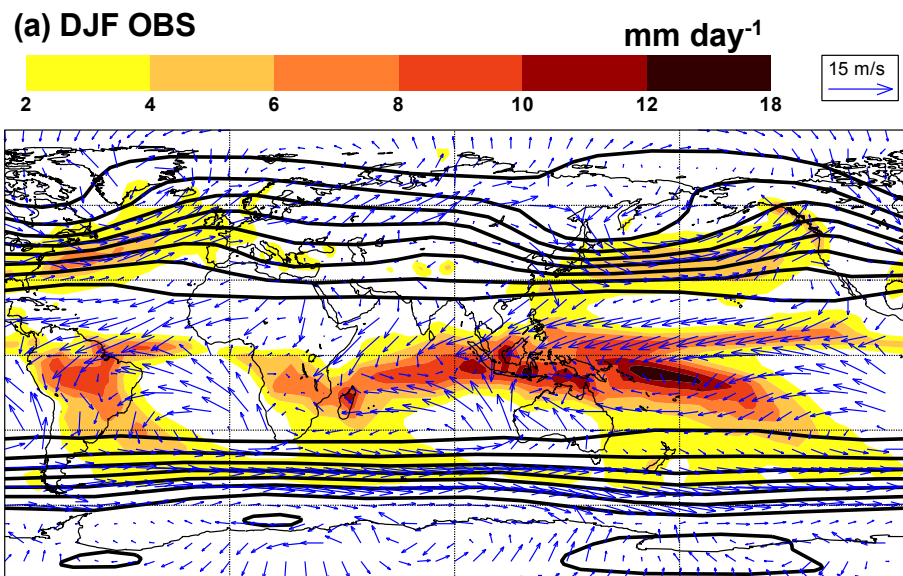




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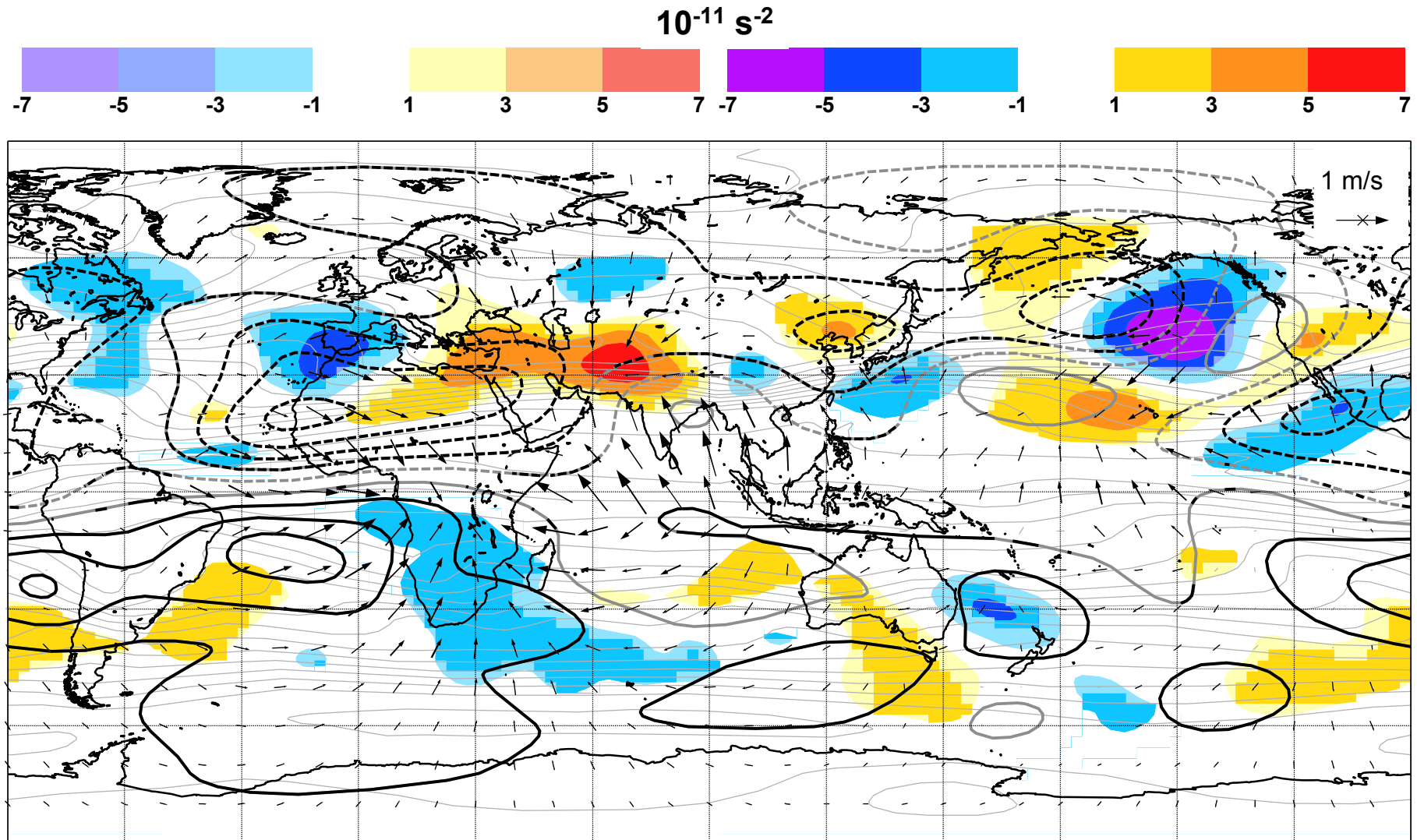
The December—February Season

DJF Precipitation, v_{925} and Z500



Precip: Xie-Arkin 1980–1999. v_{925} , Z500: ERA40 1962–01, (a) 10, (b)–(d) 2 dam. 26R3 seasonal data for the same period

DJF New-Old RWS, \underline{v}_x , Ψ and mean ζ



Precipitation / RWS agreement suggests possibility for interaction with extra-tropical physics
Rossby wave path agrees with that predicted by Hoskins and Ambrizzi (1993)

Summary

- **Physics changes have global implications!**
 - Statistical tests can reveal **which** aspects are attributable to a change
 - To understand **why**, a set of diagnostic tools is needed
- **Analysis Increments and Initial Tendencies**
 - Useful to help understand local physics changes (and subsequent interactions)
 - Different from climate simulations and single column experiments
- **Equatorial waves**
 - Help explain the mean tropic-wide response
 - Linear waves can 'set the scene'
 - Coupling with convection enhances the response
- **Extra-tropical Rossby waves**
 - Help explain the mean extra-tropical response
 - Understanding is aided by linearity
 - Extra-tropical interaction with physics could be studied with PV approach

