

# Joint Probabilities of Storm Surges Waves and River Discharges

*Thomas I. Petroligkis (JRC)*  
*Evangelos Voukouvalas (JRC)*  
*Juliana Disperati (JRC)*  
*Jean Bidlot (ECMWF)*

*Paul Dando & Carsten Maass (Support)*

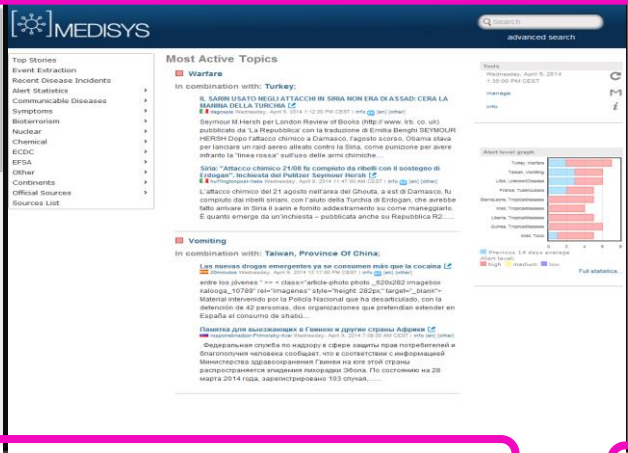
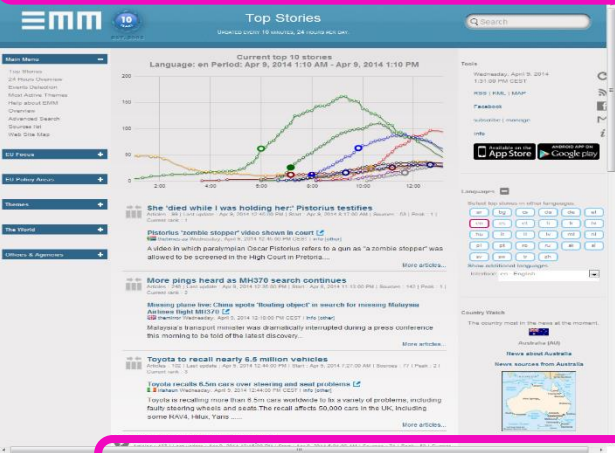
*Utilising statistical dependence methodologies & techniques*

**Going After High-Impact Compound Events**

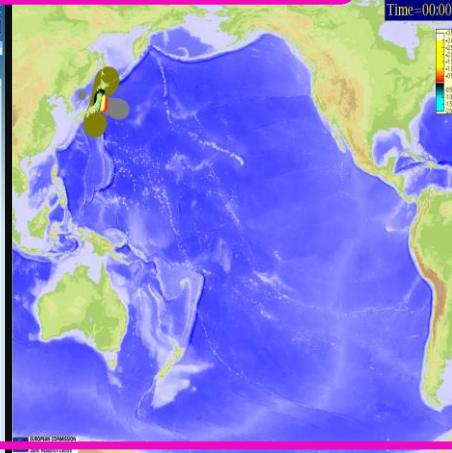
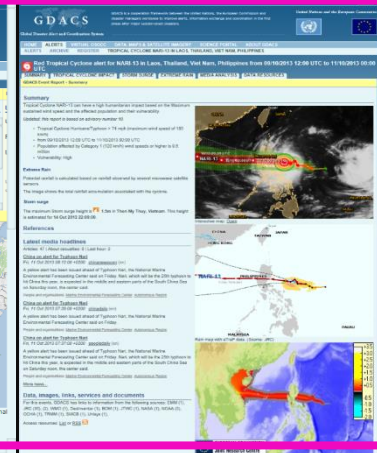
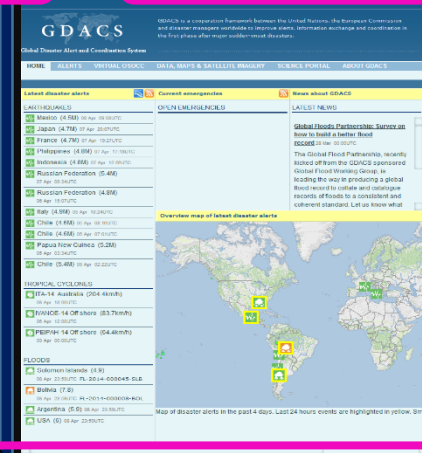
Joint Research Center

# Global Security & Crisis Management Unit Institute for Protection & Security of Citizen (Joint Research Center)

## Open Source Monitoring for Media Analysis and Security

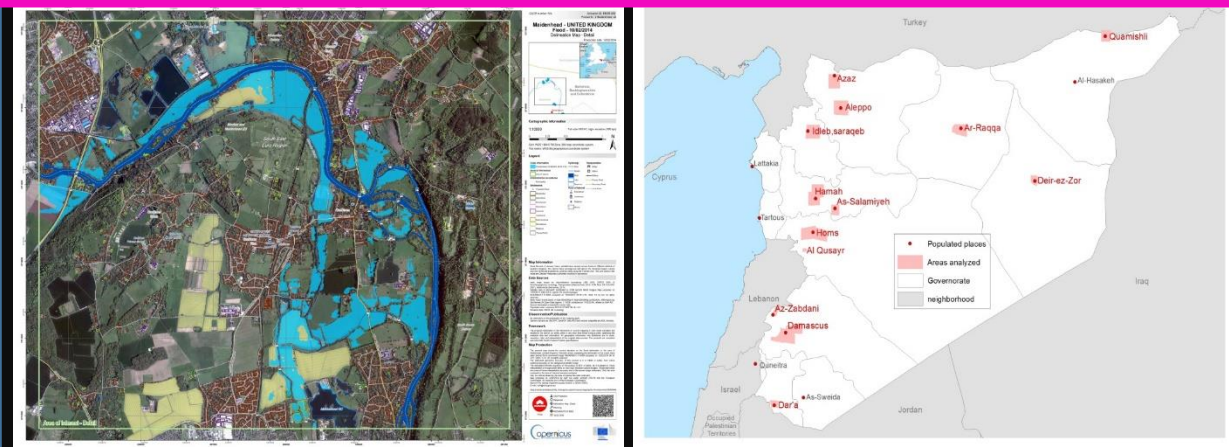
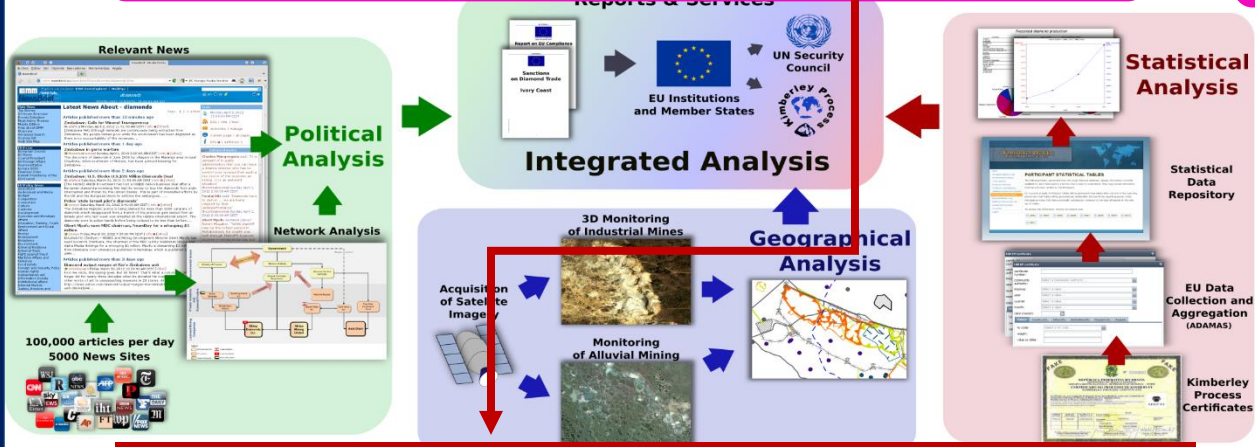


## Natural Disasters Monitoring and Analysis



## Conflict Prevention through the Kimberly Process

## European Emergency Mapping & International Reconstruction

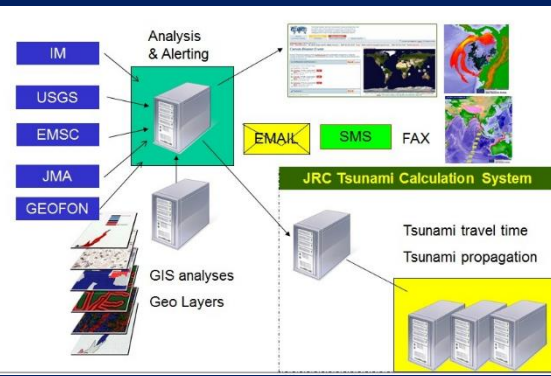


*Going After Blood (War-Torn Areas) Diamonds...*

# Natural Disasters Monitoring and Analysis Global Disaster Alert & Coordination System

[www.gdacs.org](http://www.gdacs.org) JRC – UN – OCHA – UNOSAT

Tsunami Analysis Tool (TAT)



**GDACS**  
Global Disaster Alert and Coordination System

HOME ALERTS VITAL INFO DATA, MAPS & SATELLITE IMAGES SERVICES PORTAL ABOUT GDACS

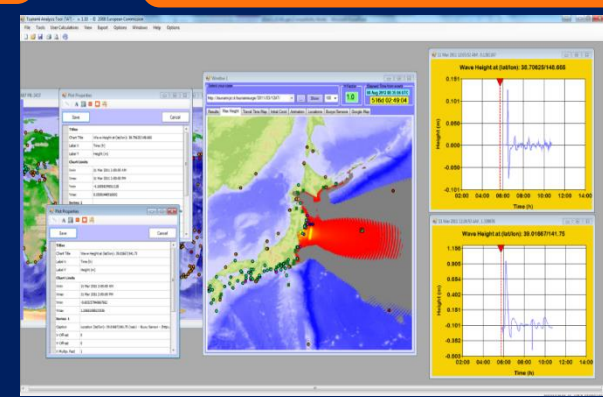
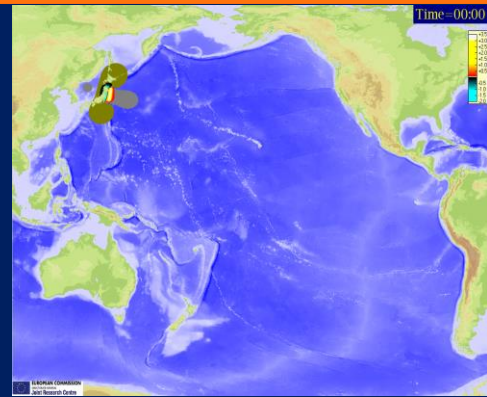
**RECENT EARTHQUAKES**

Mexico (4.5M)	01 Apr 08:00:00
Japan (4.7M)	01 Apr 08:00:00
France (4.7M)	01 Apr 08:00:00
Philippines (4.8M)	01 Apr 08:00:00
Indonesia (4.8M)	01 Apr 08:00:00
Russian Federation (5.4M)	01 Apr 08:00:00
Russian Federation (4.8M)	01 Apr 08:00:00
Italy (4.8M)	01 Apr 08:00:00
China (4.8M)	01 Apr 08:00:00
Chile (4.9M)	01 Apr 08:00:00
Principes New Guinea (4.7M)	01 Apr 08:00:00
Chile (4.9M)	01 Apr 08:00:00

**OPEN EMPLOYERS**

**LATEST NEWS**

**Map of disaster alerts in the past 4 days. Last 24 hours events are highlighted in yellow.**



- Population density model connected with vulnerability and magnitude of the disaster
- The objective is to distinguish between large earthquake in unpopulated regions and smaller earthquake in higher populated areas.

**Green Earthquake Alert Bolivia M 6.7**

**Red Earthquake Alert Pakistan M 6.0**

## Tropical Cyclone Impacts

## Storm Surge Monitoring & Daily Bulleting

**GDACS**  
Global Disaster Alert and Coordination System

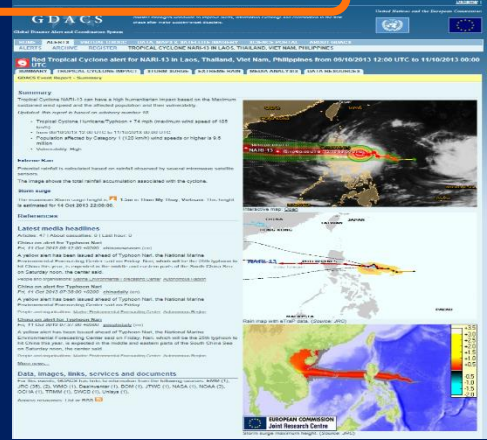
**Tropical Cyclone Alert for NAMI-13 in Laos, Thailand, Viet Nam, Philippines from 00:10:00 UTC to 01:00:00 UTC on 11/02/2013**

**Summary**

The JRC has developed a global tsunami wave height calculation model which is used for each earthquake based on seismological methods around the world. This report is for earthquake update 194706 of event 194706 issued at 11/02/2013 00:40 (GDACS Event ID: 194706, Latest update ID: 194706).

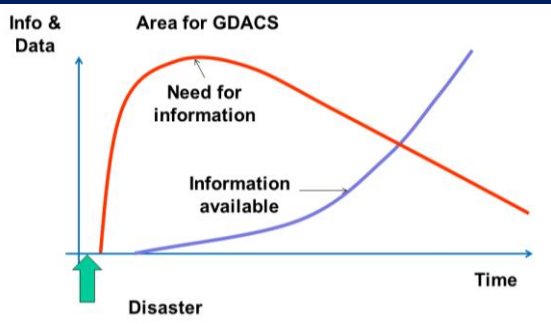
**Affected locations**

Date	Name	Country	Population	Population density
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120
11/02/2013 00:32 GMT	Phnom Penh	Cameroon	1,200,000	120



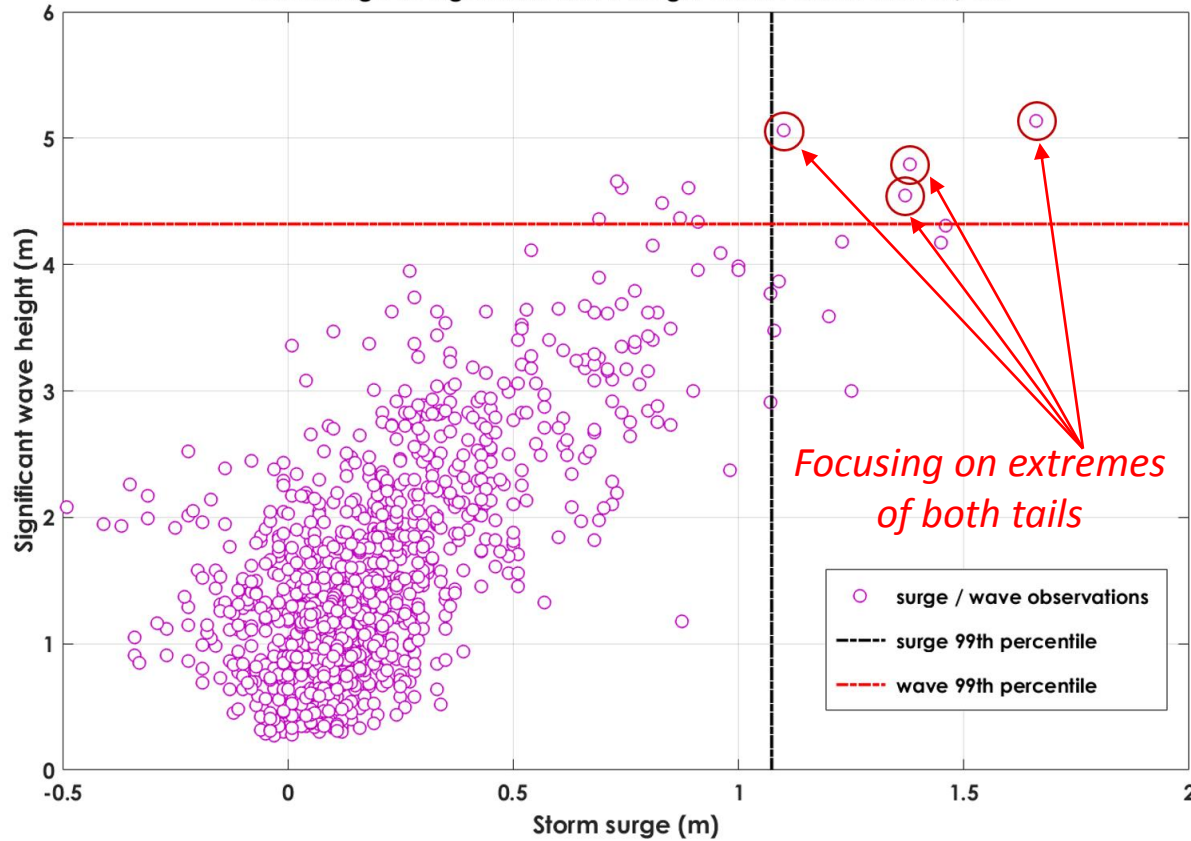
**Storm Surge Bulletin**

**13 February 2014: UK, Ireland - Severe Weather**



## Focusing on Wind – Precipitation & Storm Surge Impact(s)

Storm surge Vs significant wave height observations at HVH / LIC



## IPCC, 2012: Compound Events

special category of weather / climate extremes, resulting from the combination of two or more events, i.e. extremes either from a statistical perspective (tails of distribution) or associated with a specific (critical) threshold(s) ...

# CoastALRisk

Prototype of a first Global Integrated Coastal Impact-based of Flood **Alert** and **Risk** Assessment Tool

The Exploratory Research Project Coastal-Alert-Risk

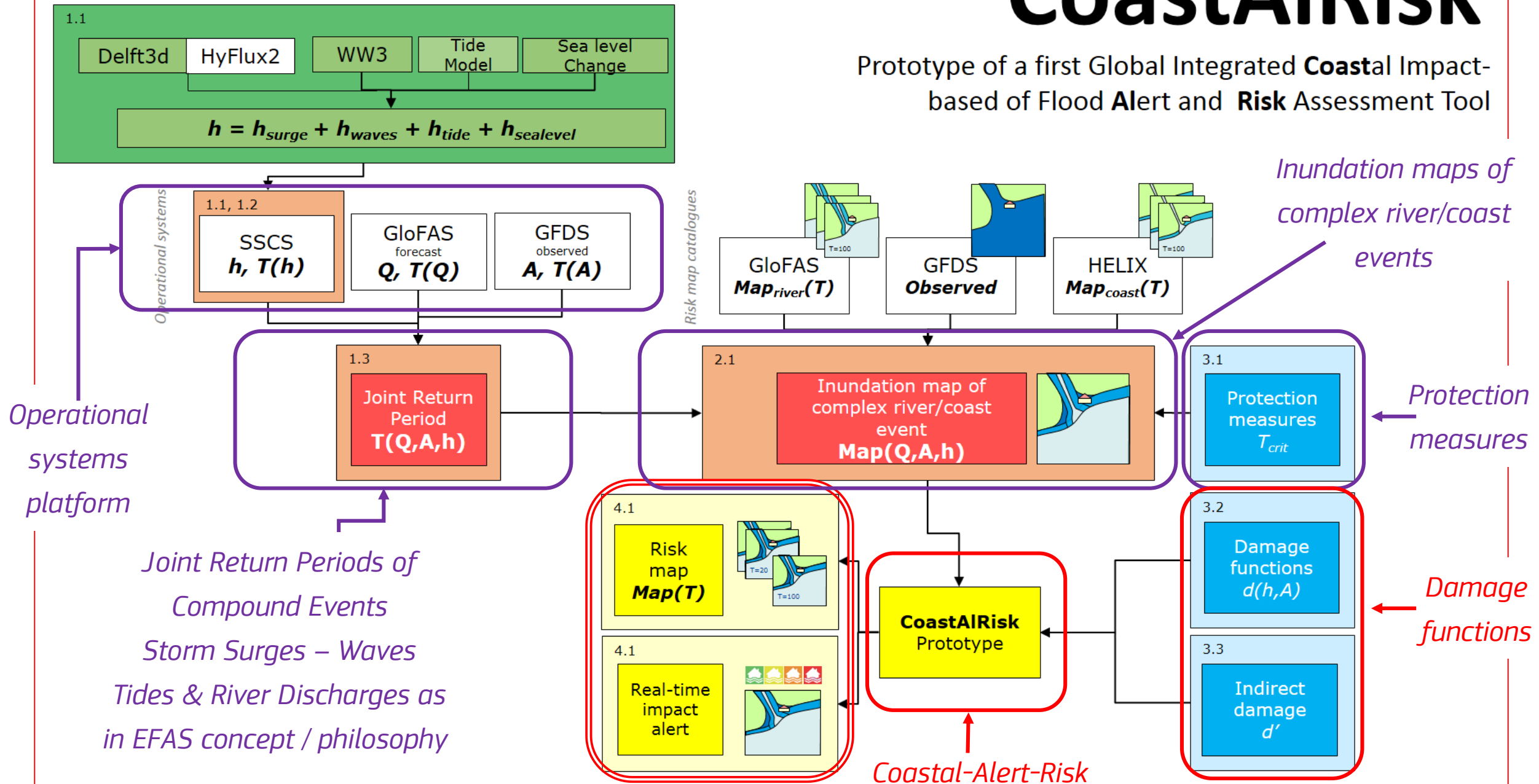
of the Joint Research Center has been an initial effort of developing the first global integrated coastal flood risk management system with emphasis

on such compound events, by linking satellite monitoring, coupled wave, tide and surge forecasting, inundation modelling and impact analysis

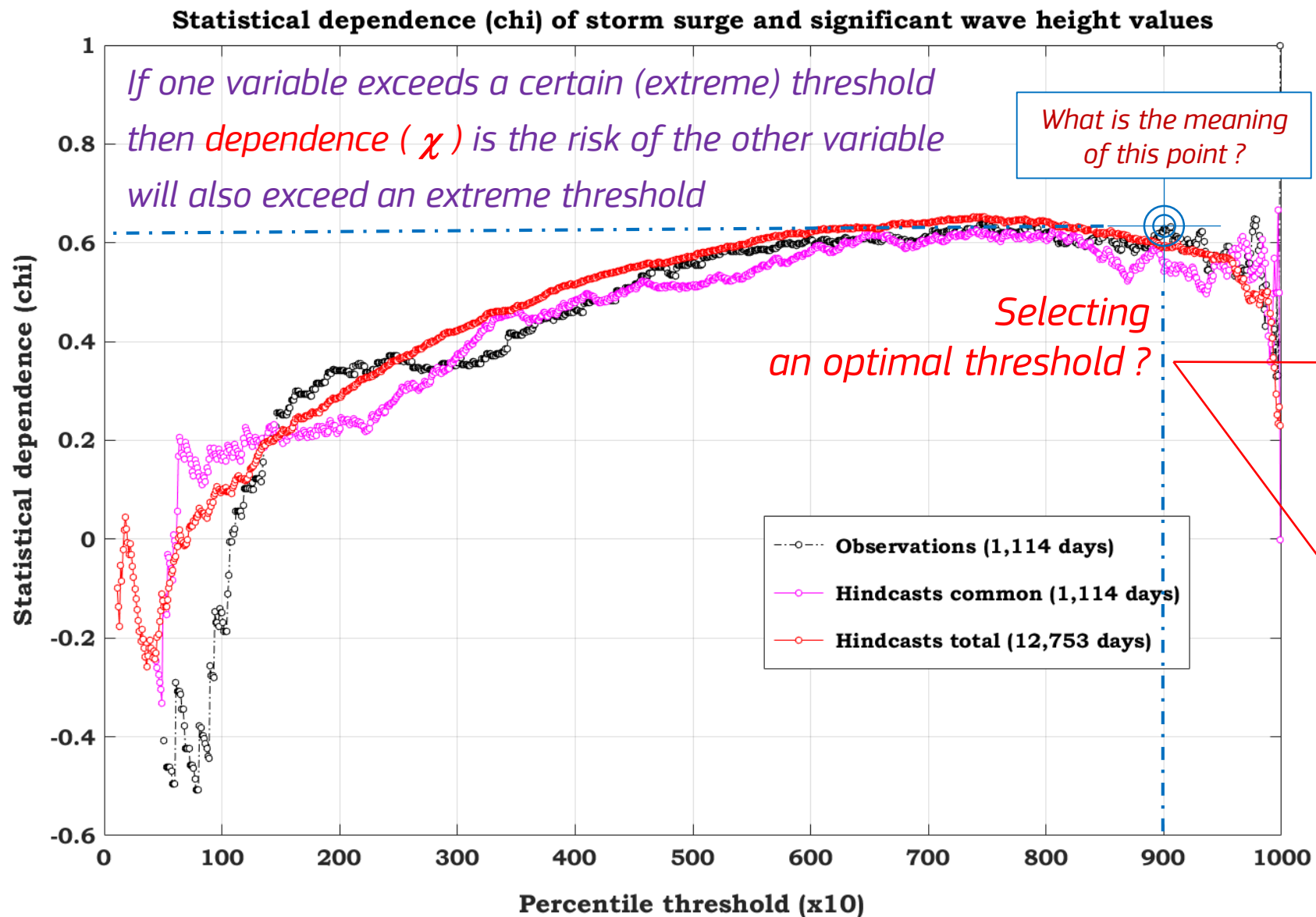


# CoastAIRisk

Prototype of a first Global Integrated **Coastal** Impact-based of Flood **Alert** and **Risk** Assessment Tool



# Estimating joint probabilities by utilising statistical dependencies of component events



**WHY ?**

**Dependence can modulate  
Joint Return Period ...**

Firstly  
to have enough data points  
above the threshold  
to be able  
to determine dependence

and secondly  
the threshold  
to be high enough  
to regard the values as extreme  
(Svensson and Jones 2003)

**Example of how statistical dependence (chi) modulates joint return period**

$$T_{X,Y} = \sqrt{\frac{T_x \cdot T_y}{\chi^2}}$$

$T_{X,Y}$  = Joint Return Period

$T_x$  = Return Period (surge)

$T_y$  = Return Period (wave)

Utilizing matlab routines to fit GEV (General Extreme Value) Distributions to surge & wave values both 100-year return period values of total hindcast datasets for HVH (storm surge) / LIC (significant wave) were estimated ...

	Surge / 100 RP	Wave / 100 RP	chi	JRP
Hind total	1.78	6.05	0.5730	174.53

**Probability** of the combined event in total hindcasts mode

surge = 1.78 & wave height = 6.05 meters

**to be exceeded in a year**

if considered independent events is given by

$1/100 \times 1/100 = 1 / 10,000 = 0.0001\%$

However, in case of  $\chi = 0.57$

JRP = 174.95 years

**Then probability of exceeding**

$= 1 / \text{Joint Return Period} = 1/174.95 = 0.0057$

(~57 times higher)

Considering **U** and **V** with distributions [ 0, 1 ]  
and a critical threshold (**u**)

$$P(V > u | U > u) = \frac{P(U > u, V > u)}{P(U > u)}$$

$$\chi(u) = 2 - \frac{\ln P(U \leq u, V \leq u)}{\ln P(U \leq u)} \text{ for } 0 \leq u \leq 1$$

$$P(U \leq u, V \leq u) = \frac{\text{Number of } (X, Y) \text{ such that } X \leq x^* \text{ and } Y \leq y^*}{\text{Total number of } (X, Y)}$$

$$\ln P(U \leq u) = \frac{1}{2} \ln \left[ \frac{\text{Number of } X \leq x}{\text{Total number of } X} \cdot \frac{\text{Number of } Y \leq y^*}{\text{Total number of } Y} \right]$$

*since we are after the  
Joint Return Period ...  $T_{xy}$   
so, we need the value  
of dependence*



$$T_{X,Y} = \sqrt{\frac{T_x \cdot T_y}{\chi^2}}$$

*The theoretical return period  
is the inverse of the probability  
that a certain event will be  
exceeded in any one year ...*

*To define the number of extremes  
two (2) methodologies exist  
- Annual (Block) Maxima &  
- Peaks-Over-Threshold (POT)*



From Svensson & Jones (2003)

If  $\alpha$  is the annual maximum non-exceedance probability

$$\alpha = \text{Prob}(\text{Annual maximum} \leq x)$$

then Return Period:  $T\alpha = 1 / (1-\alpha)$

For Peaks-Over-Threshold (POT)

Not referring to an annual maximum with  $p$  as non-exceedance probability of POT series

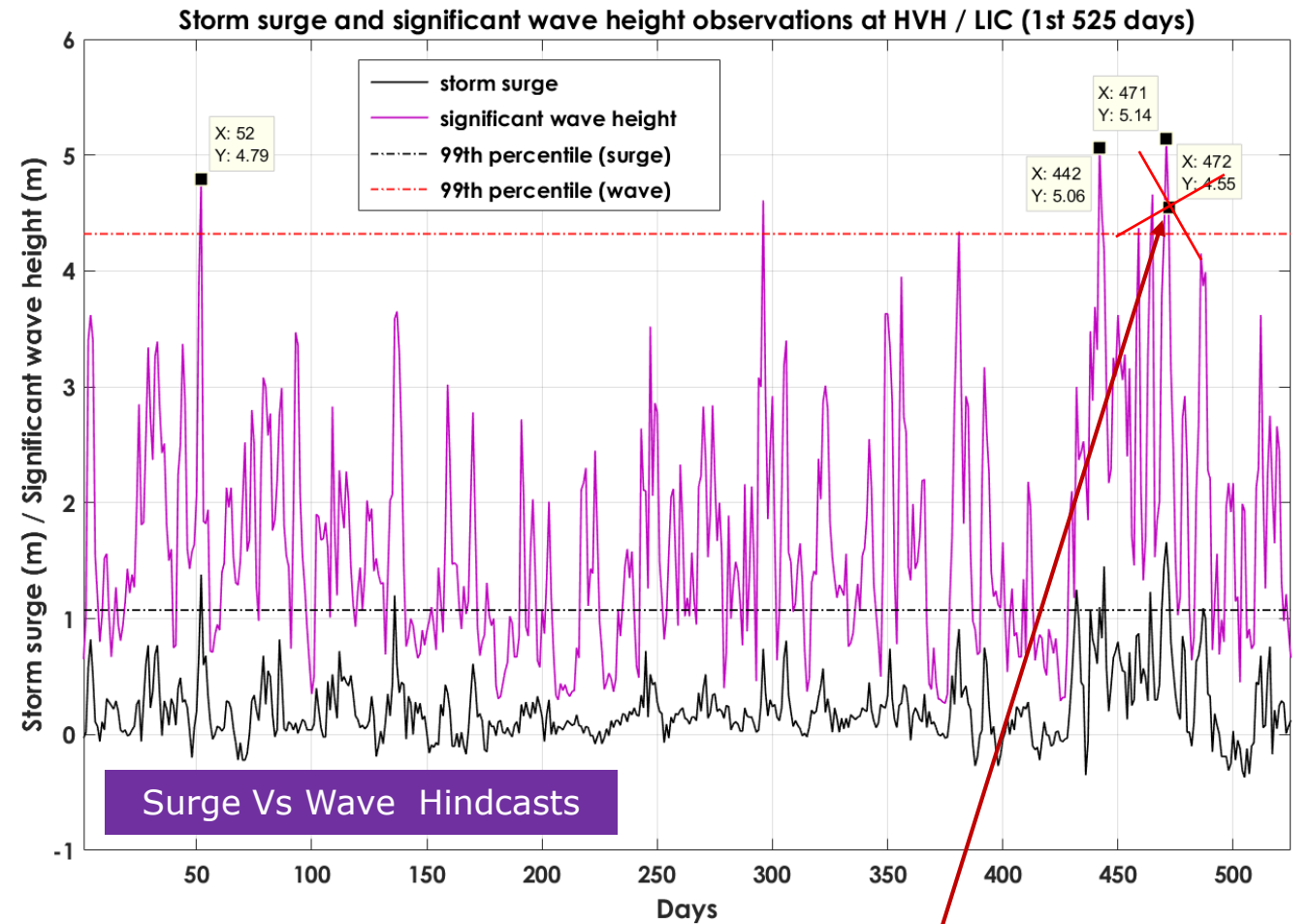
and the rate of  $\lambda$  events per year

$\alpha = \exp(-\lambda(1-p))$  ... For our estimations we adapt

**~2.3 events / yearly** to exceed that  $\rightarrow \alpha = 0.1$  ...

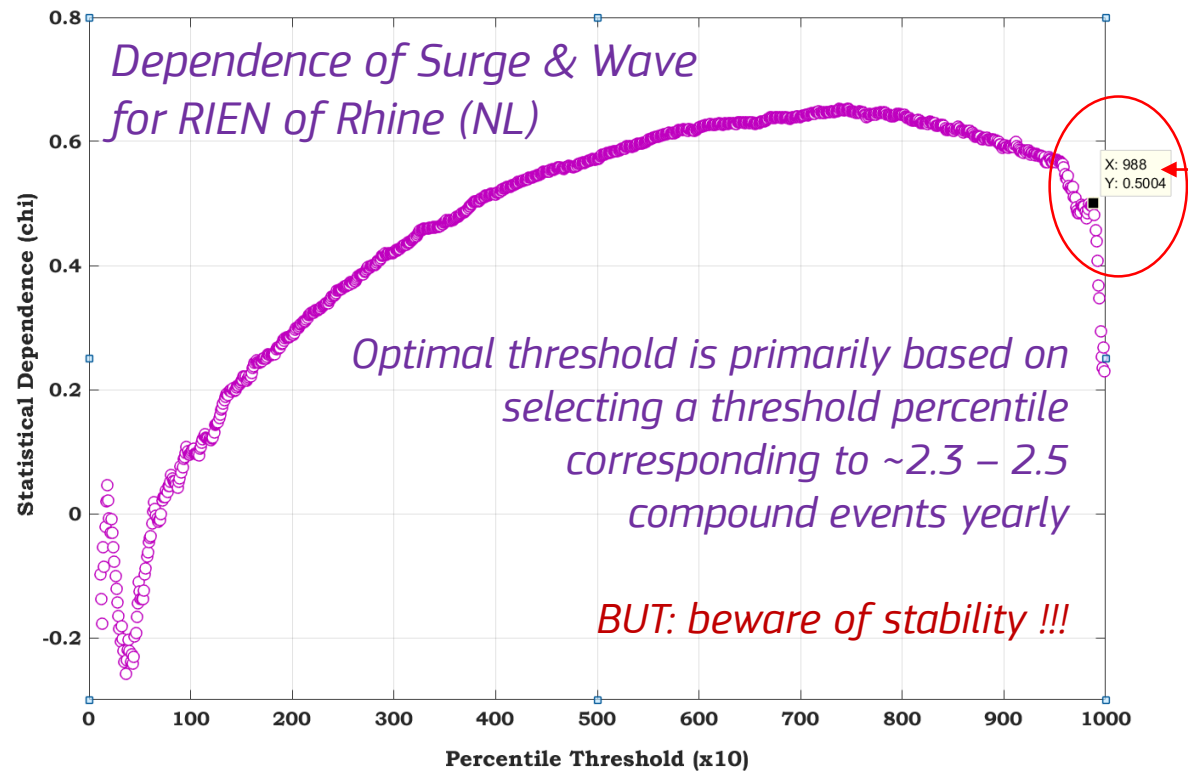
based on the number of the events being allowed to exceed yearly **~2.3 (max ~2.5)**

we have the ability to define an **appropriate percentile threshold**

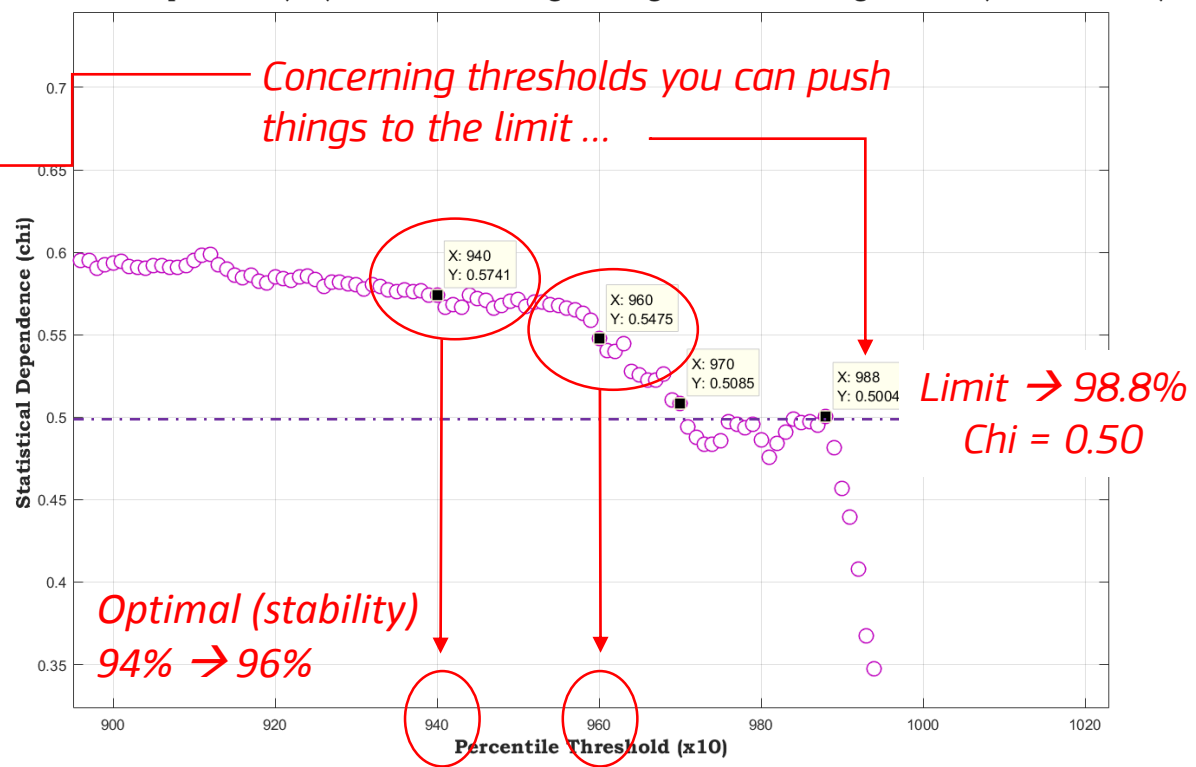


*POT example of skipping consecutive events falling inside 3-day block ...*

Statistical dependence (chi) between storm surge and significant wave height max24 (total hindcasts)



Statistical dependence (chi) between storm surge and significant wave height max24 (total hindcasts)



RIEN	River	CHI	Max	Type	Per	CHI (R)	Max (R)	Type (R)
17	Rhine (NL)	0.5475	*	super	0.0	0.5739	*	super

Selecting optimal threshold besides stability has to be in harmony with ~2.3 - 2.5 events per year if NOT then: selection of another threshold to meet imposed criteria most of the times (but not all) a higher value percentile leading to lower values of dependence } for this case selected threshold 95%

*Study over 32 RIEN  
(River Ending) Points*

*Irish Sea*

*Bristol Channel*

*English Channel*

*Norwegian Sea*

*North Sea*

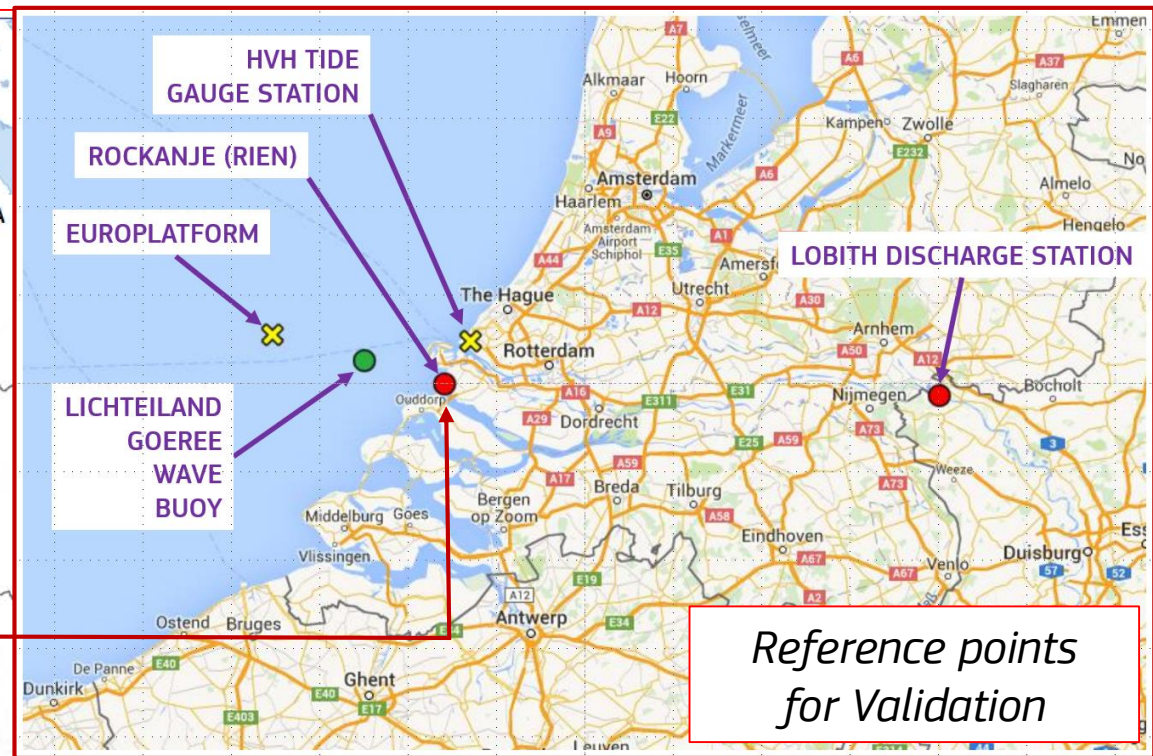
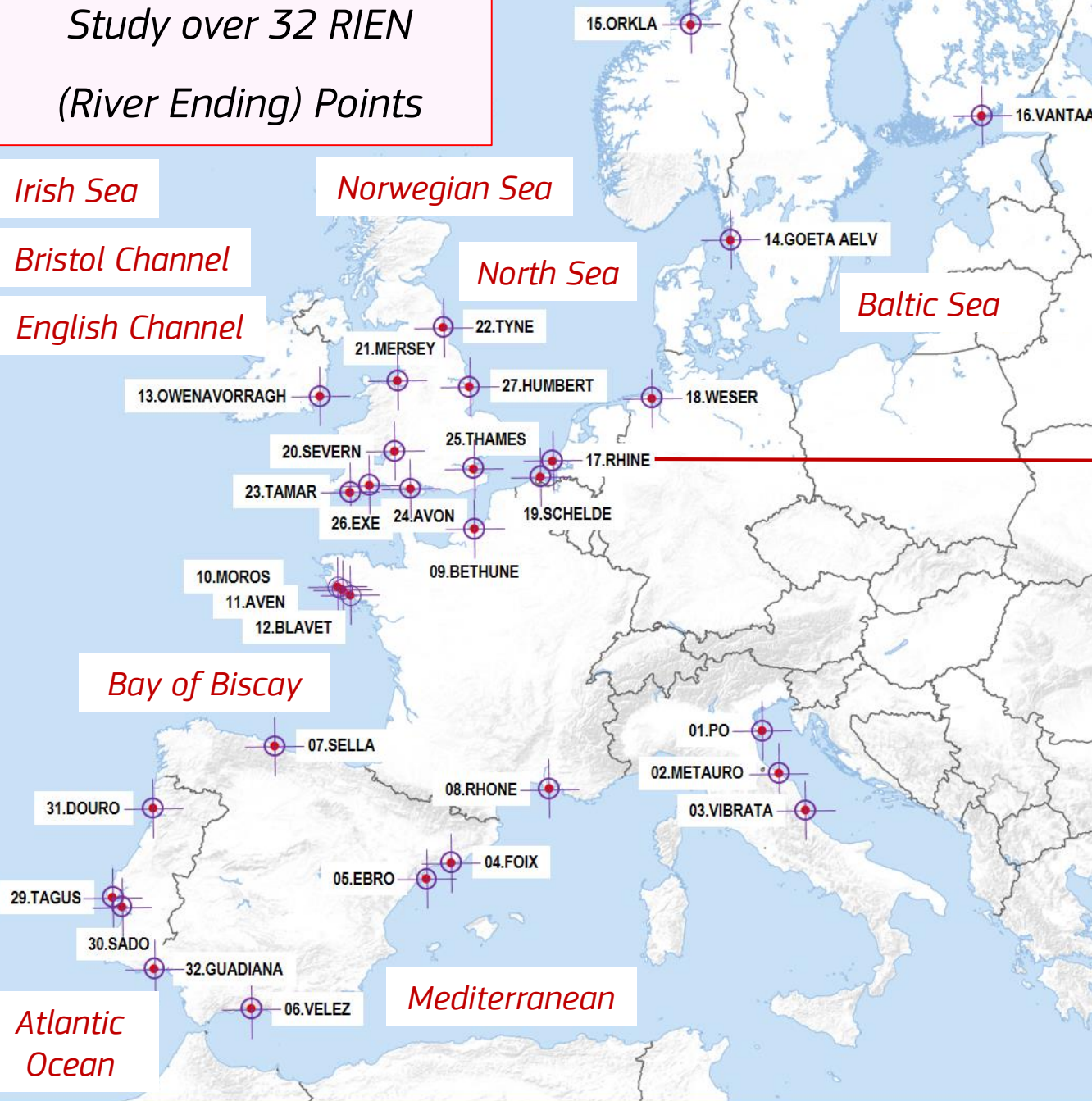
*Baltic Sea*

*Black Sea*

*Bay of Biscay*

*Mediterranean*

*Atlantic Ocean*

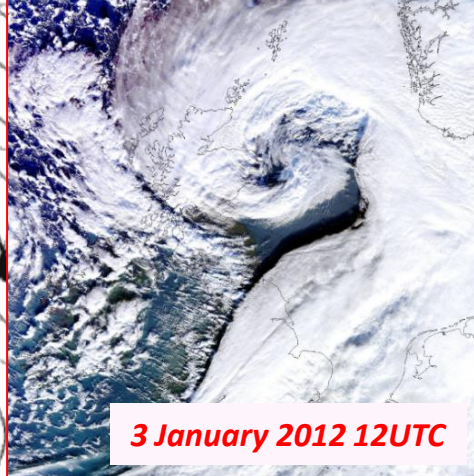
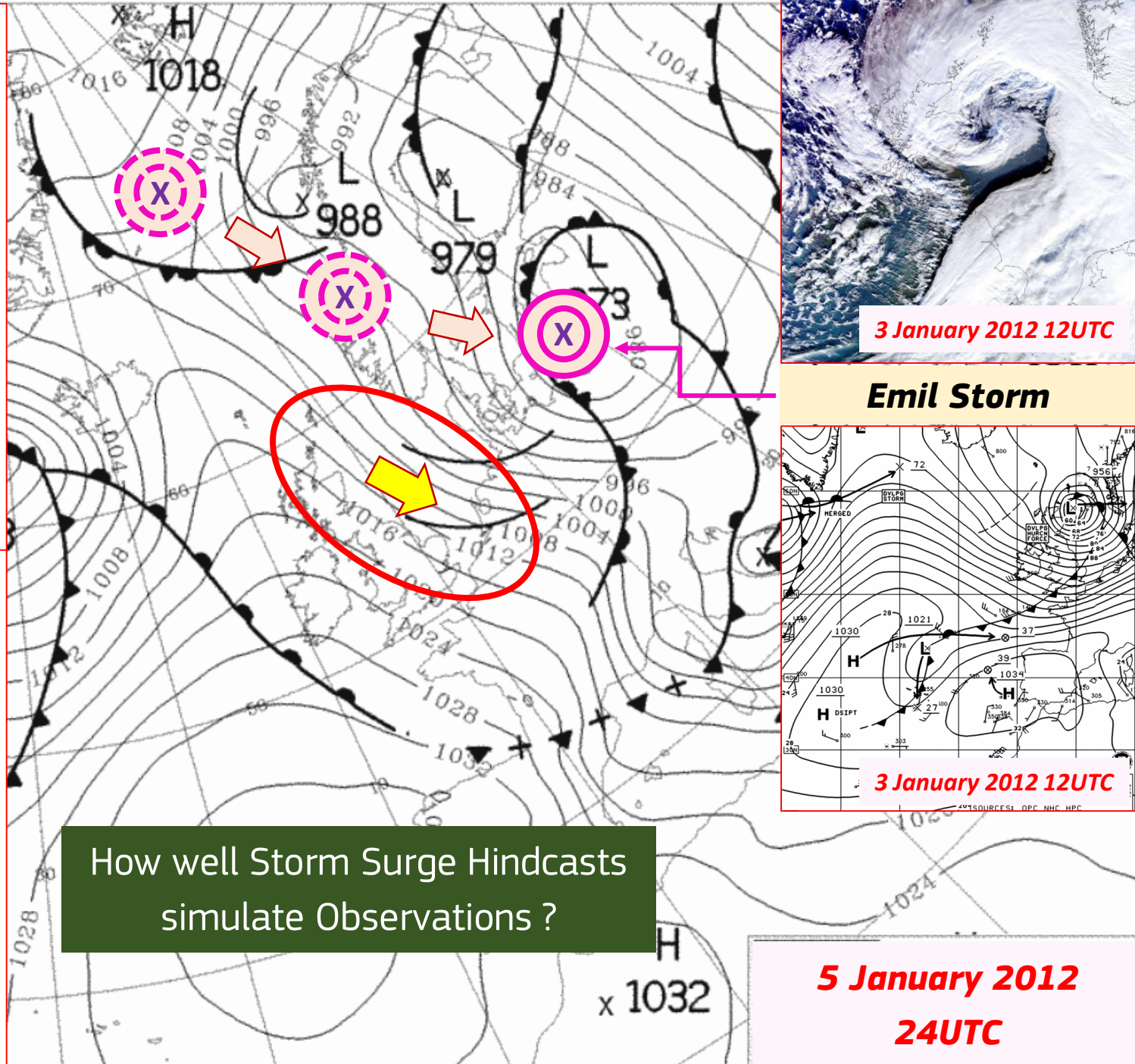
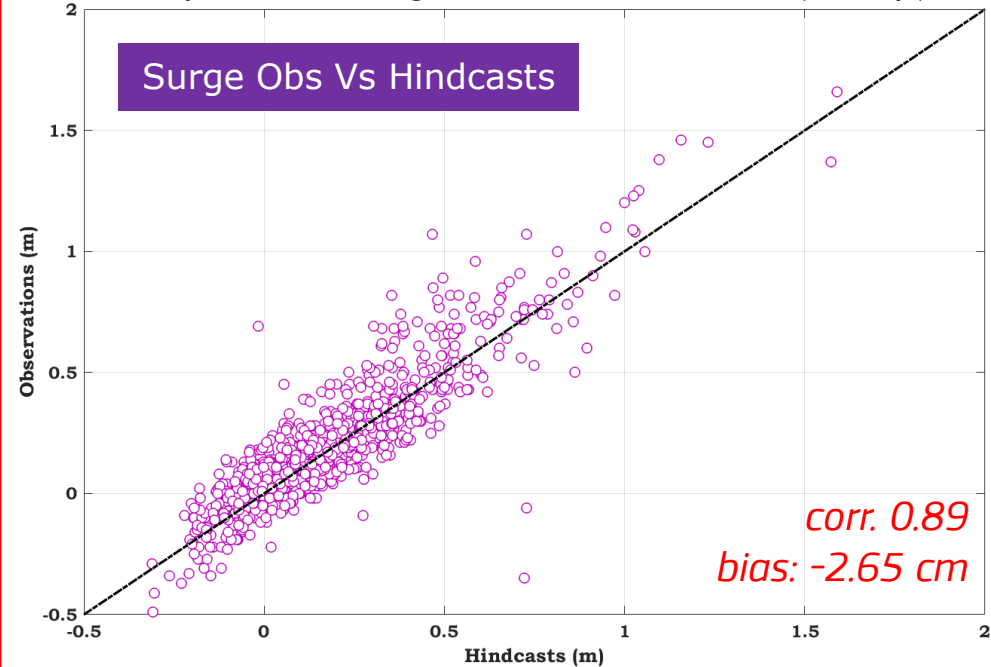


<i>Hindcasts</i>			
<i>Variables</i>	<i>Start</i>	<i>End</i>	<i>No. of days</i>
Waves – HS / Storm Surge	1 Jan 1980	30 Nov 2014	12,753
Waves – HS / River Discharge	1 Jan 1990	9 Oct 2013	8,683
Storm Surge / River Discharge	1 Jan 1990	9 Oct 2013	8,683
<i>Observations</i>			
<i>Variables</i>	<i>Start</i>	<i>End</i>	<i>No. of days</i>
LIC Waves – HS / HVH Storm Surge	22 Sep 2010	30 Dec 2014	1,561
LIC Waves / LOB River Discharge	22 Sep 2010	30 Dec 2014	1,561
HVH Storm Surge / LOB River Discharge	4 Apr 2010	30 Dec 2014	1,732
<b>Hindcasts / Observations</b>			
Common Interval for Validation	22 Sep 2010	9 Oct 2013	<b>1,114</b>

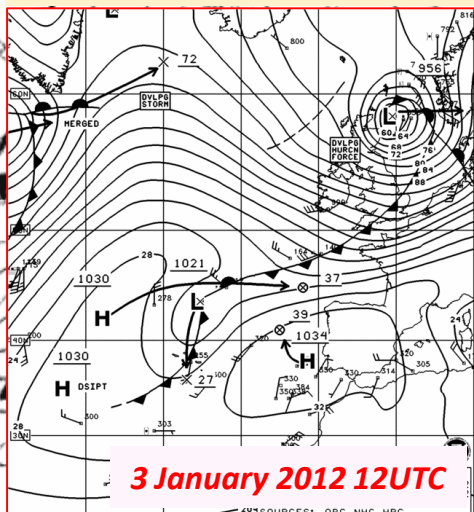
*Study over 32 RIEN (River Ending) Points  
Utilising Hindcasts of Storm Surge, Significant Wave Height & River Discharges*

- Storm surge hindcasts were performed by utilising the hydrodynamic model **Delft3D-Flow** (resol. 0.2 x 0.2 deg) forced by wind and pressure terms from ECMWF ERA-Interim reanalysis
- Wave hindcasts were generated by latest version of ECMWF **ECWAM** wave (stand-alone) model (resol. 0.25 x 0.25 deg), forced by neutral wind terms from ERA-Interim
- For river discharge hindcasts the **LISFLOOD** model developed by the floods group of the Natural Hazards Project of the Joint Research Centre (JRC), was employed (resol. 5 x 5 km)
- Validation of hindcasts was made over the **RIEN** (River Ending) point of river **Rhine (NL)** where coincident observations were available
- Considering the physical driver complexity behind interactions among surge, wave height and discharge variables hindcasts were found to perform quite well, not only simulating observation values over the common interval of interest, **but also in resolving the right type and strength of both correlation and statistical dependence**

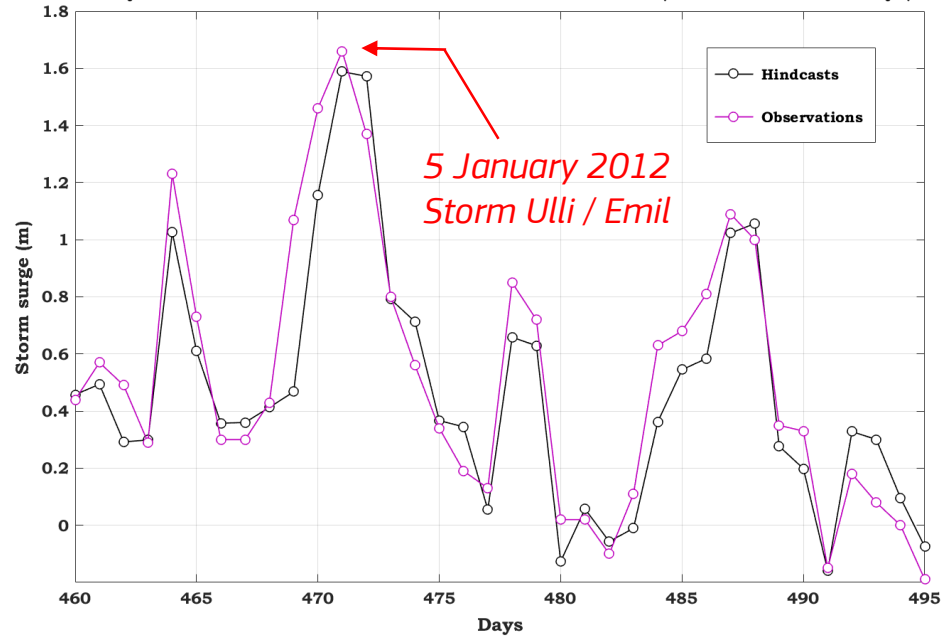
Daily maximum storm surge hindcasts Vs observations for HVH (1,114 days)

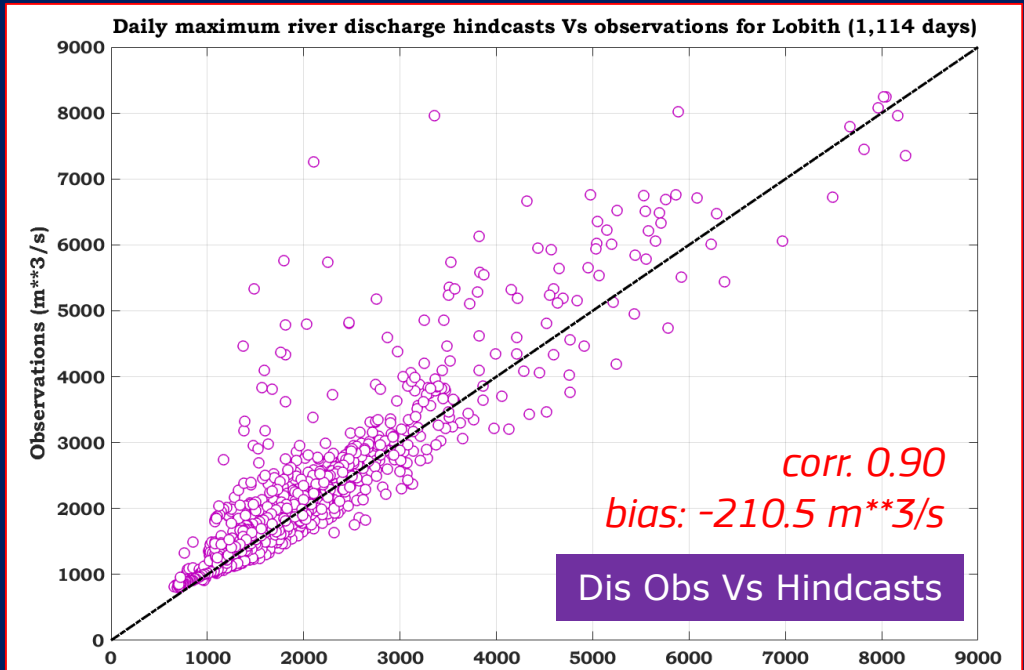
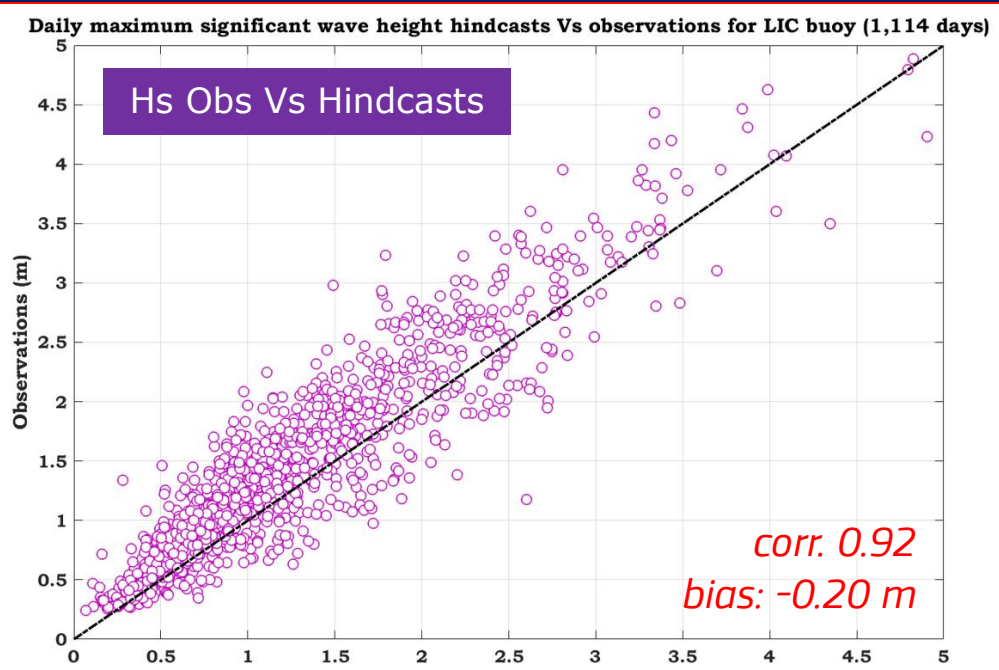


Emil Storm

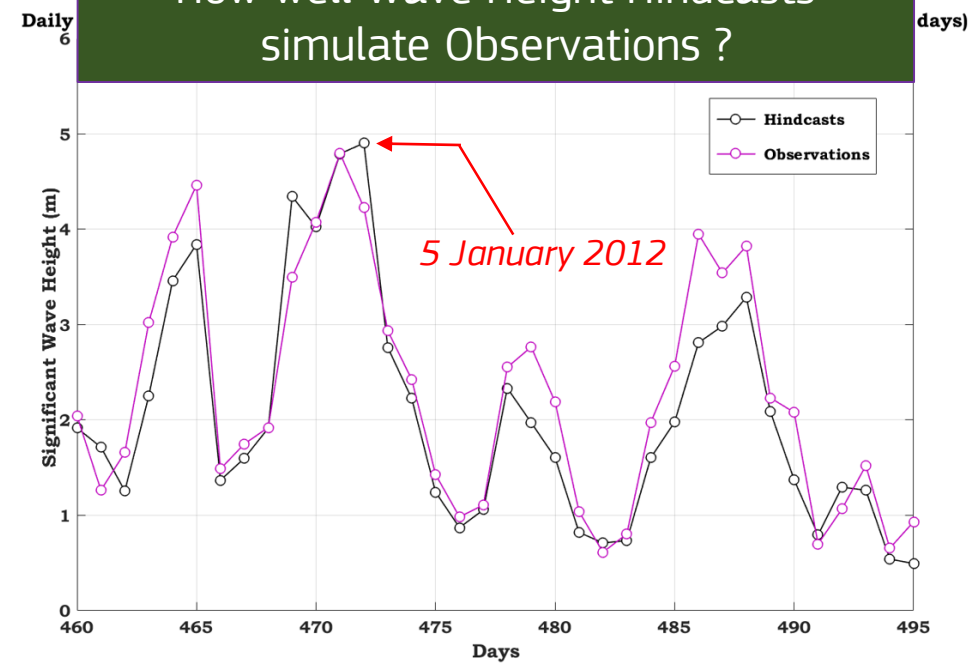


Daily maximum storm hindcasts and observations for HVH (subsection 460-495 days)

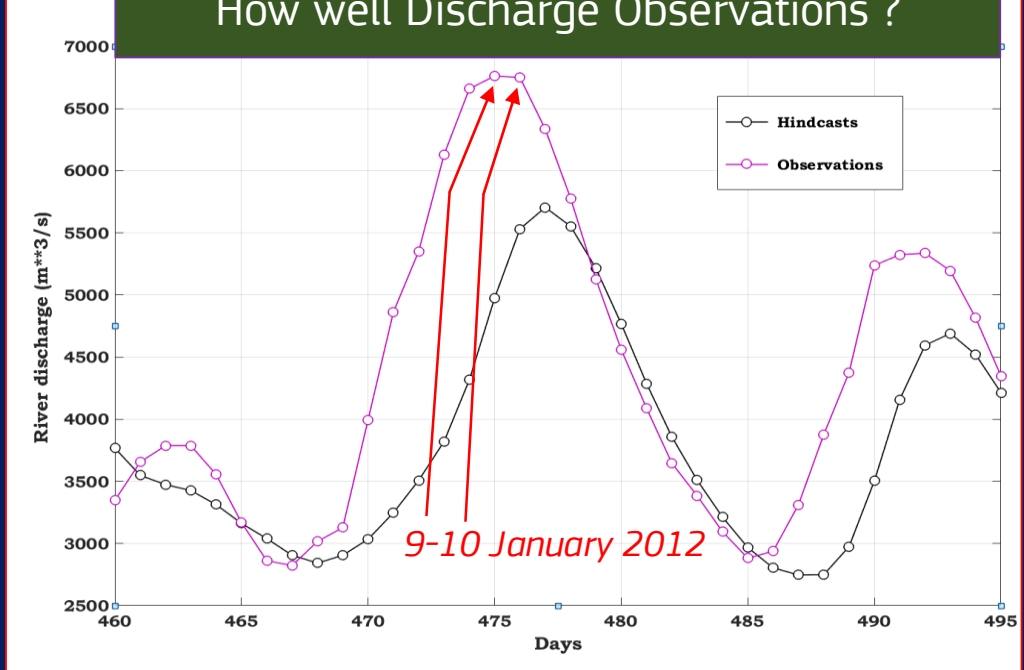




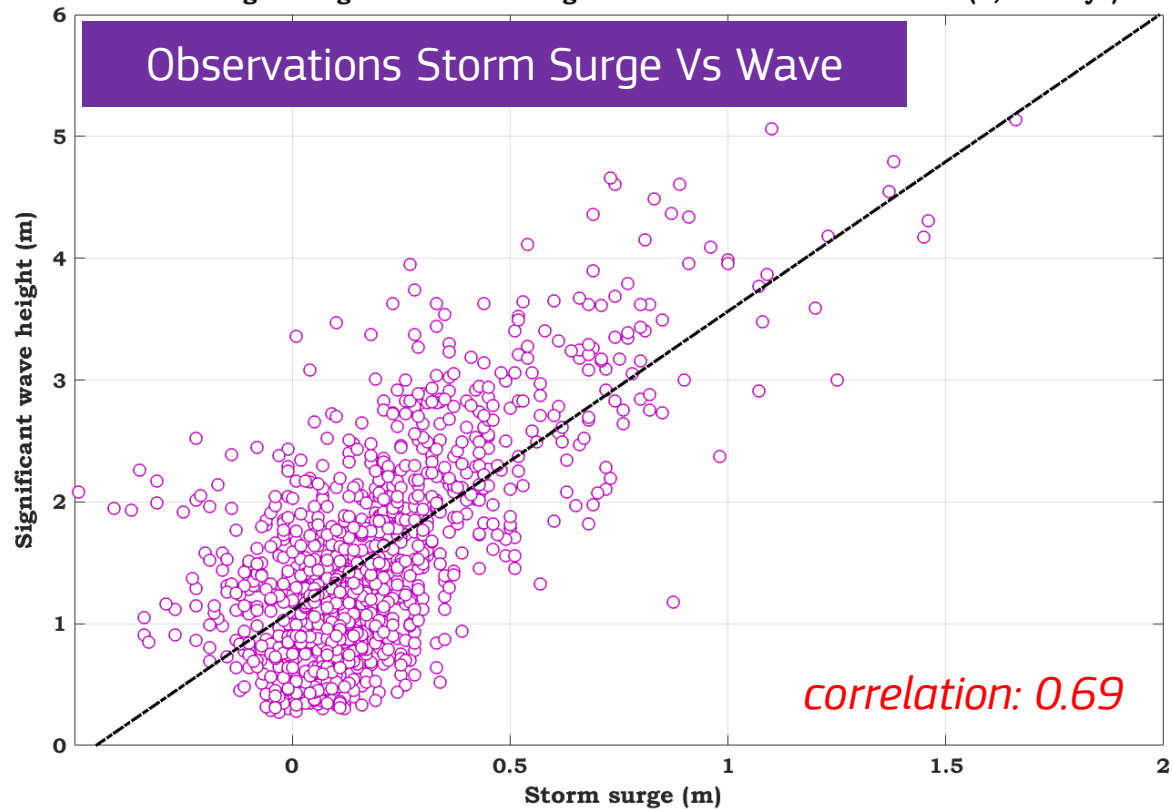
How well Wave Height Hindcasts simulate Observations ?



How well Discharge Observations ?

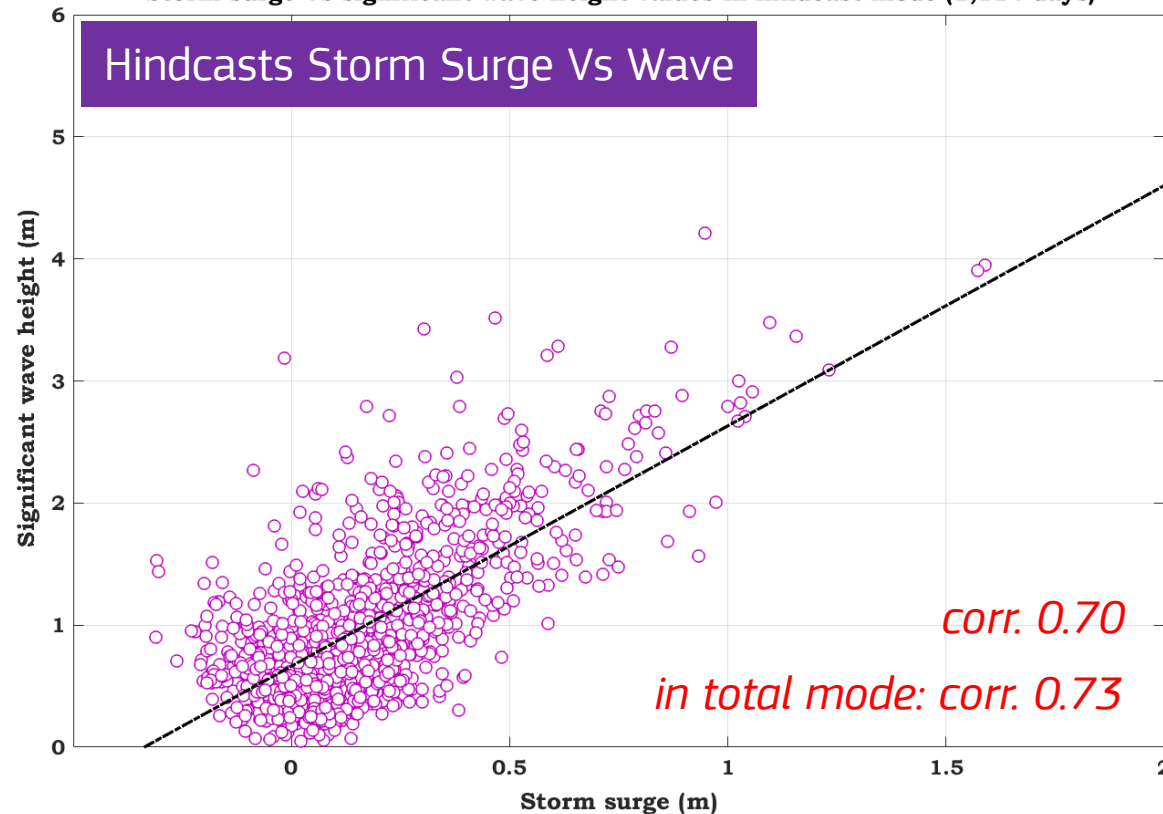


Storm surge Vs significant wave height values in observations mode (1,114 days)



Observations Mode

Storm surge Vs significant wave height values in hindcast mode (1,114 days)

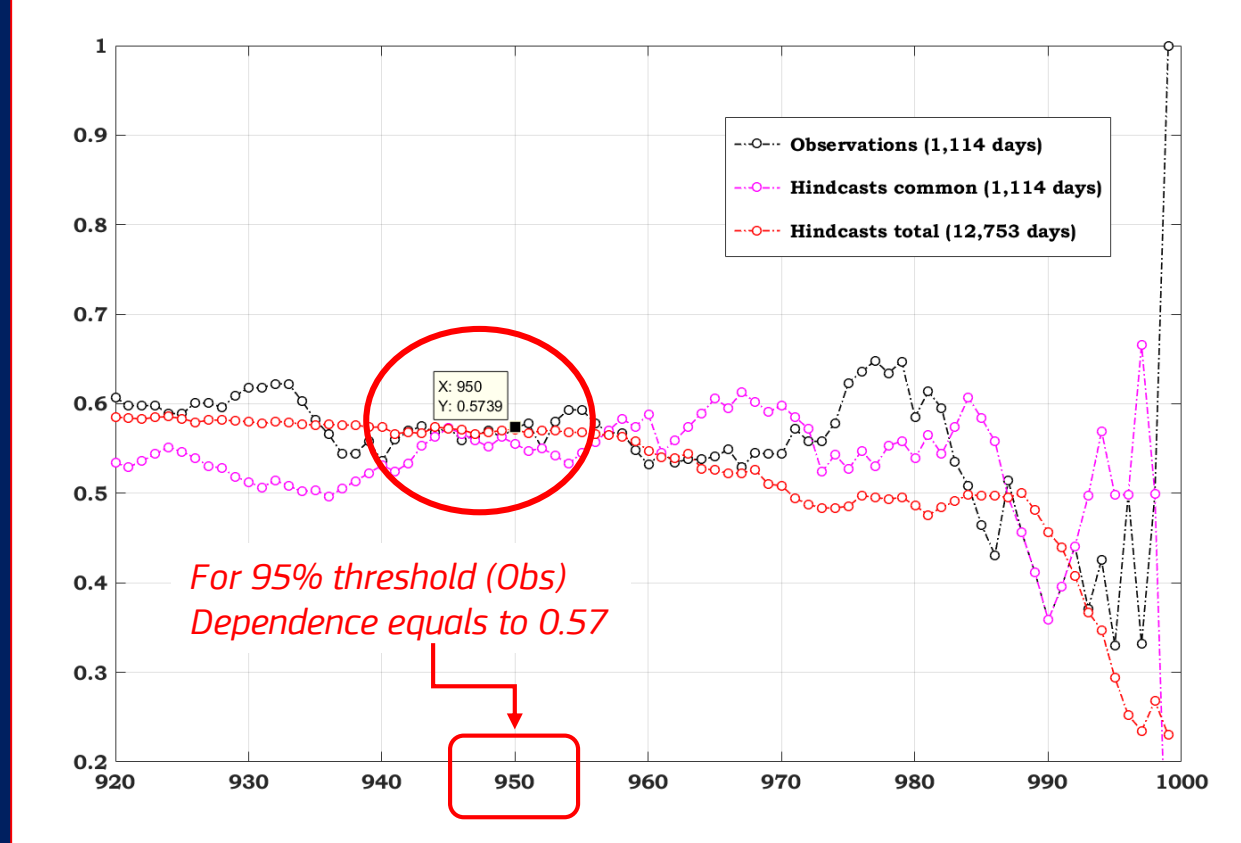
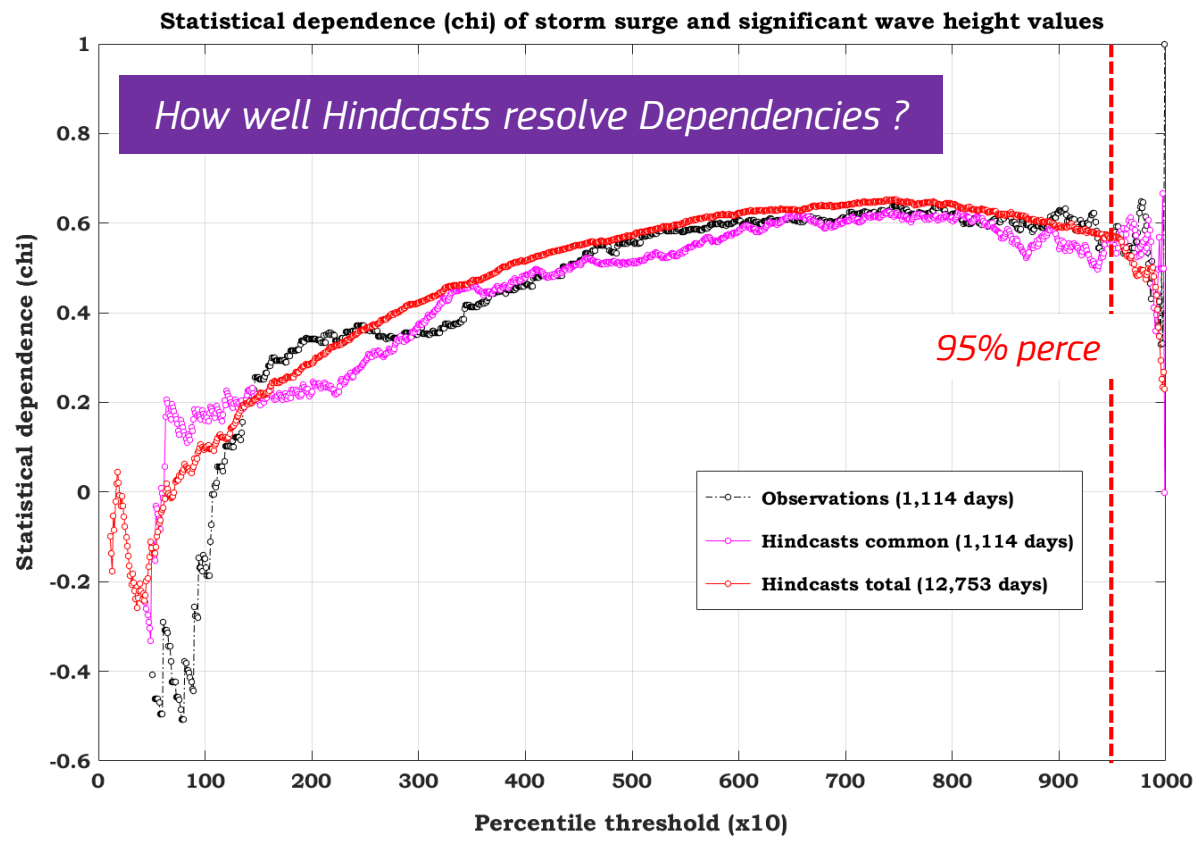


Hindcasts Mode

How well Hindcasts resolve Correlations ?

	<i>obs com</i>	<i>max (lag)</i>	<i>hind com</i>	<i>max (lag)</i>	<i>hind all</i>	<i>max (lag)</i>
<i>SUR / WAV</i>	0.6947	0.6947 (0)	0.7002	0.7002 (0)	0.7292	0.7292 (0)
<i>SUR / DIS</i>	0.1490	0.3030 (5)	0.0897	0.3208 (7)	0.0981	0.3283 (7)
<i>WAV / DIS</i>	0.1361	0.2724 (6)	0.1418	0.3683 (8)	0.1341	0.3630 (7)

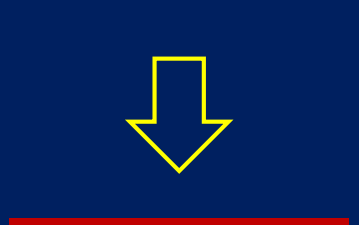
Pretty well ...



Surge Vs Wave in Obs / Hind Common / Hind Total Mode

	lead	thres	R (chiplot)	max	mat_chi	max (mat)	lag	R (taildep)	R max
obs	s / w	95%	0.6276	0.6276	0.5739	0.5739	0	0.5925	0.5925
hind_com	s / w	95%	0.5551	0.5551	0.5551	0.5551	0	0.5745	0.5745
hind_tot	s / w	95%	0.5683	0.5683	0.5712	0.5712	0	0.5850	0.5850

**Storm Surge Vs Waves**



**Pretty well ...**

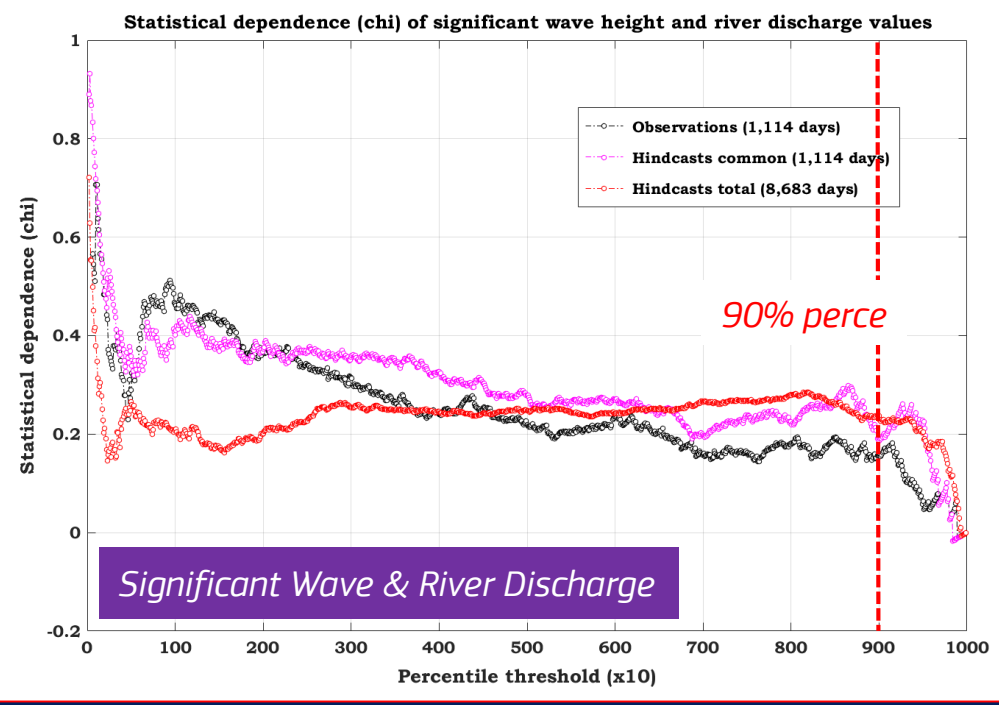
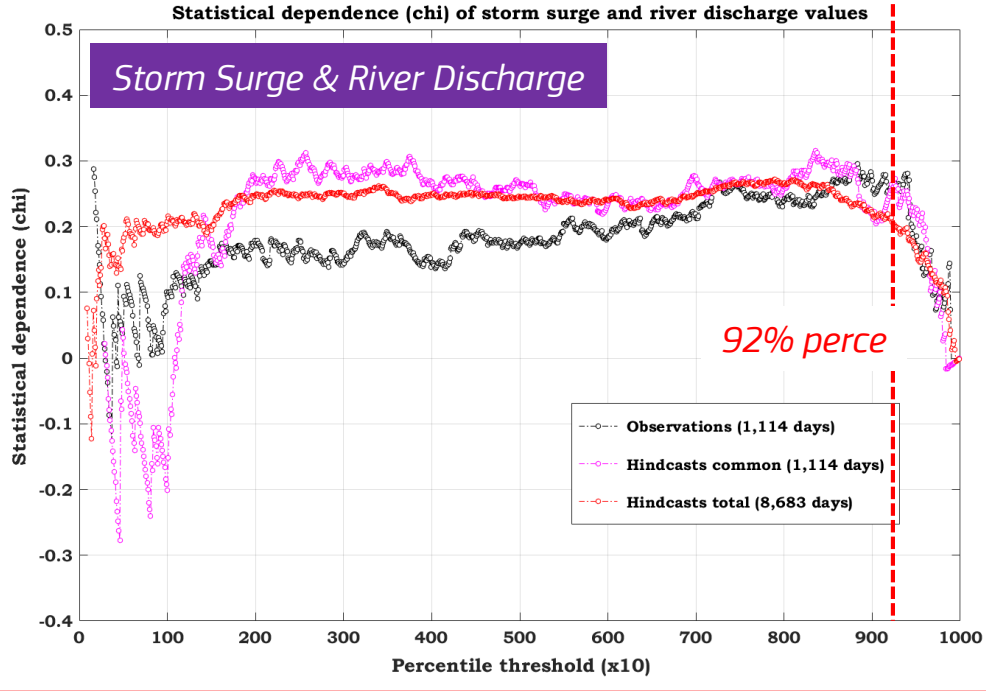


## How well Hindcasts resolve Dependencies (cont.)

### Storm Surge & River Discharge in all Modes

	<i>lead</i>	<i>thres</i>	<i>R (chiplot)</i>	<i>max</i>	<i>mat_chi</i>	<i>max (mat)</i>	<i>lag</i>	<i>R (taildep)</i>	<i>R max</i>
<i>obs</i>	<i>s / d</i>	92%	0.1798	0.2939	0.1430	0.2571	6	0.2020	0.3161
<i>hind</i>	<i>s / d</i>	92%	0.0815	0.2444	0.0874	0.2503	6	0.1571	0.3200
<i>total</i>	<i>s / d</i>	92%	0.0897	0.2272	0.0754	0.2129	6	0.1468	0.2843

→ Storm surge and river discharge hindcasts exhibit **almost identical** (max-lag) values of statistical dependence with observations

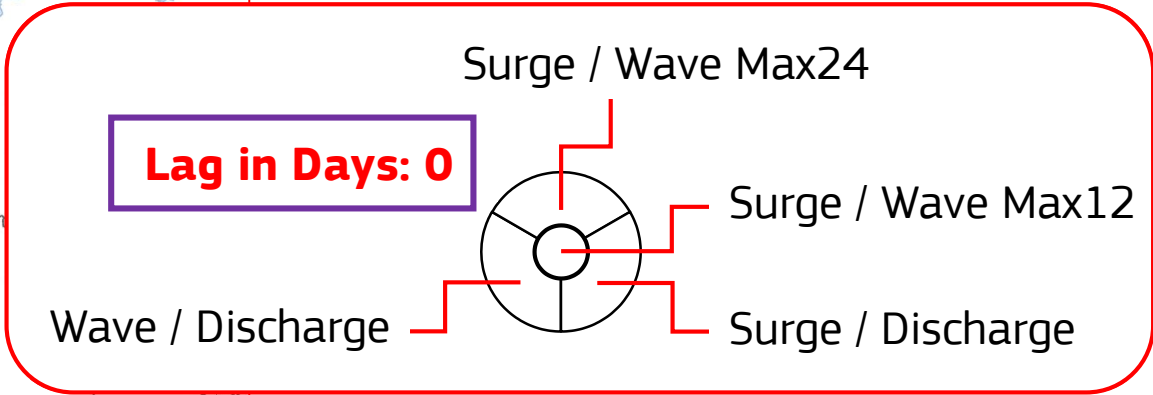
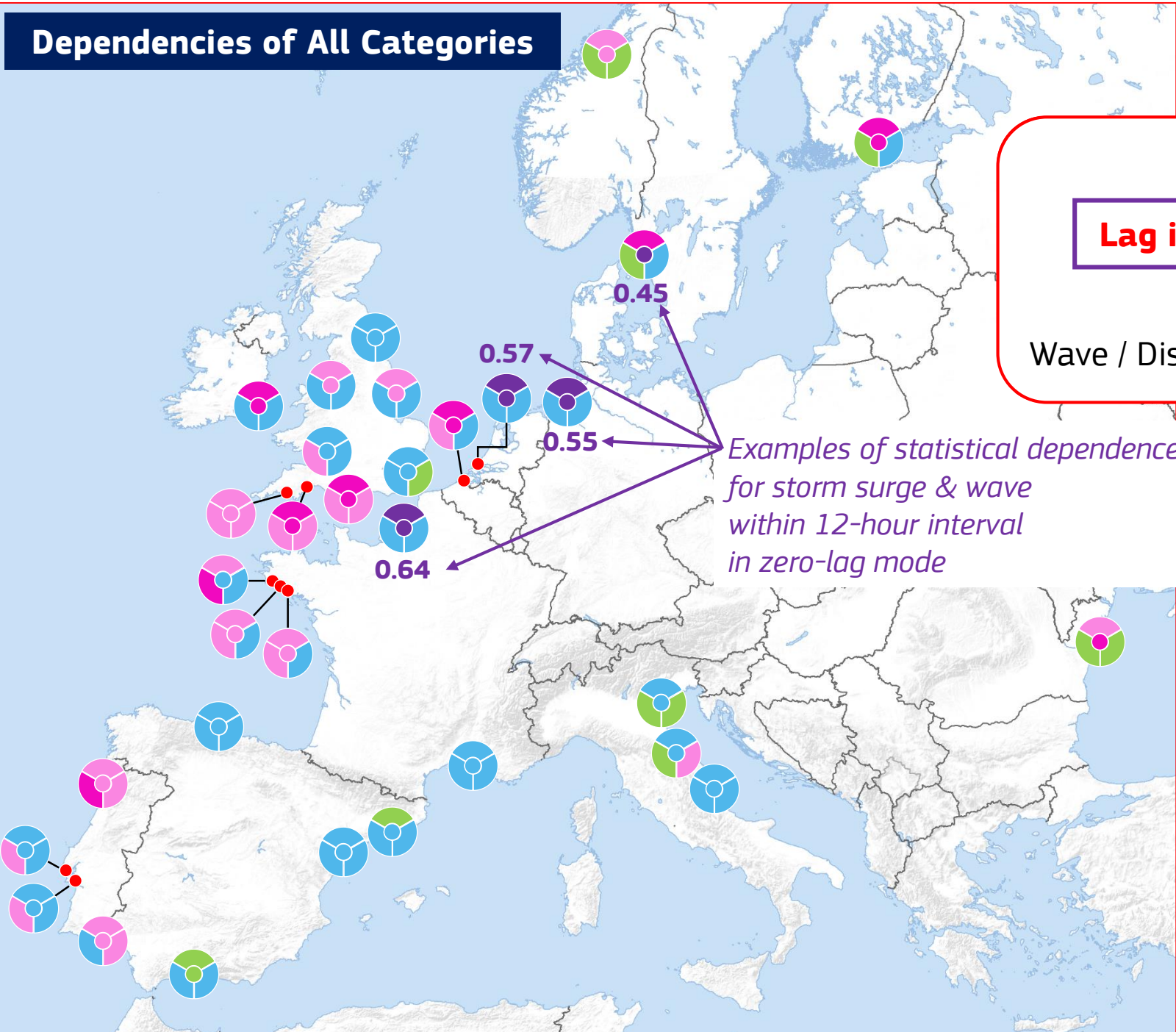


### Significant Wave & River Discharge in all Modes








	<i>lead</i>	<i>thres</i>	<i>R (chiplot)</i>	<i>max</i>	<i>mat_chi</i>	<i>max (mat)</i>	<i>lag</i>	<i>R (taildep)</i>	<i>R max</i>
<i>obs</i>	<i>w / d</i>	90%	0.0996	0.2145	0.0427	0.1576	6	0.1346	0.2495
<i>hind</i>	<i>w / d</i>	90%	0.1001	0.2972	0.0310	0.2281	8	0.1346	0.3317
<i>total</i>	<i>w / d</i>	90%	0.0900	0.2544	0.0823	0.2467	7	0.1704	0.3348

→ Significant wave and river discharge hindcasts exhibit **similar** (max-lag) values of statistical dependence with observations

# Dependencies of All Categories



*Adaptation of Svensson & Jones, 2003 Tables*

	Dependence (chi)	Category
	$chi \leq -0.06$	Negative
	$-0.05 \leq chi \leq 0.05$	Zero
	$0.06 \leq chi \leq 0.14$	Low
	$0.15 \leq chi \leq 0.24$	Modest
	$0.25 \leq chi \leq 0.34$	Well
	$0.35 \leq chi \leq 0.44$	Strong
	$chi \geq 0.45$	Very Strong

## Results: Dependencies in Zero LAG Mode

Results are presented by means of analytical tables and detailed maps referring to both correlation and dependence ( $\chi$ ) values being estimated over RIEN points

It is then straightforward to estimate the joint probability value as the inverse of the joint return period



$$T_{X,Y} = \sqrt{\frac{T_x \cdot T_y}{\chi^2}}$$

## Results: Dependencies in Max LAG Mode

RIEN	River	Ocean / Sea	L	S / W12	L	S / W24	L	S / R24	L	W / R24
01	Po (IT)	Adriatic Sea	0	mod	0	mod	4	mod	3	mod
02	Metauro (IT)	Adriatic Sea	0	mod	0	mod	0	well	0	mod
03	Vibrata (IT)	Adriatic Sea	0	mod	0	mod	2	well	1	mod
08	Rhone (FR)	Gulf of Lion	0.5	mod	0	mod	4	well	2	mod
04	Foix (ES)	Balearic Sea	0	mod	0	low	1	mod	0	mod
05	Ebro (ES)	Balearic Sea	0	mod	0	mod	3	mod	>7	well
06	Velez (ES)	Alboran Sea	0	low	0	low	0	mod	0	mod
07	Sella (ES)	Bay of Biscay	0.5	mod	0	mod	1	mod	1	mod
10	Moros (FR)	Bay of Biscay	0	mod	0	well	0	mod	0	strong
11	Aven (FR)	Bay of Biscay	0	well	0	well	0	mod	3	strong
12	Blavet (FR)	Bay of Biscay	0	well	0	well	0	mod	1	strong
13	Owenavorrhagh (IE)	Irish Sea	0	strong	0	strong	2	mod	3	mod
21	Mersey (UK)	Irish Sea	0	well	0	well	2	mod	1	mod
20	Severn (UK)	Bristol Channel	0	mod	0	mod	3	well	3	well
15	Orkla (NO)	Norwegian Sea	0	well	0	well	2	low	0	low
16	Vantaa (FI)	Baltic Sea	0	strong	0	strong	0	mod	2	mod
22	Tyne (UK)	North Sea	0.5	mod	0	mod	0	mod	0	mod
27	Humber (UK)	North Sea	0	well	0	well	0	mod	1	mod
14	Goeta Aelv (SE)	North Sea	0.5	v. strong	1	strong	1	mod	2	mod
17	Rhine (NL)	North Sea	0	v. strong	0	v. strong	4	well	5	well
18	Weser (DE)	North Sea	0	v. strong	0	v. strong	6	well	6	well
19	Schelde (BE)	North Sea	0	strong	0	strong	1	mod	2	well
25	Thames (UK)	North Sea	1	well	1	mod	0	low	1	mod
09	Bethune (FR)	English Channel	0	v. strong	0	v. strong	4	well	3	well
24	Avon (UK)	English Channel	0	strong	0	strong	2	well	3	well
26	Exe (UK)	English channel	0	~strong	0	strong	0	well	1	well
23	Tamar (UK)	English Channel	0	well	0	well	0	well	0	well
28	Danube (RO)	Black Sea	0.5	strong	0	well	>7	mod	0	low
31	Douro (PT)	Atlantic Ocean	0	well	0	well	1	well	1	strong
29	Tagus (PT)	Atlantic Ocean	0.5	mod	0	mod	>7	well	4	well
30	Sado (PT)	Atlantic Ocean	0	mod	0	mod	3	well	4	strong
32	Guadiana (ES)	Atlantic Ocean	0	well	0	well	3	well	3	~strong



Overall, besides the demonstration of how to apply **statistical dependence methodologies & techniques**

- The highest values of (strong / very strong) correlations and dependencies were found **between surges and waves** mainly **over North Sea and English Channel** taking place on the same day (**zero-lag mode**)
- **Moderate to well** category dependencies were found **for most sea areas**, also on a **zero-lag mode**
- In the case of **surge and river discharge**, **moderate to well** category values were found in most cases but **NOT in a zero-lag mode** as in surge & wave case
- It became clear that in order to achieve such (relatively high) values, **considerable lag time interval** of a few days was required with surge clearly leading discharge values
- For the case of **wave and river discharge**, **well to strong** category values were found but once more mostly **in NON-zero lag mode** indicating the necessity of a considerable lag time interval for dependence to reach such (well / strong) values with wave distinctly leading discharge values

# Going After High-Impact



# Compound Events ...

