

Climate model wind stress biases in the northern low latitudes from a momentum balance perspective.

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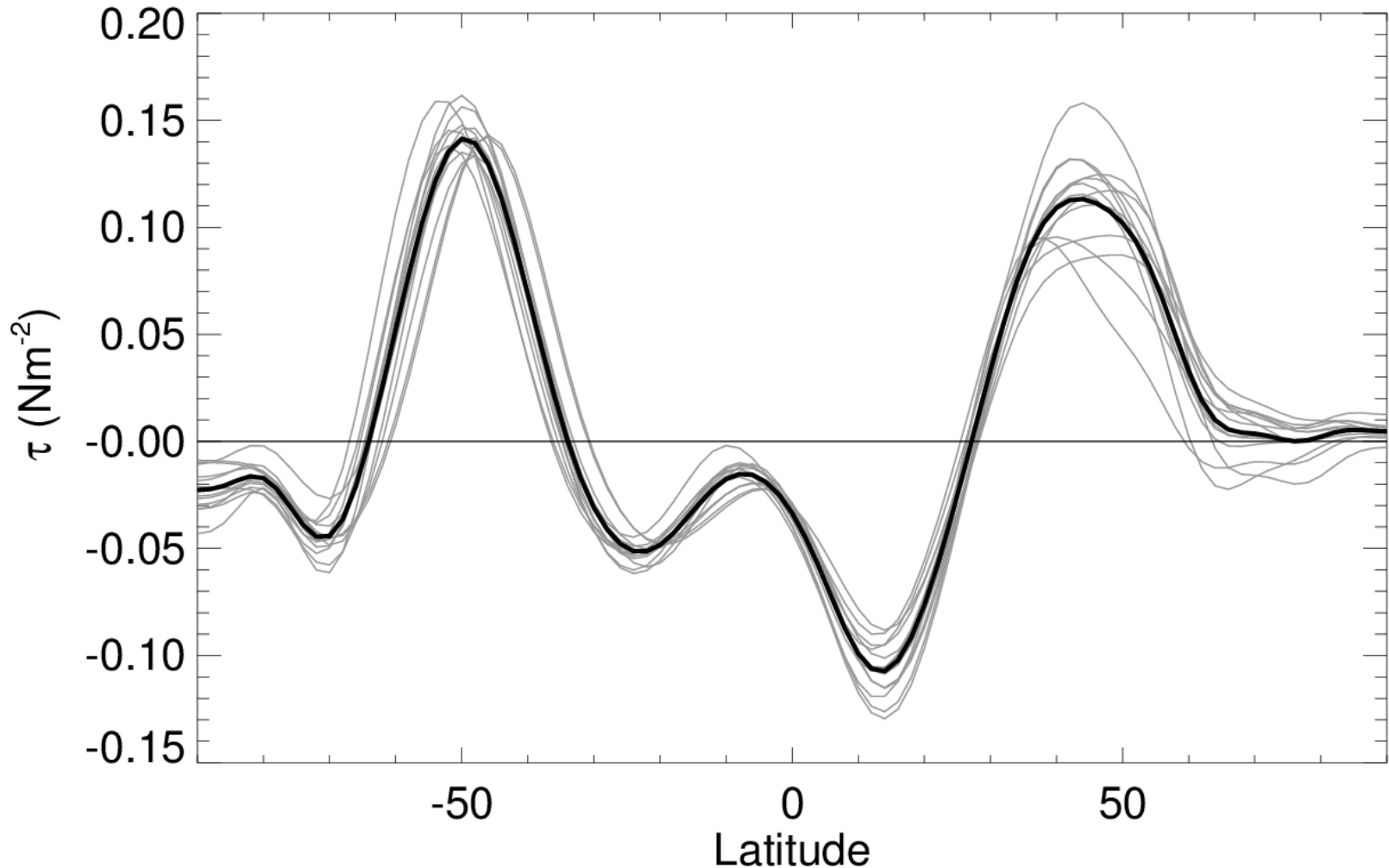
## Surface Wind Stress

- CMIP5 variable (*tauu*) = surface downward eastward wind stress (excluding gravity wave drag surface stress)
- ERA-Interim variable = Eastward turbulent surface stress. (i.e. not including GWD surface stress)

**Sign Convention:** will show the downward stress  
i.e. -1 x forcing on the atmosphere

# Zonal mean surface wind stress during DJF, 1979-2005

Surface wind stress, DJF, 1979-2005

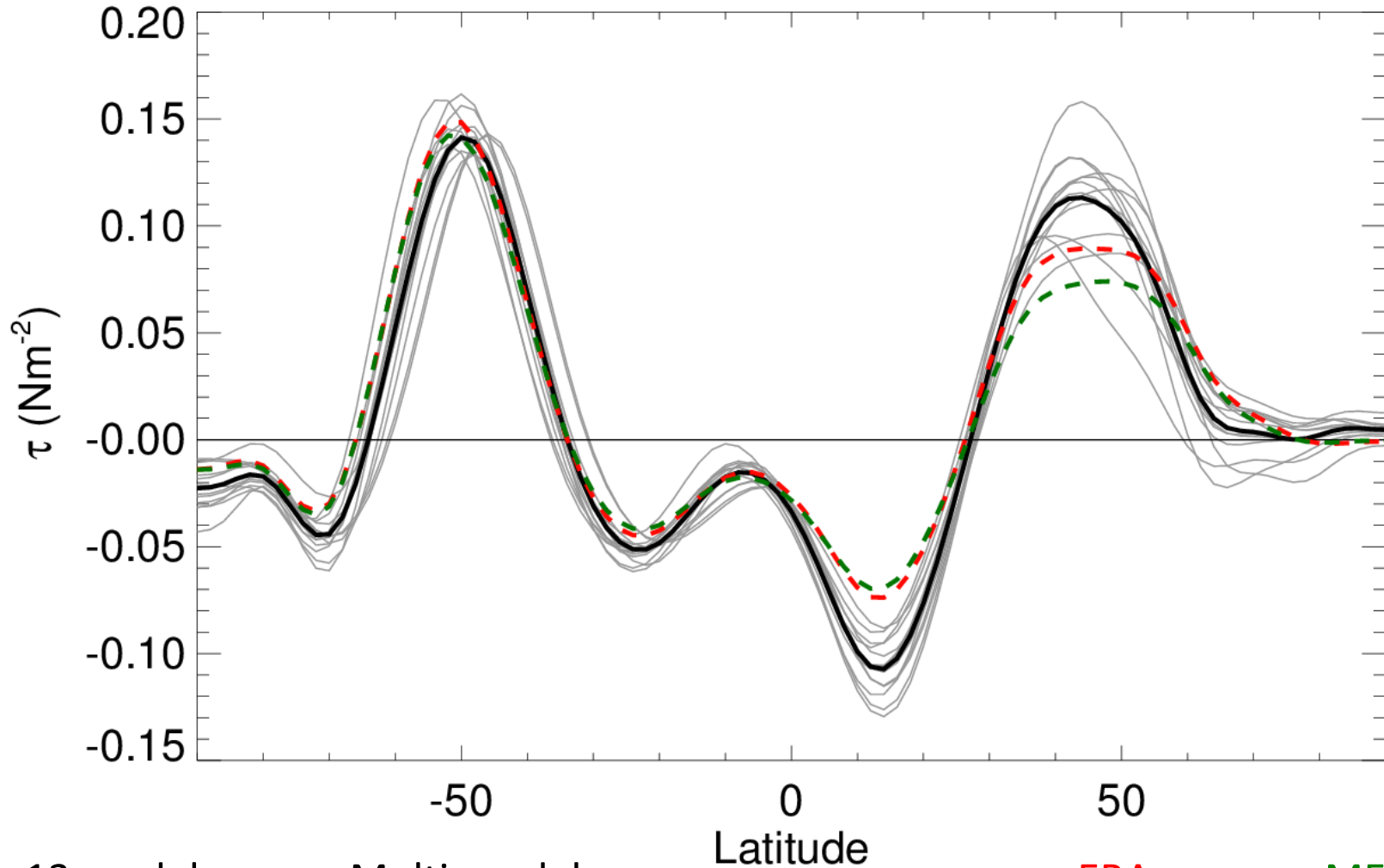


— 13 models    — Multi-model mean

(Coupled historical simulations)

# Zonal mean surface wind stress during DJF, 1979-2005

## Surface wind stress, DJF, 1979-2005



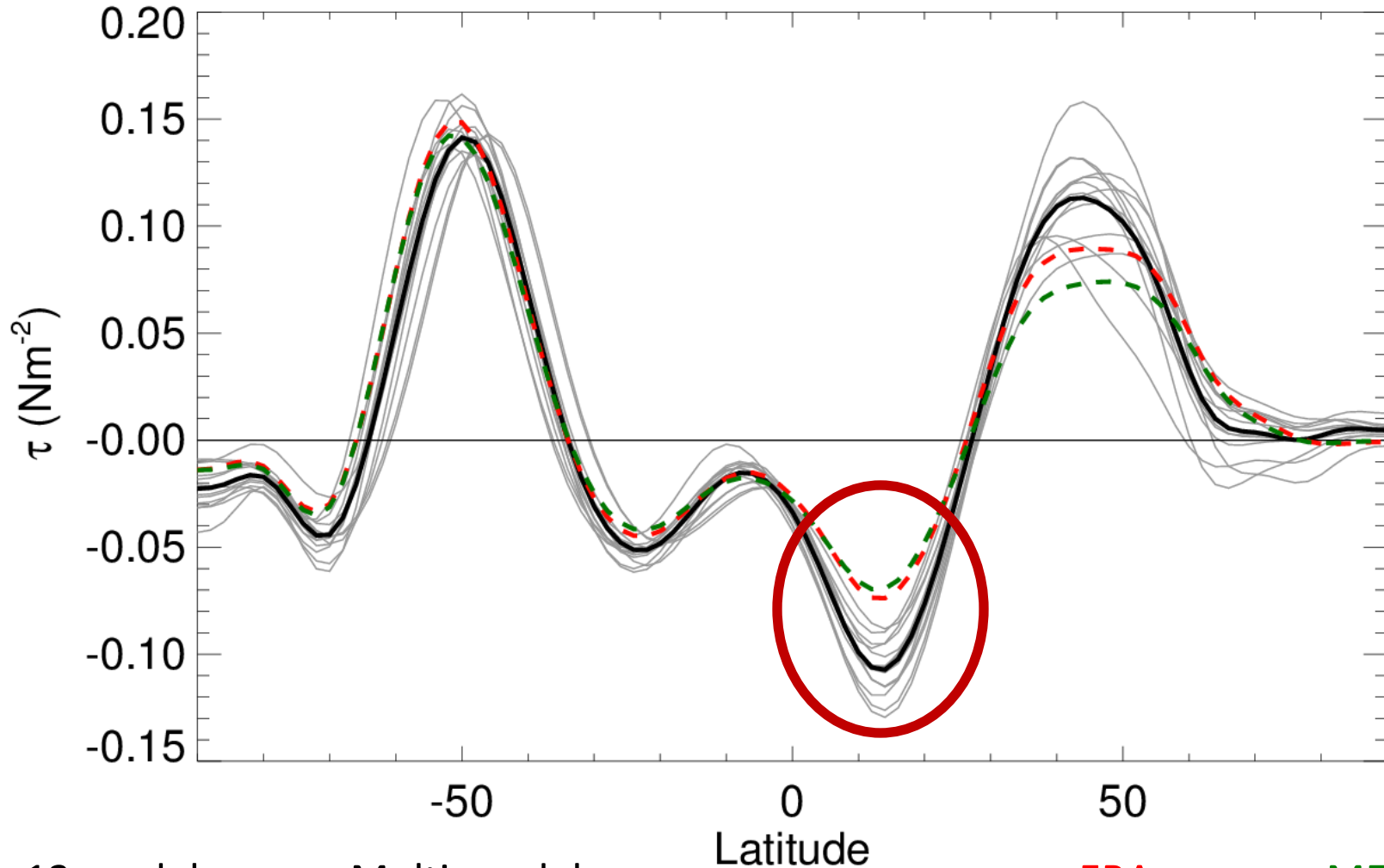
— 13 models    — Multi-model mean

--- ERA    --- MERRA



# Zonal mean surface wind stress during DJF, 1979-2005

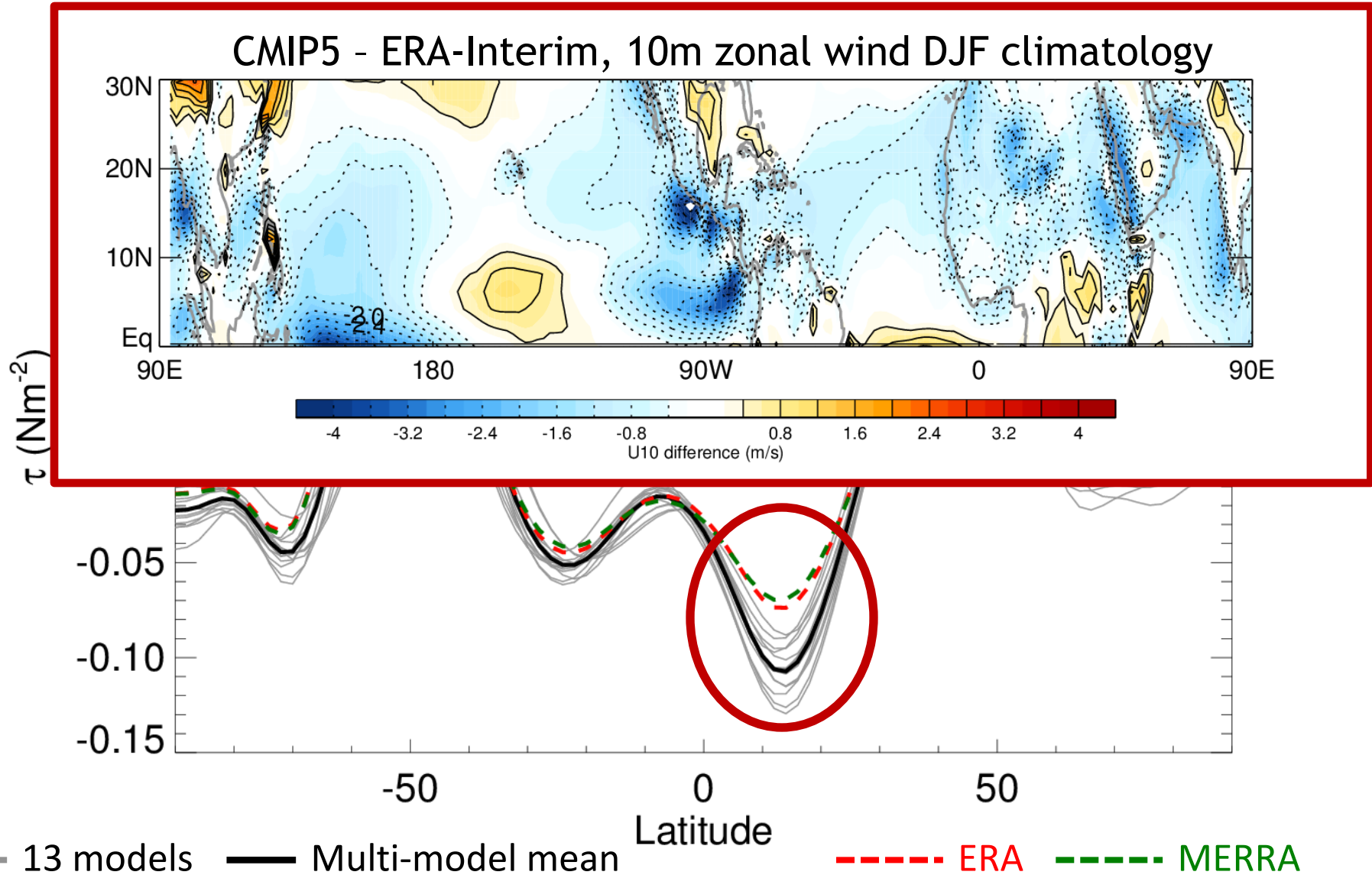
## Surface wind stress, DJF, 1979-2005



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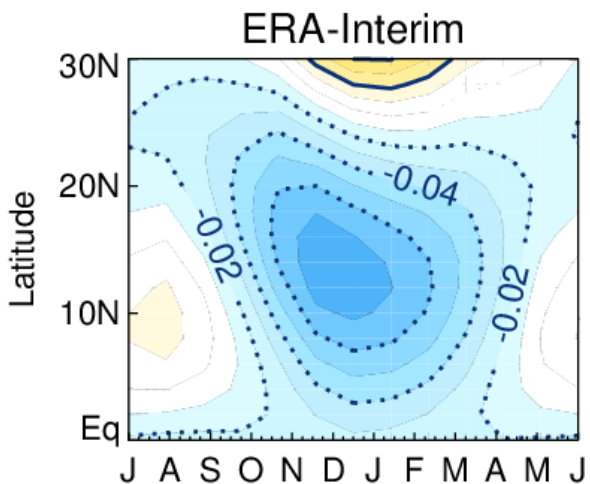
- - - ERA    - - - MERRA

# Zonal mean surface wind stress during DJF, 1979-2005

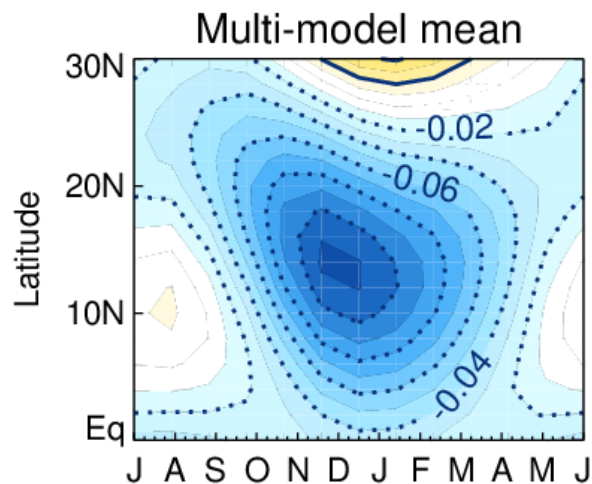


# Seasonal evolution of low latitude wind stress differences

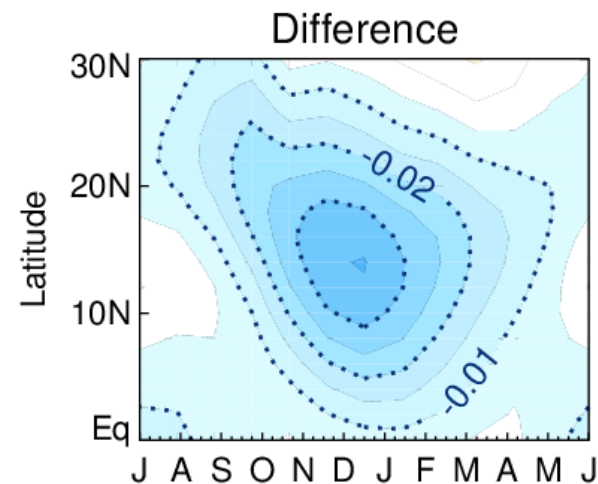
## ERA-Interim vs multi-model mean



ERA-Interim



CMIP5



CMIP5 - ERA-Interim

What can we learn about these zonal mean surface wind stress differences from the vertically integrated momentum balance?

# The Vertically Integrated Momentum Balance

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The zonal momentum equation on a pressure surface:

$$\frac{\partial u}{\partial t} = fv - \frac{1}{a \cos \varphi} \frac{\partial \Phi}{\partial \lambda} - \frac{1}{a \cos^2 \varphi} \frac{\partial (uv \cos^2 \varphi)}{\partial \varphi} - \frac{1}{a \cos \varphi} \frac{\partial (uu)}{\partial \lambda} - \frac{\partial (u\omega)}{\partial p} + F_u + X$$

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Coriolis  
Force

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Geopotential  
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Tendency from  
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Tendency from other parameterizations  
(GWD, horizontal diffusion etc)

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(GWD, horizontal diffusion etc)

Calculate the mass weighted vertical integral at each lon and lat

$$[.] = \frac{1}{g} \int_0^{p_s(\lambda, \varphi, t)} (.) dp$$

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The zonal momentum equation on a pressure surface:

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Calculate the mass weighted vertical integral at each lon and lat

$$[.] = \frac{1}{g} \int_0^{p_s(\lambda, \varphi, t)} (.) dp$$

Then take the zonal mean.

# The Vertically Integrated Momentum Balance

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Don't have this  
for CMIP5



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$[F_u] = -\tau_u$

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$[F_u] = -\tau_u$

$-u_s \omega_s$

Don't have this for CMIP5

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$$[fv] - \left[ \frac{1}{a \cos \varphi} \frac{\partial \Phi}{\partial \lambda} \right] - \left[ \frac{1}{a \cos^2 \varphi} \frac{\partial (uv \cos^2 \varphi)}{\partial \varphi} \right] - \left[ \frac{1}{a \cos \varphi} \frac{\partial (uu)}{\partial \lambda} \right] - u_s \omega_s = \tau_u$$

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Upon taking the zonal mean...

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Mountain Torque (M)

Upon taking the zonal mean...

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 small small

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↑ small small


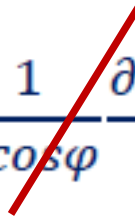
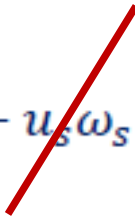
Mountain Torque (M)

Upon taking the zonal mean...

$$[fv] + M - \left[ \frac{1}{a \cos^2 \varphi} \frac{\partial (uv \cos^2 \varphi)}{\partial \varphi} \right] = \tau_u$$

# The Vertically Integrated Momentum Balance

$$[fv] - \left[ \frac{1}{a \cos \varphi} \frac{\partial \Phi}{\partial \lambda} \right] - \left[ \frac{1}{a \cos^2 \varphi} \frac{\partial (uv \cos^2 \varphi)}{\partial \varphi} \right] - \left[ \frac{1}{a \cos \varphi} \frac{\partial (uu)}{\partial \lambda} \right] - u_s \omega_s = \tau_u$$

small small

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Upon taking the zonal mean...

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Resolved Dynamics Terms

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↑~~small~~~~small~~

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Resolved Dynamics Terms

Surface Wind Stress



# The Vertically Integrated Momentum Balance

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Mountain Torque (M)

Can we explain the CMIP vs Reanalysis difference in surface wind stress through a difference in the resolved dynamics terms

Upon taking the zonal mean...

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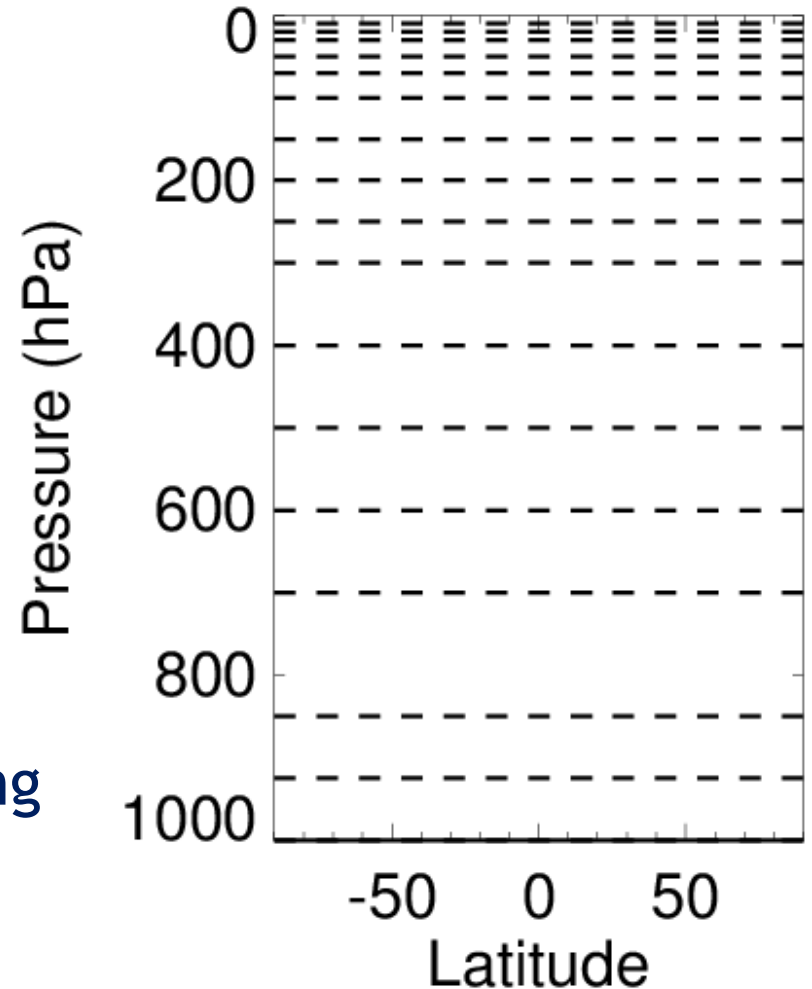
Resolved Dynamics Terms

Surface Wind Stress

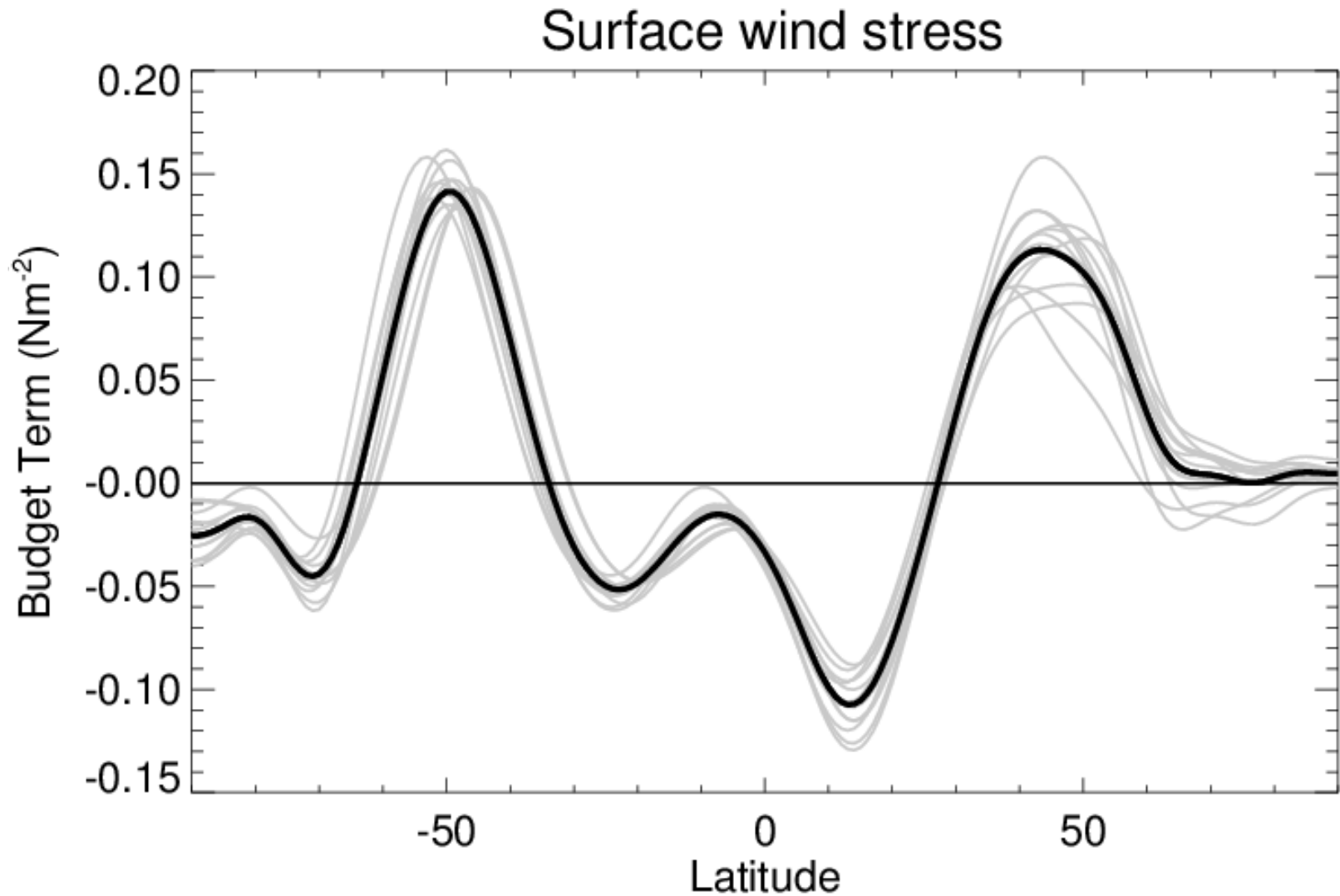
Calculated using the 17 standard CMIP5 pressure levels

Vertical integral performed on monthly mean fields using monthly mean surface pressure.

Momentum fluxes calculated using 6 hourly instantaneous fields.



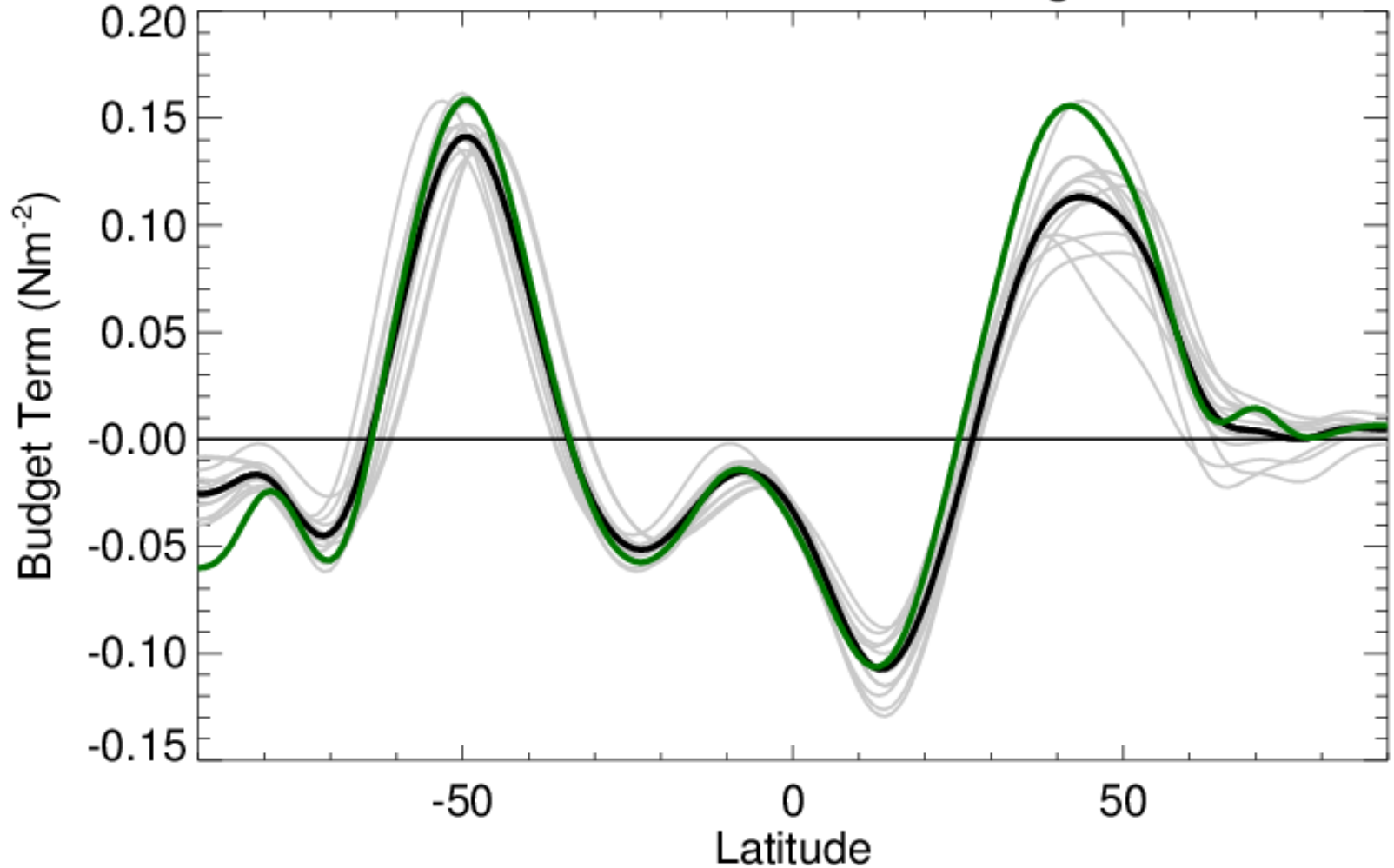
# The budget closure in the CMIP5 models (DJF)



— 13 models    — Multi-model mean

# The budget closure in the CMIP5 models (DJF)

Surface wind stress and budget sum



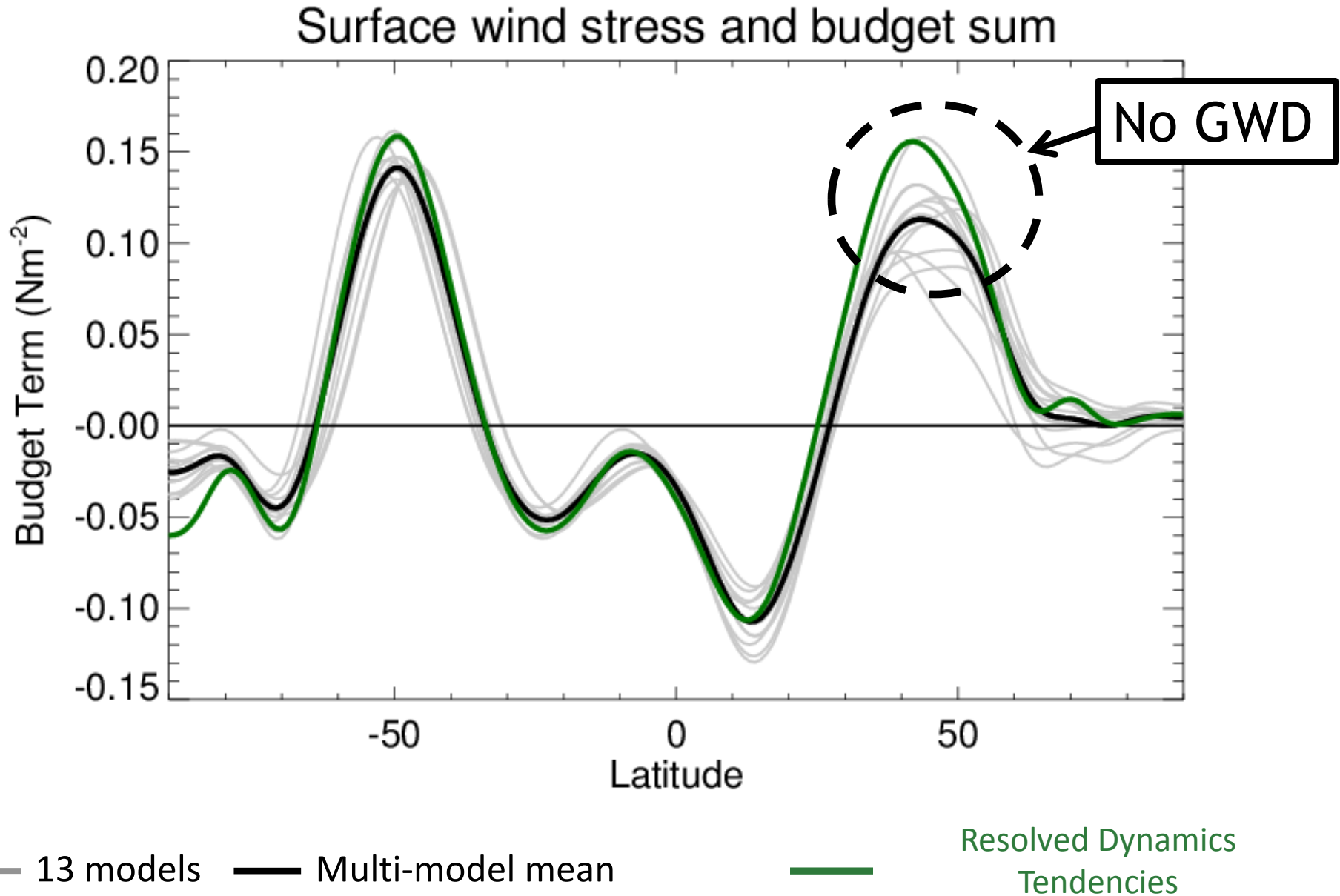
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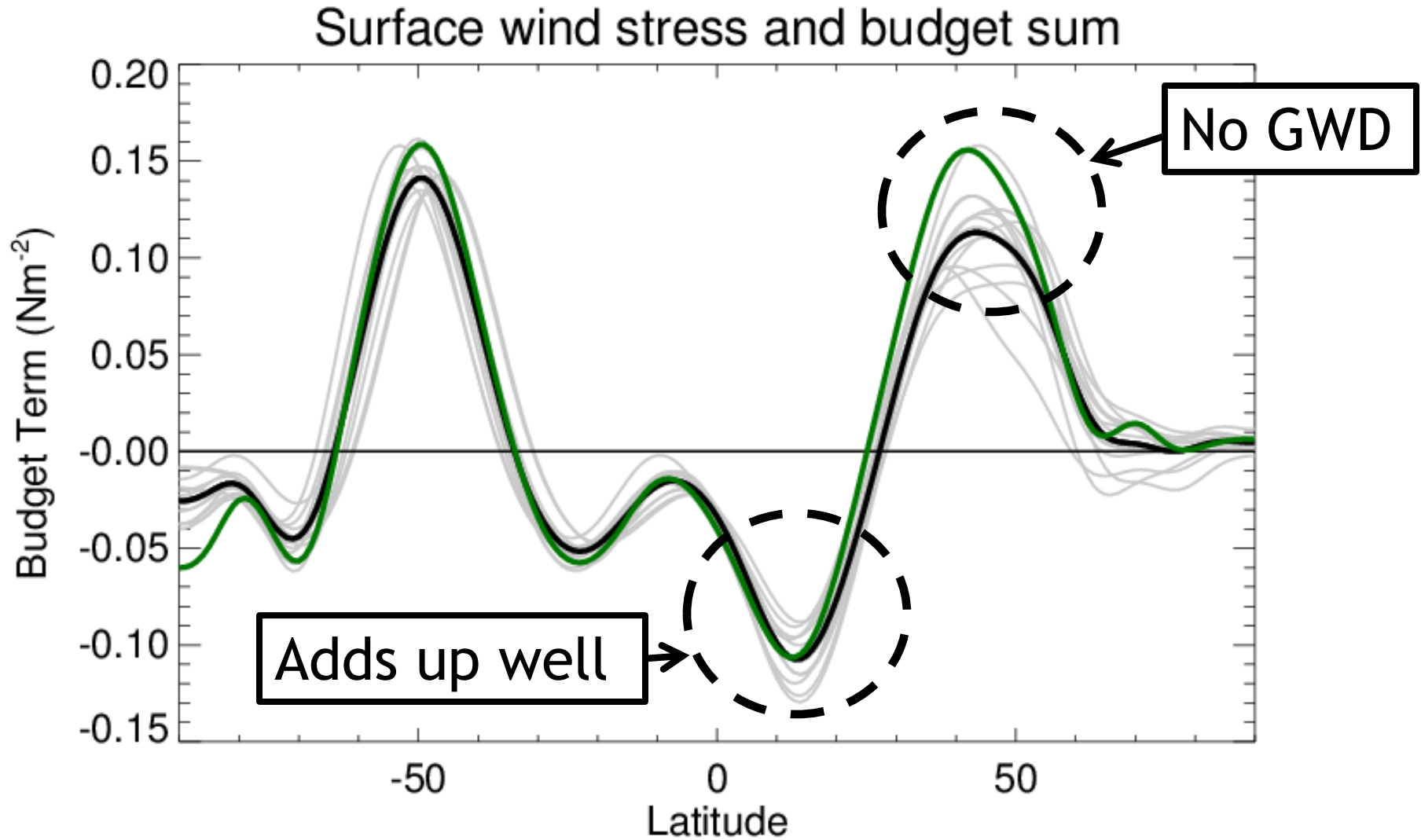
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Resolved Dynamics  
Tendencies

# The budget closure in the CMIP5 models (DJF)



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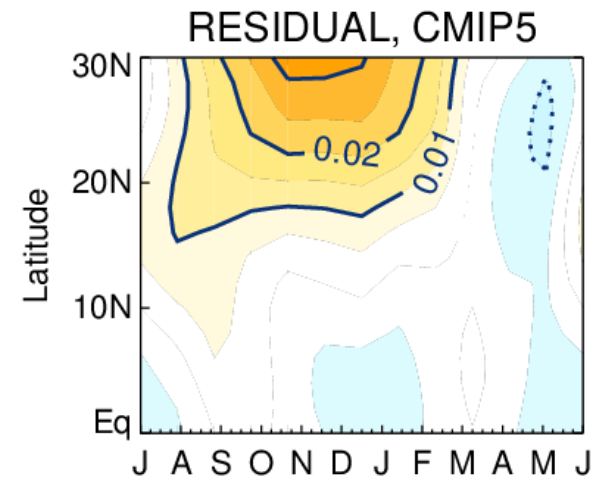
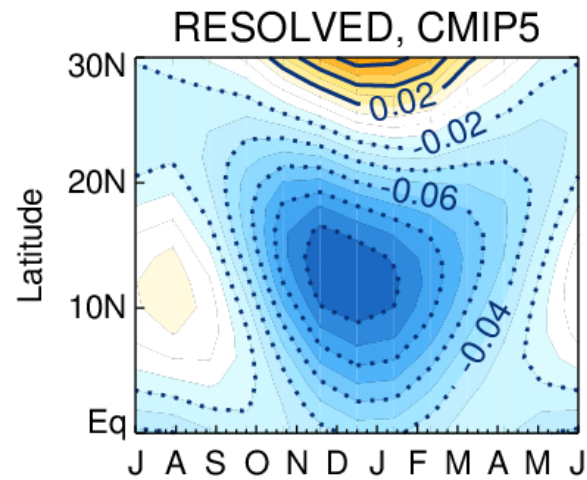
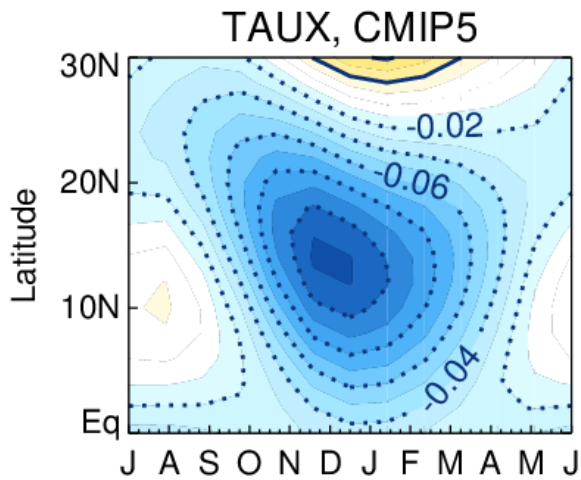
— 13 models

— Multi-model mean

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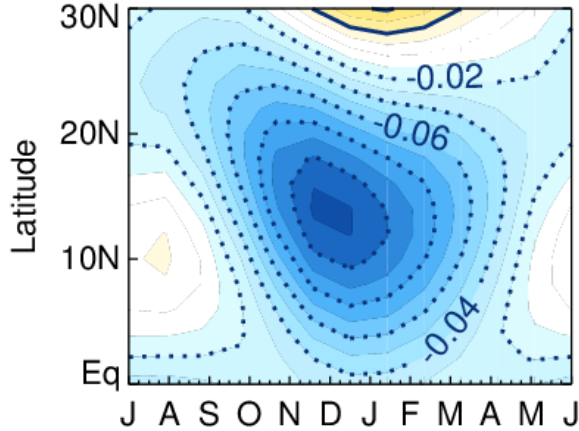
Resolved Dynamics  
Tendencies

# CMIP5 momentum budget as a function of season

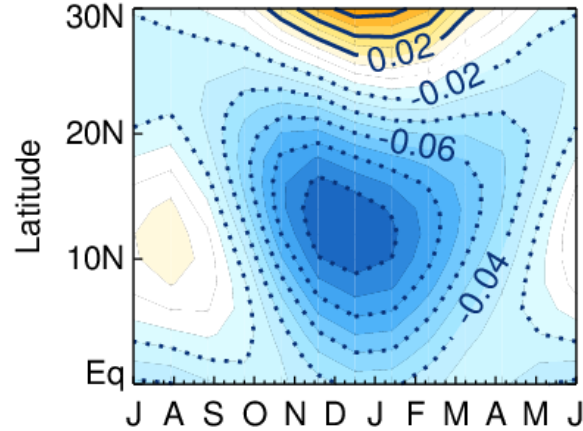


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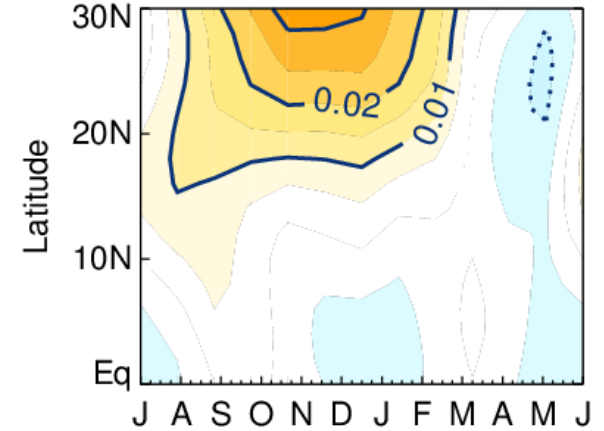
TAUX, CMIP5



RESOLVED, CMIP5

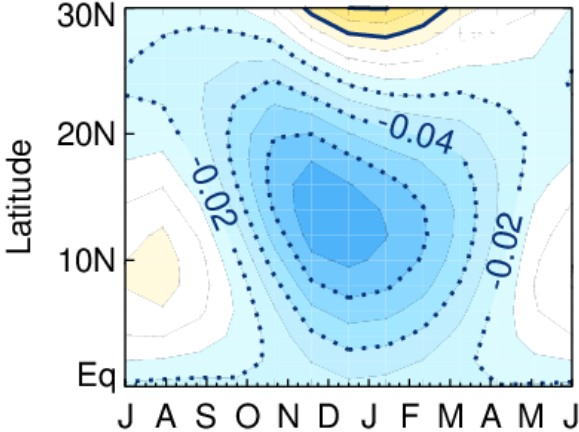


RESIDUAL, CMIP5



## ERA-Interim Budget

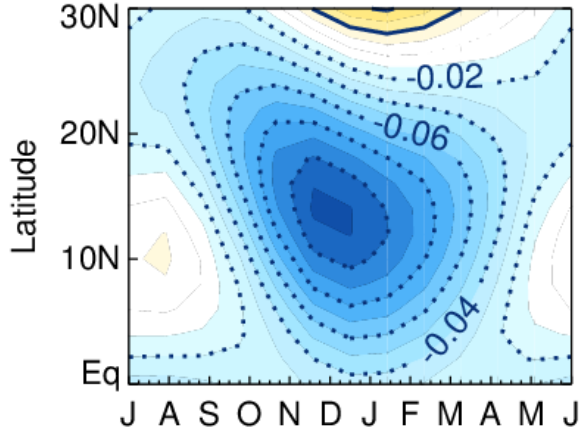
TAUX, ERA



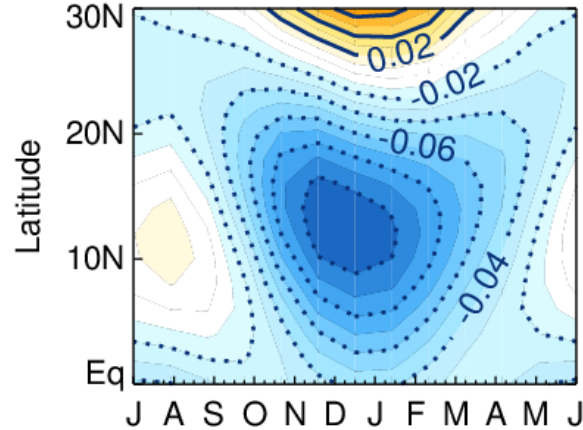


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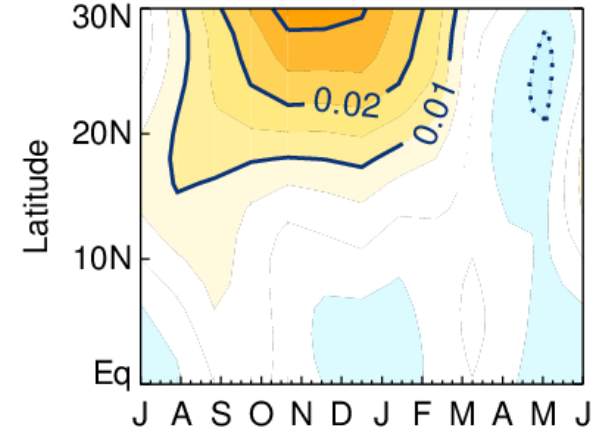
TAUX, CMIP5



RESOLVED, CMIP5

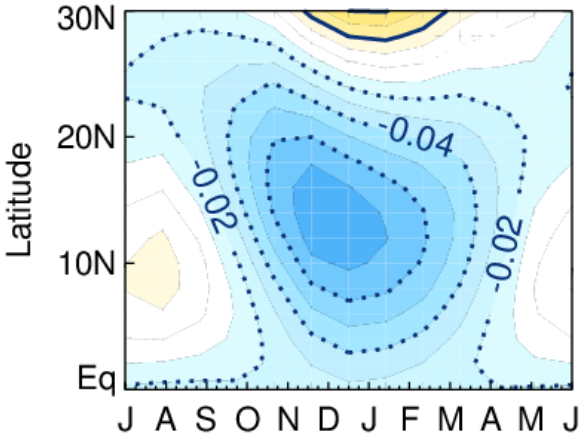


RESIDUAL, CMIP5



## ERA-Interim Budget

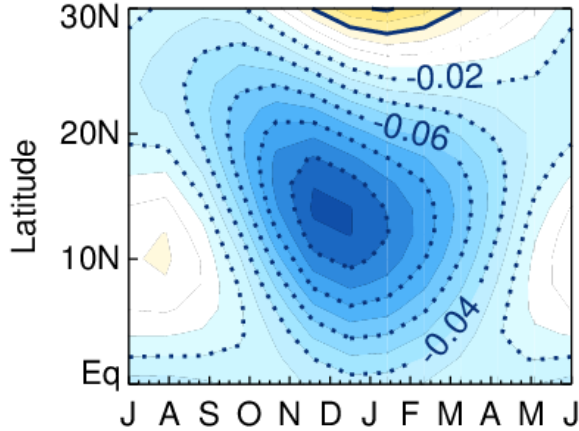
TAUX, ERA



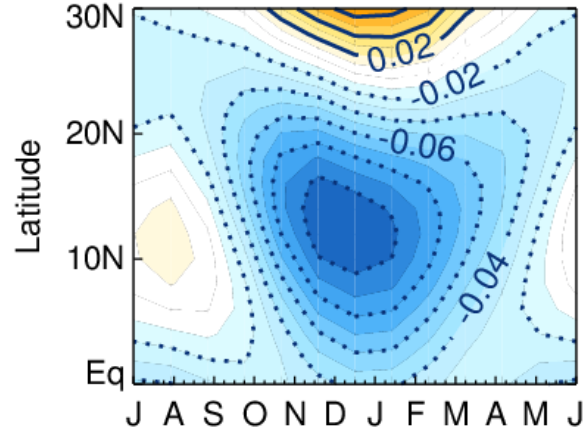
Does the surface wind stress differ because the vertically integrated tendency from the large scale circulation differs?

# CMIP5 momentum budget as a function of season

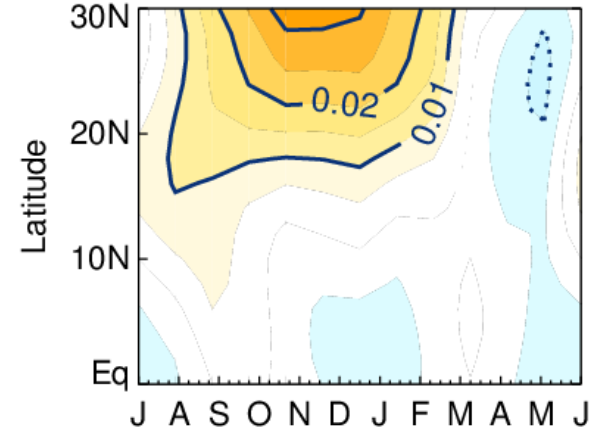
TAUX, CMIP5



RESOLVED, CMIP5

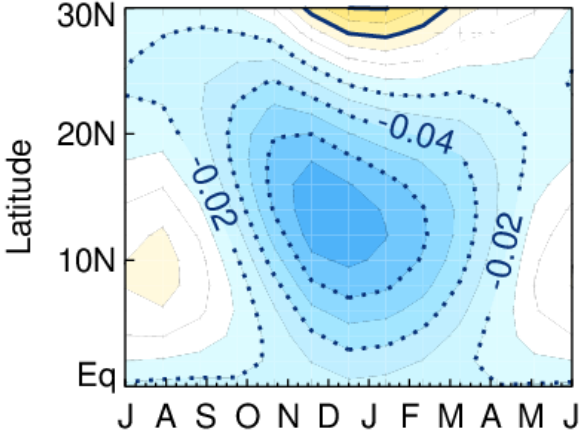


RESIDUAL, CMIP5

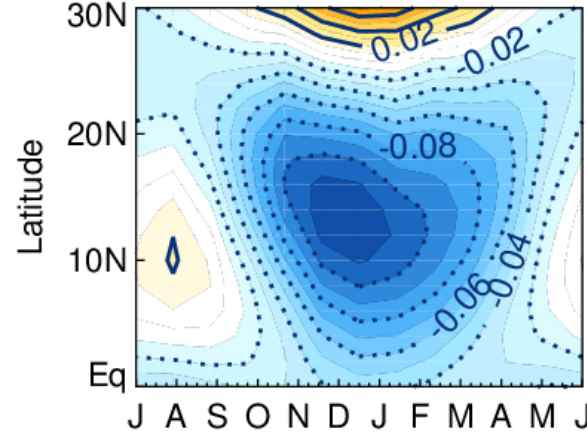


## ERA-Interim Budget

TAUX, ERA

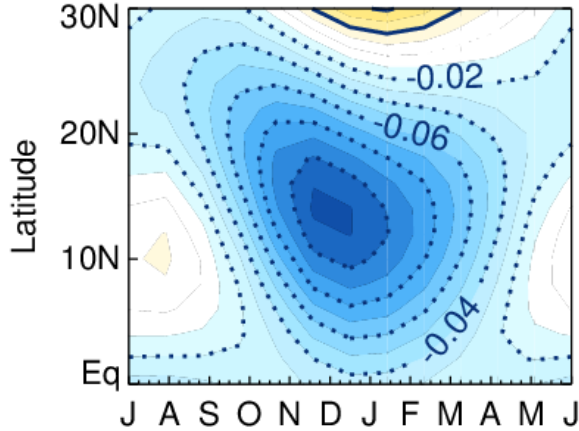


RESOLVED, ERA

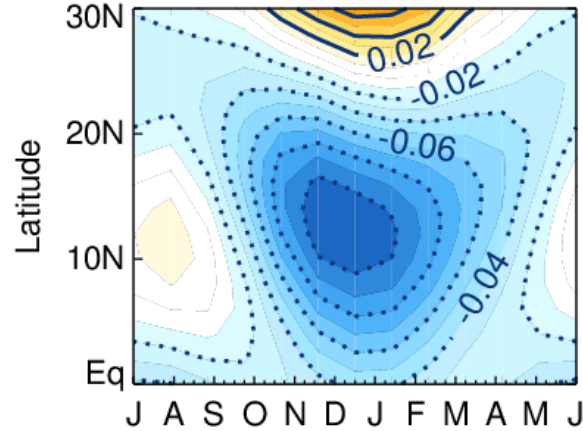


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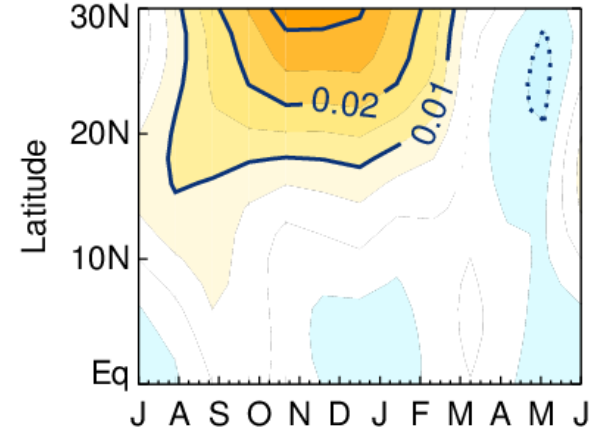
TAUX, CMIP5



RESOLVED, CMIP5

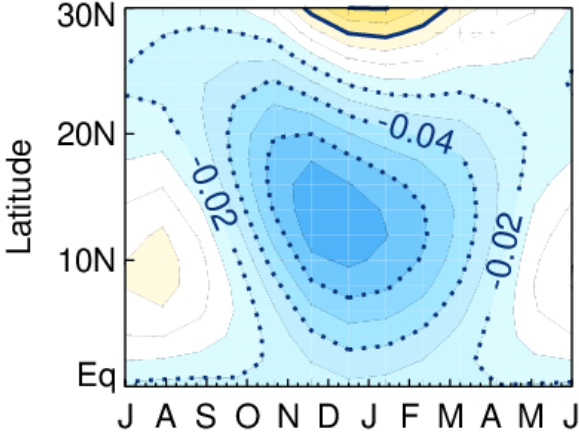


RESIDUAL, CMIP5

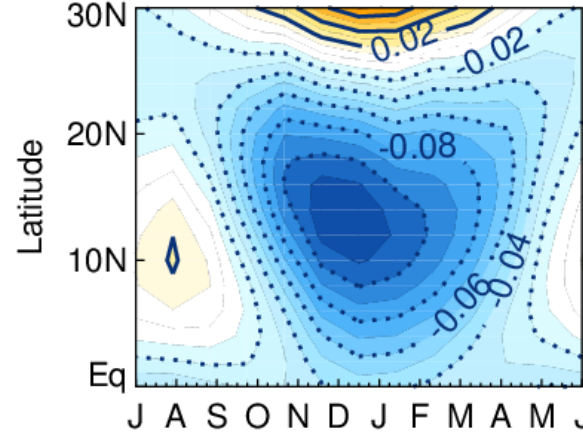


## ERA-Interim Budget

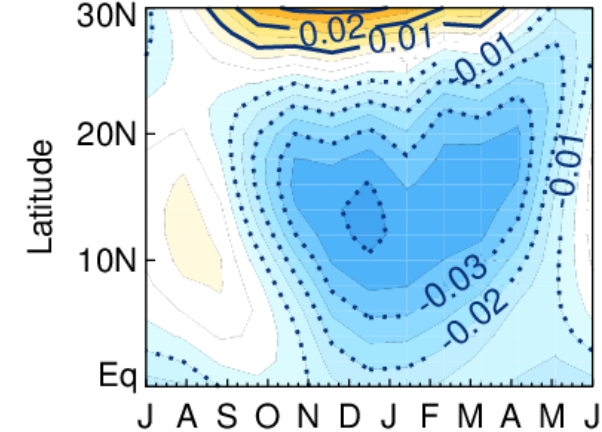
TAUX, ERA



RESOLVED, ERA



RESIDUAL, ERA



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Resolved Dynamics

=

Surface wind stress

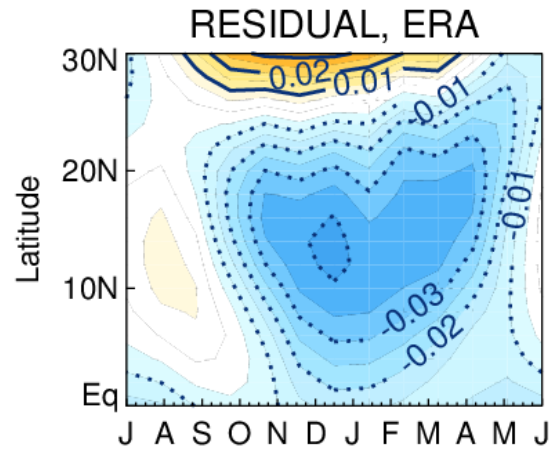
We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Resolved Dynamics

=

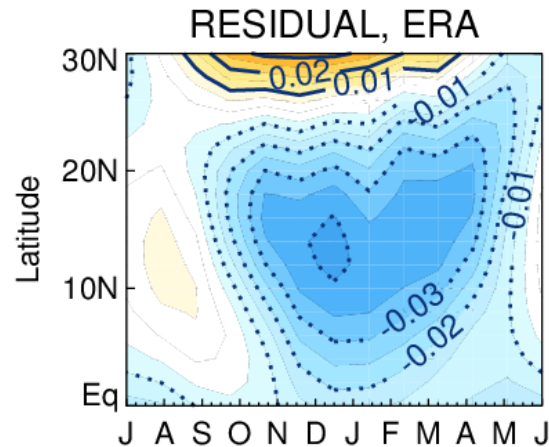
Surface wind stress

Why the residual in ERA-Interim?



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Why the residual in ERA-Interim?



Resolved Dynamics

+

Other  
parameterized  
tendencies

+

$-dU/dt$

=

Surface wind stress

We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

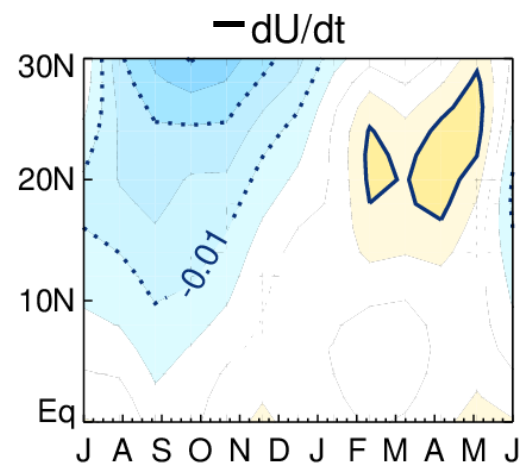
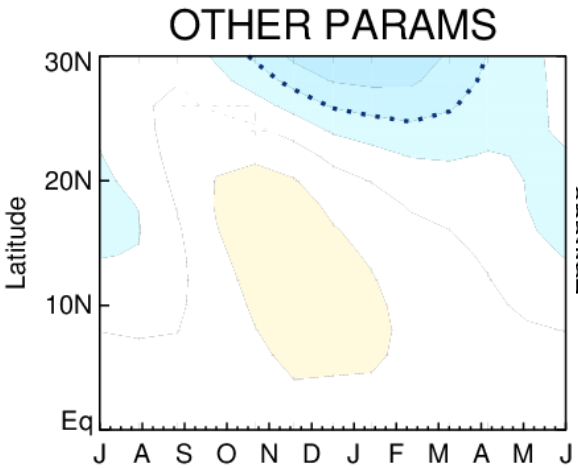
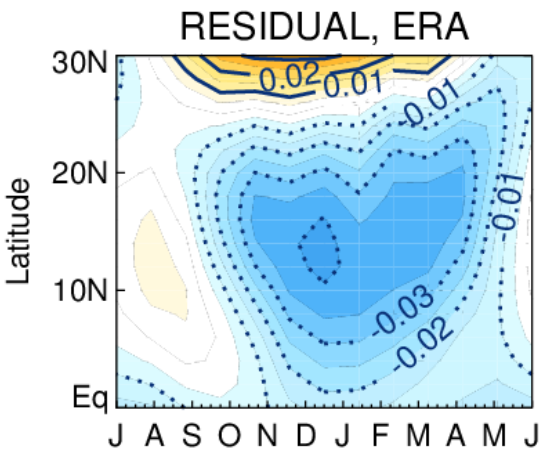
Resolved Dynamics

+  
Other parameterized tendencies

+  
 $-dU/dt$

=  
Surface wind stress

Why the residual in ERA-Interim?



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Why the residual in ERA-Interim?

Resolved Dynamics

+

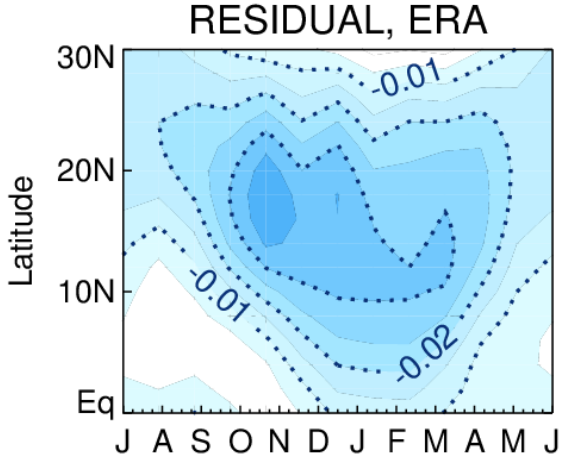
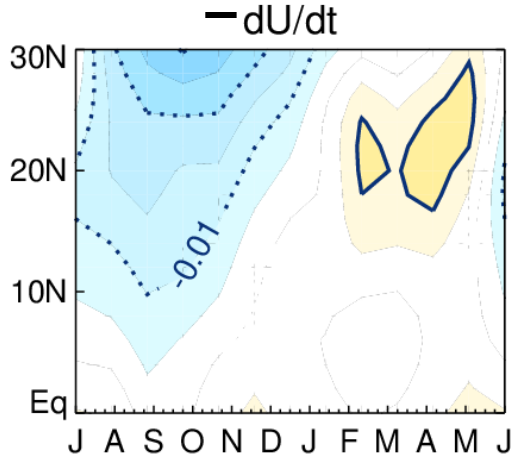
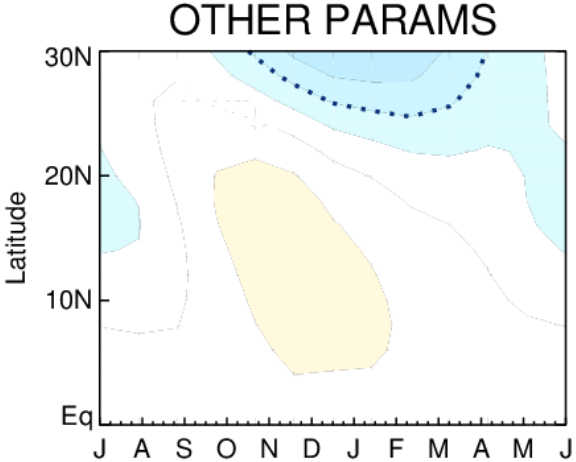
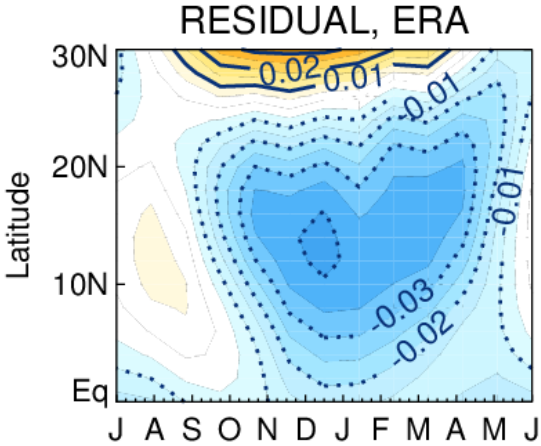
Other parameterized tendencies

+

$-dU/dt$

=

Surface wind stress





We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Why the residual in ERA-Interim?

Resolved Dynamics

+

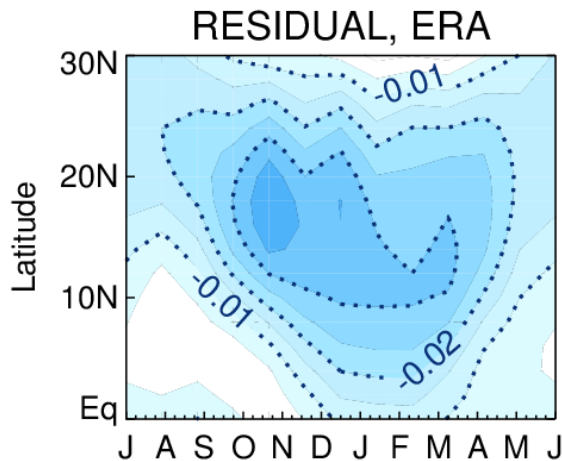
Other parameterized tendencies

+

$-dU/dt$

=

Surface wind stress



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Resolved Dynamics

+

Other parameterized tendencies

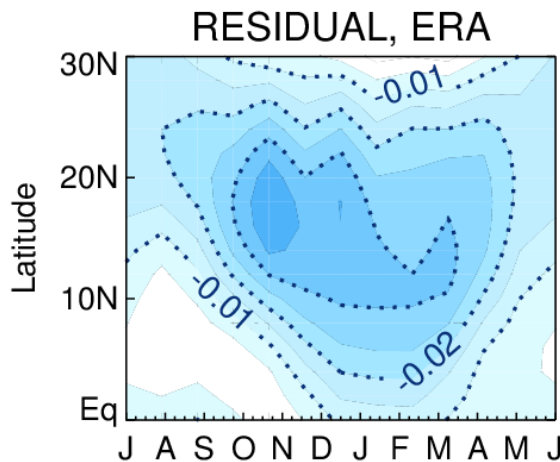
+

$-dU/dt$

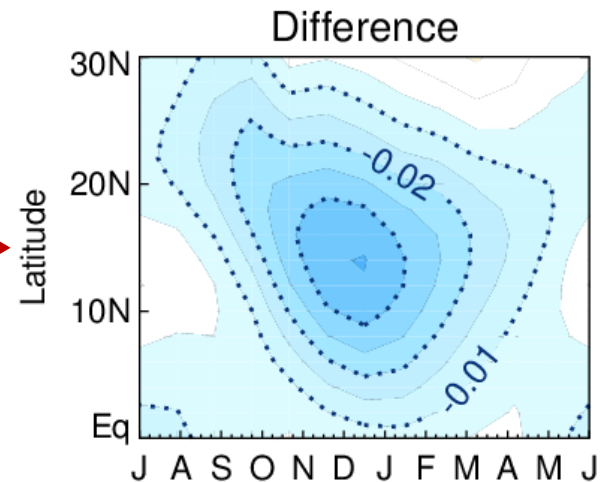
=

Surface wind stress

Why the residual in ERA-Interim?



CMIP5 - ERA Interim difference in surface wind stress.



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Resolved Dynamics

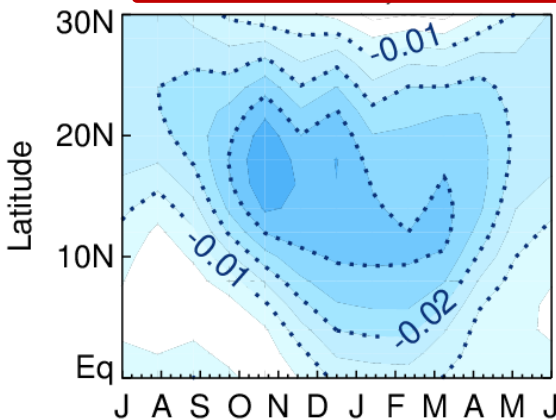
+

Other parameterized tendencies

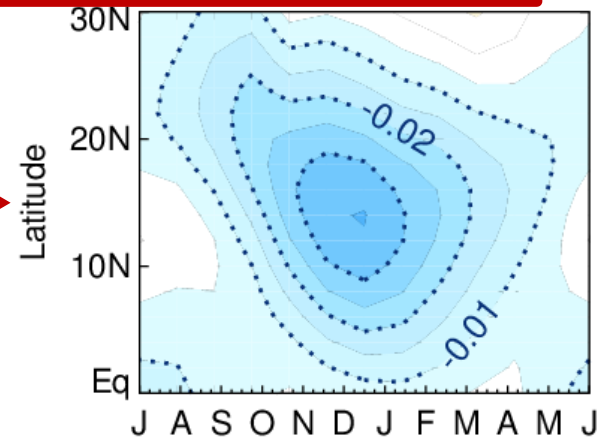
+

Why the residual in ERA-Interim?

We can't explain the difference in surface wind stress between the CMIP5 models and the reanalysis with any of the terms in the vertically integrated budget. The budget doesn't add up in ERA-Interim



CMIP5 - ERA Interim difference in surface wind stress.



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Why the residual in ERA-Interim?

Resolved Dynamics

+

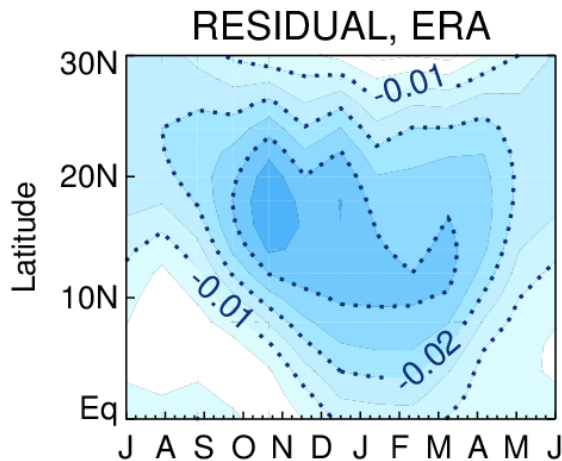
Other parameterized tendencies

+

$-dU/dt$

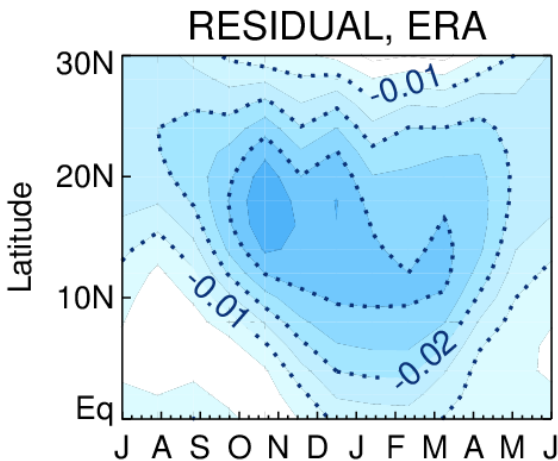
=

Surface wind stress



We can't attribute the difference in surface wind stress to a difference in the resolved dynamics terms

Why the residual in ERA-Interim?



Resolved Dynamics

+

Other  
parameterized  
tendencies

+

$-dU/dt$

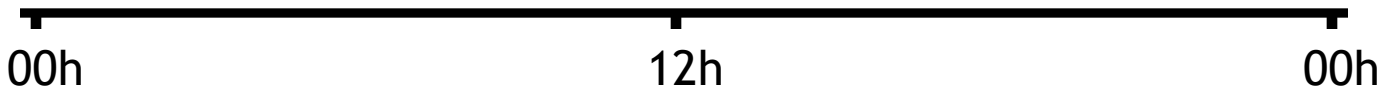
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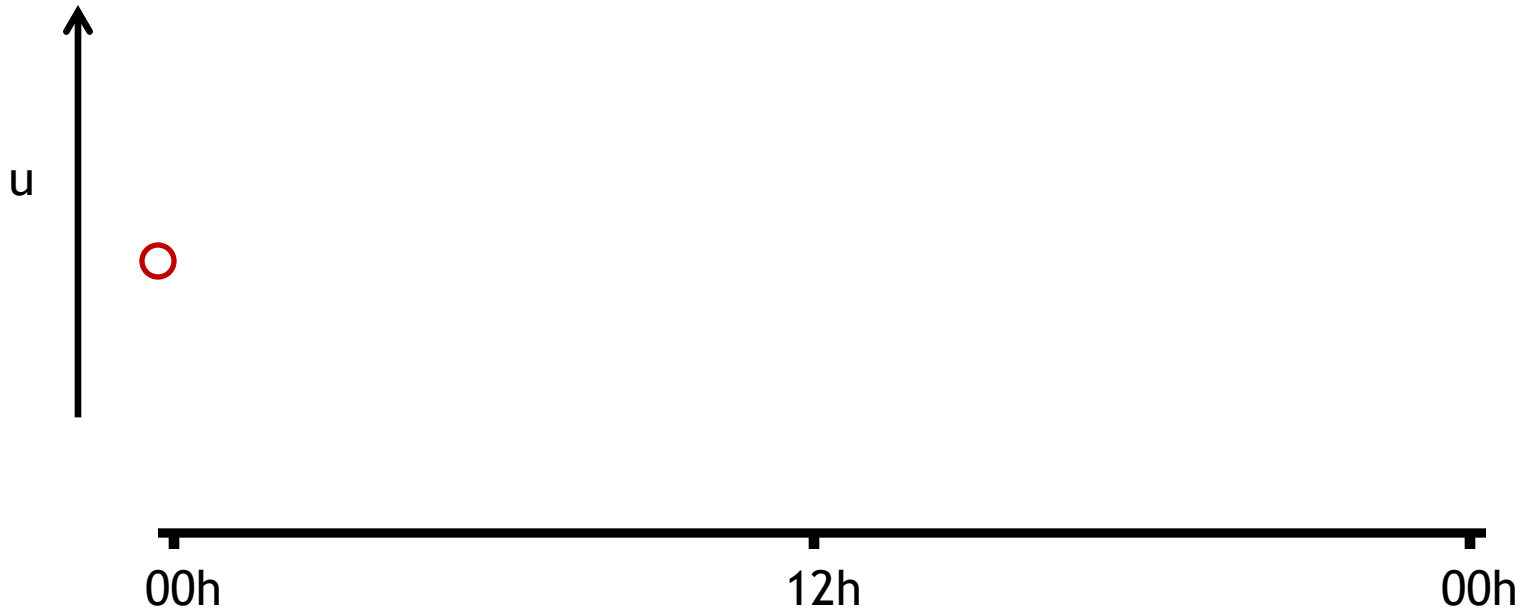
Analysis  
Increments

=

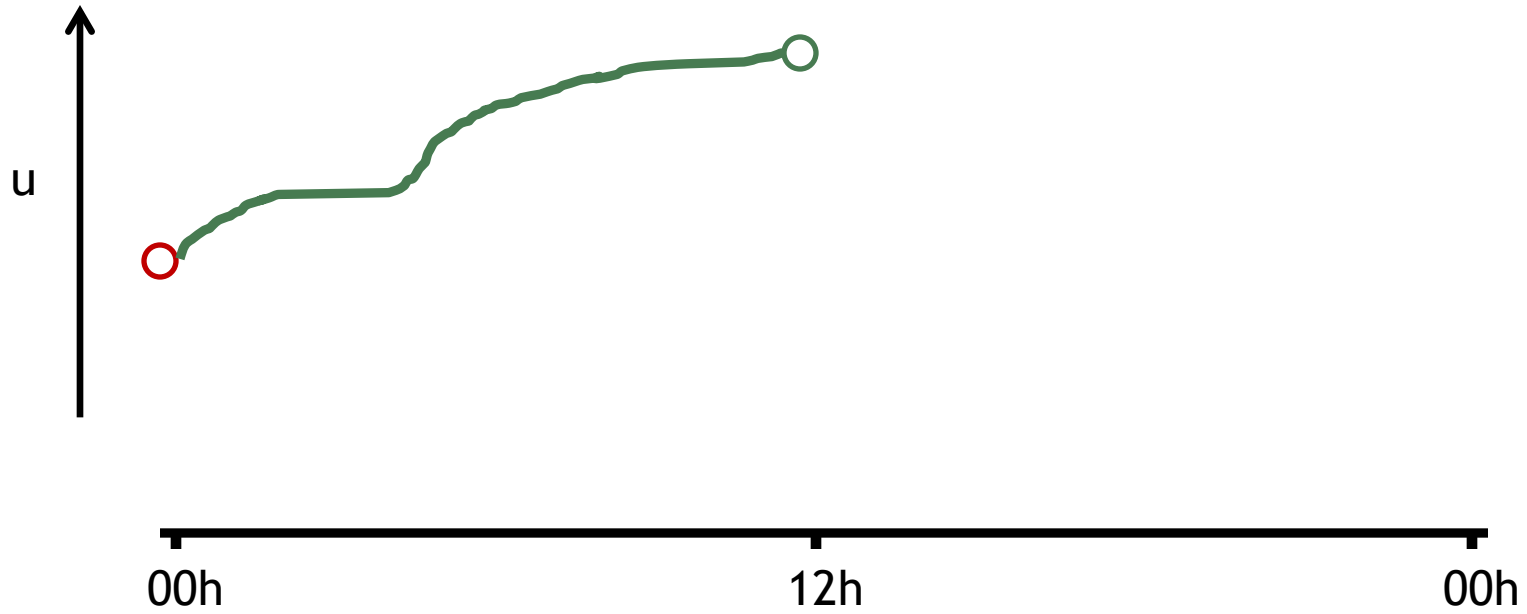
Surface wind stress

u ↑





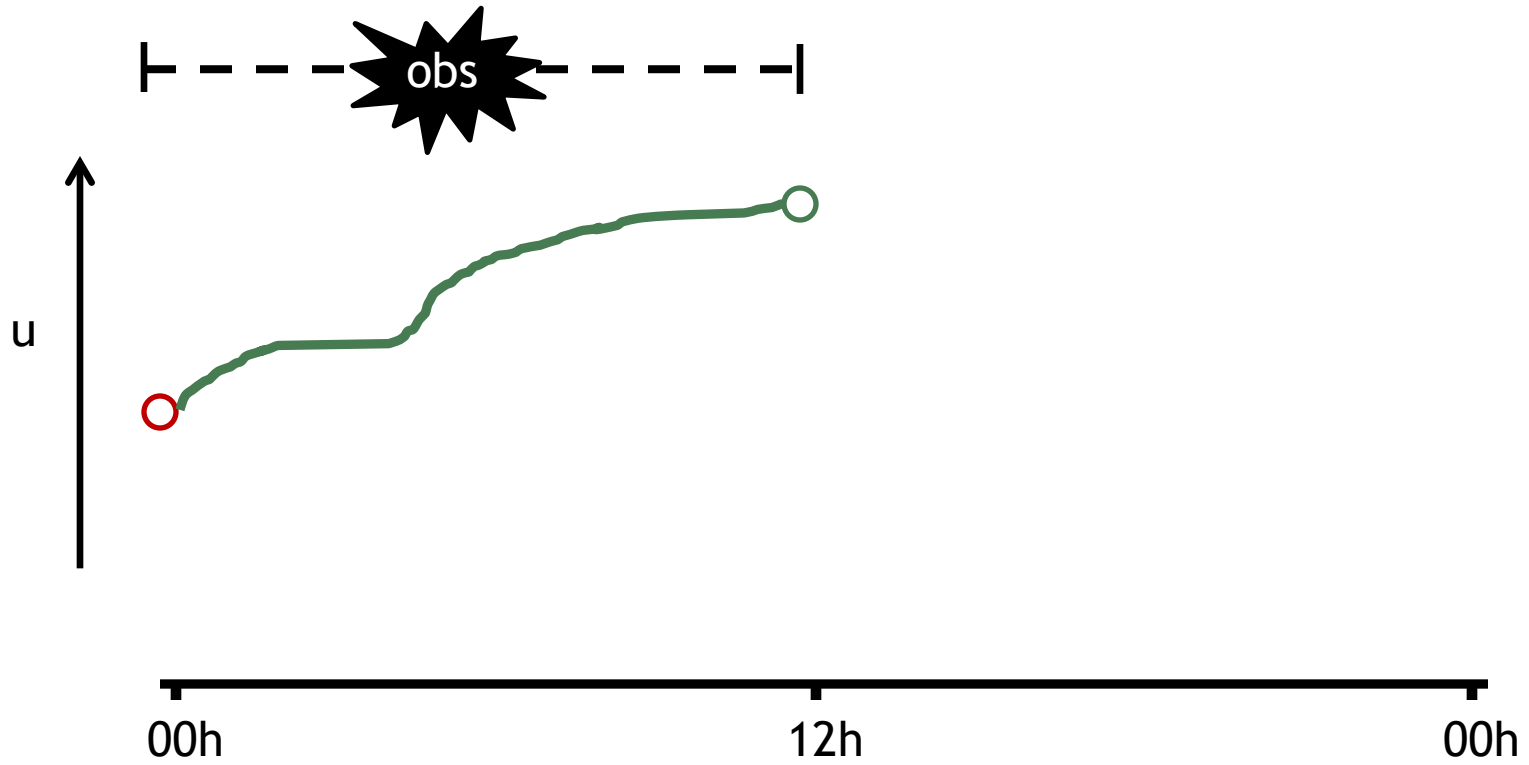
○ Analyzed State



○ Analyzed State

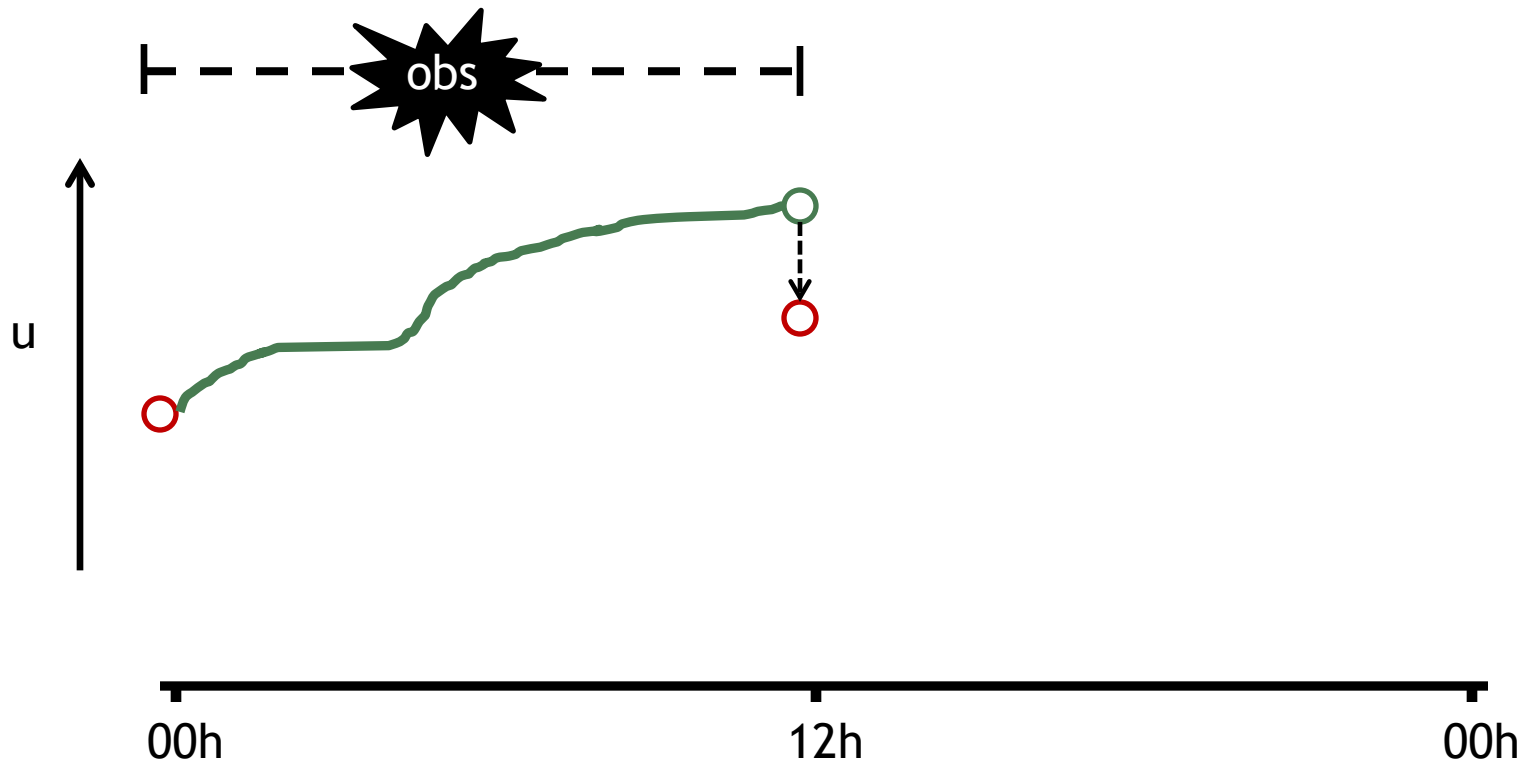
○ Forecast





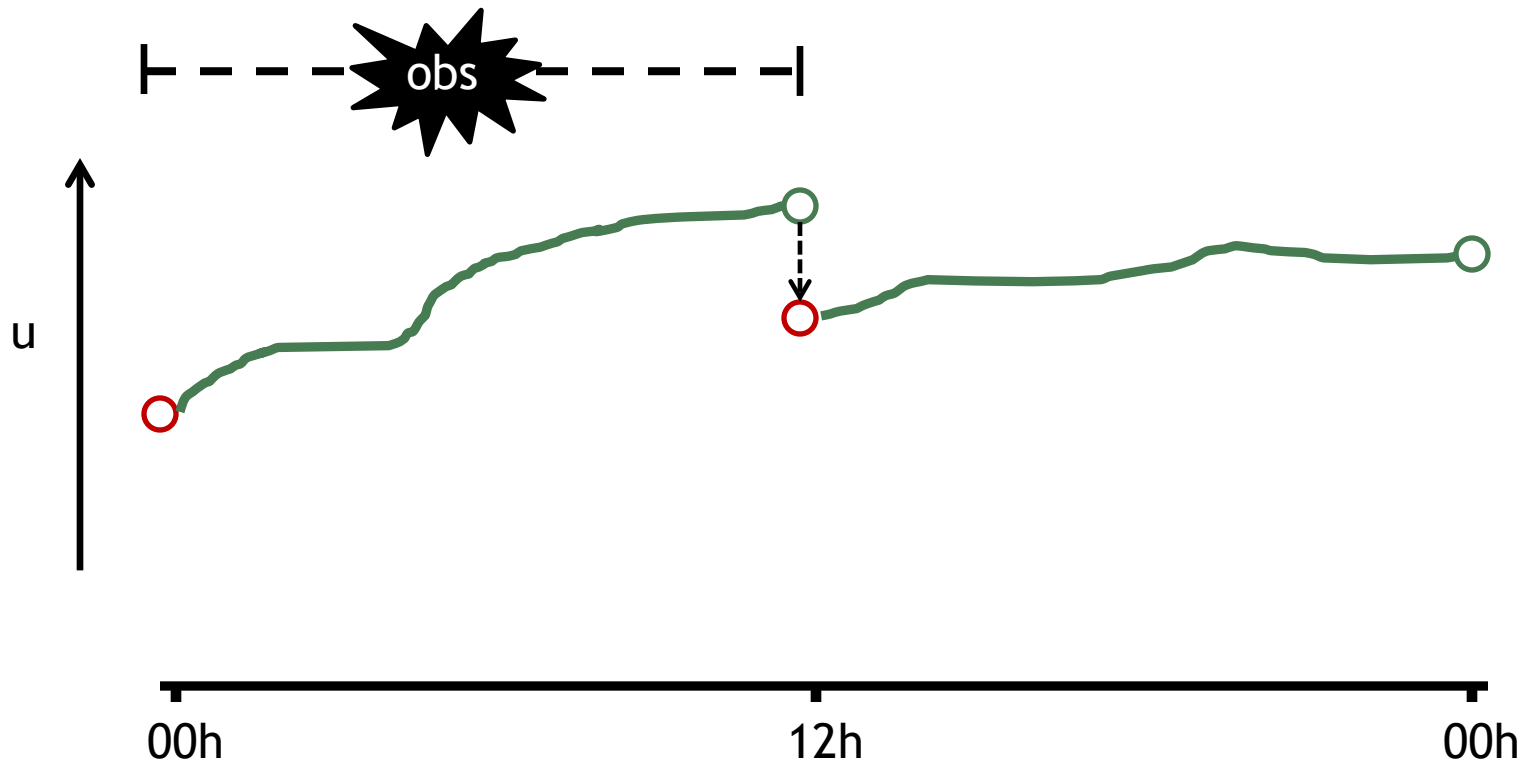
○ Analyzed State

○ Forecast



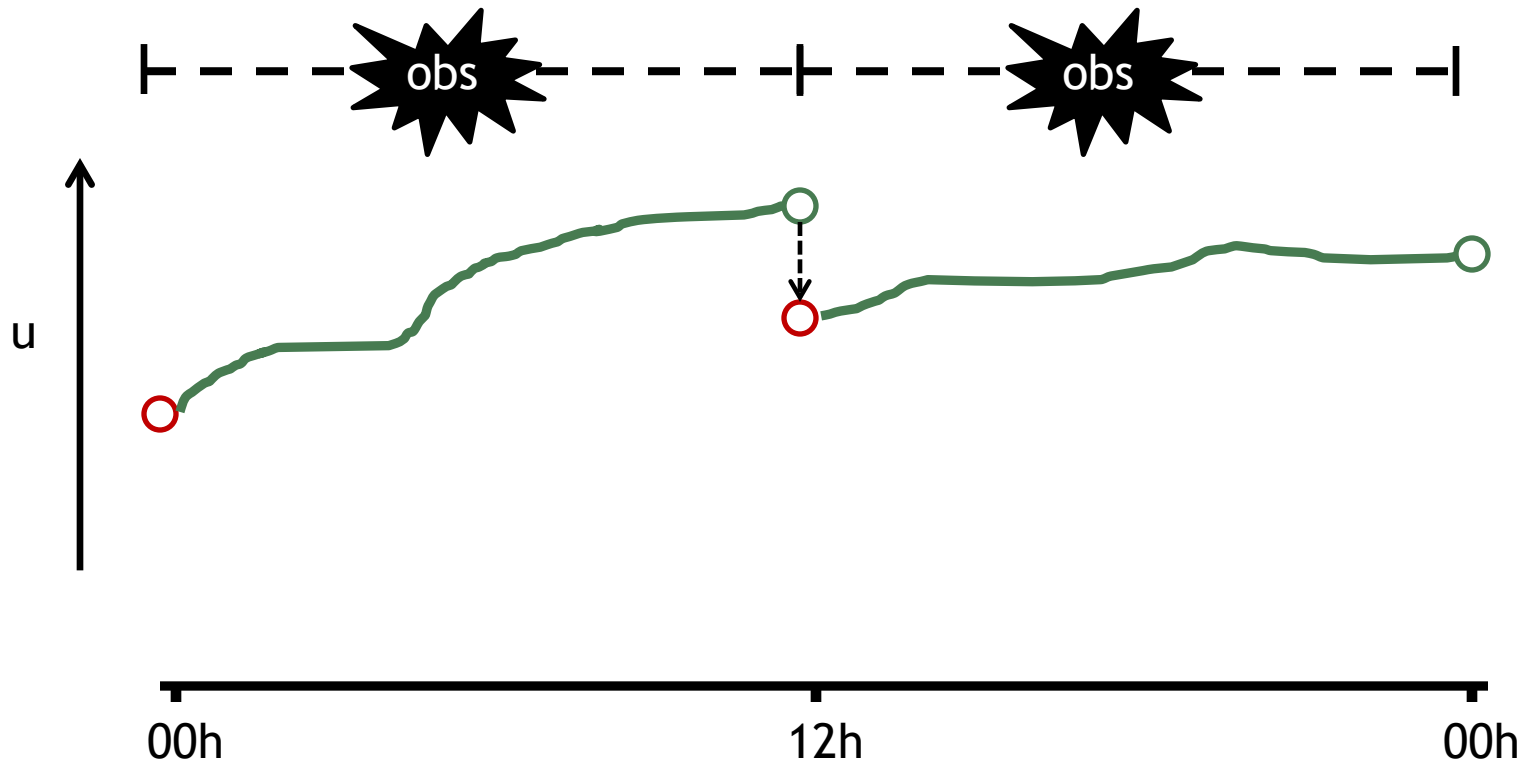
○ Analyzed State

○ Forecast



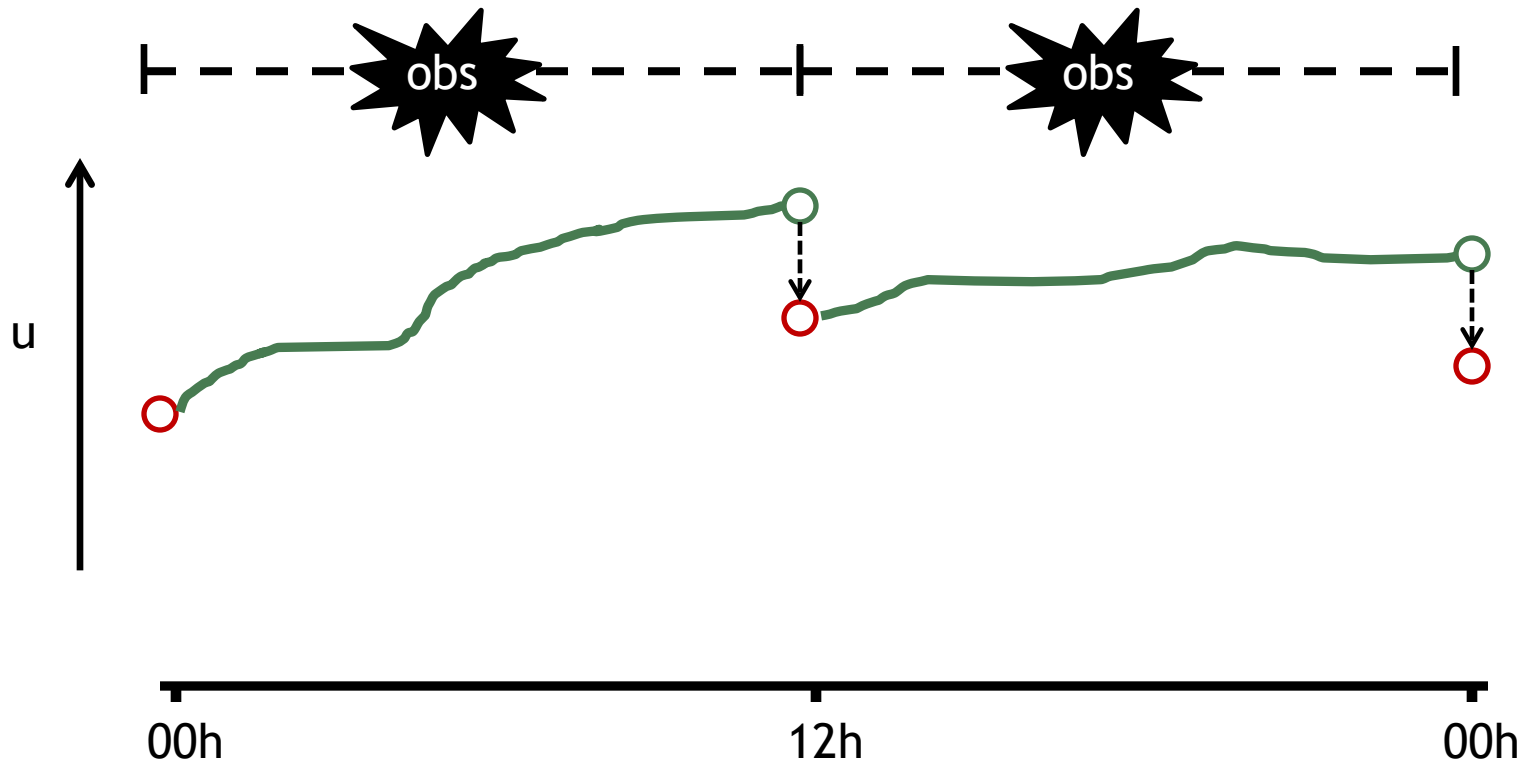
○ Analyzed State

○ Forecast



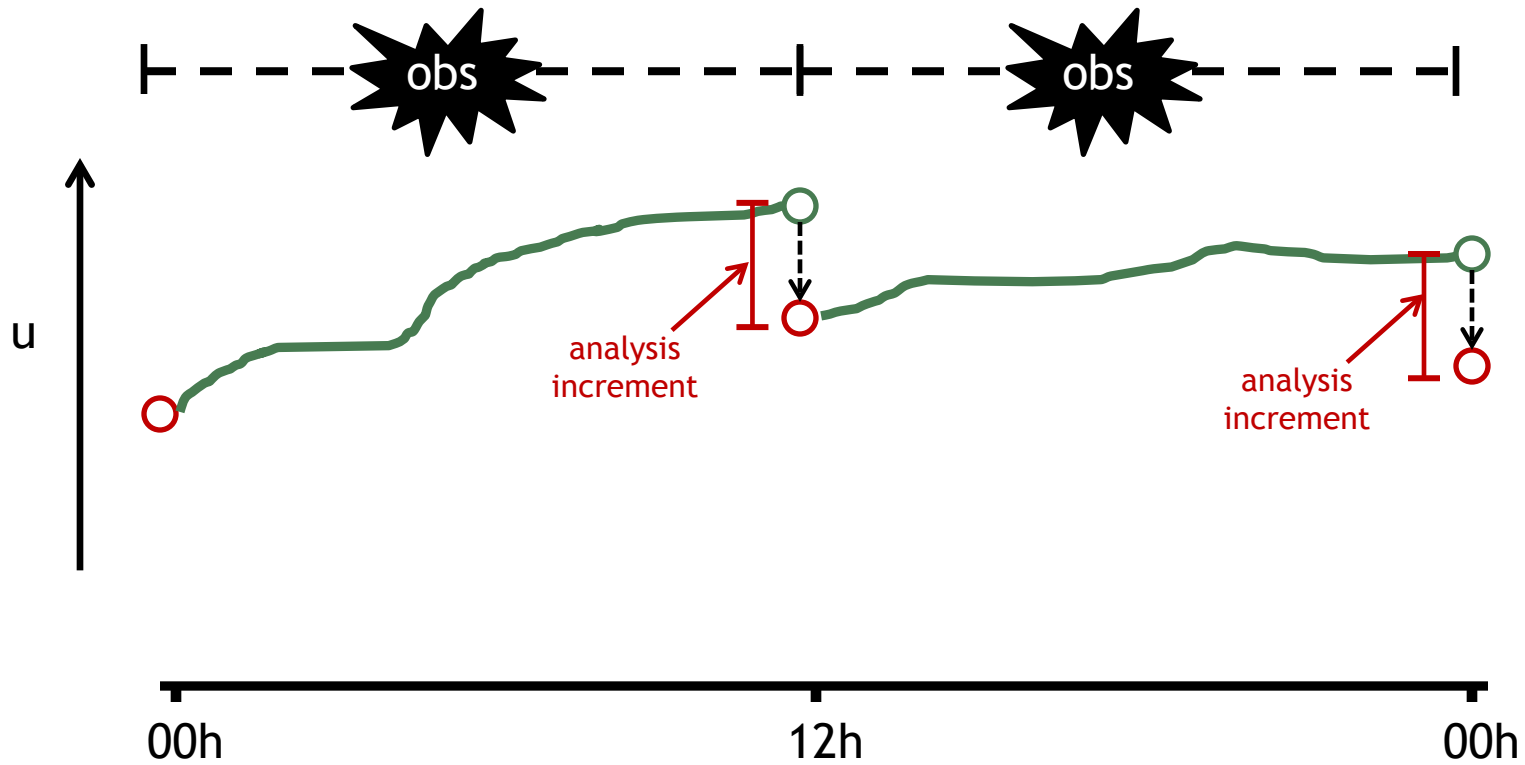
○ Analyzed State

○ Forecast



○ Analyzed State

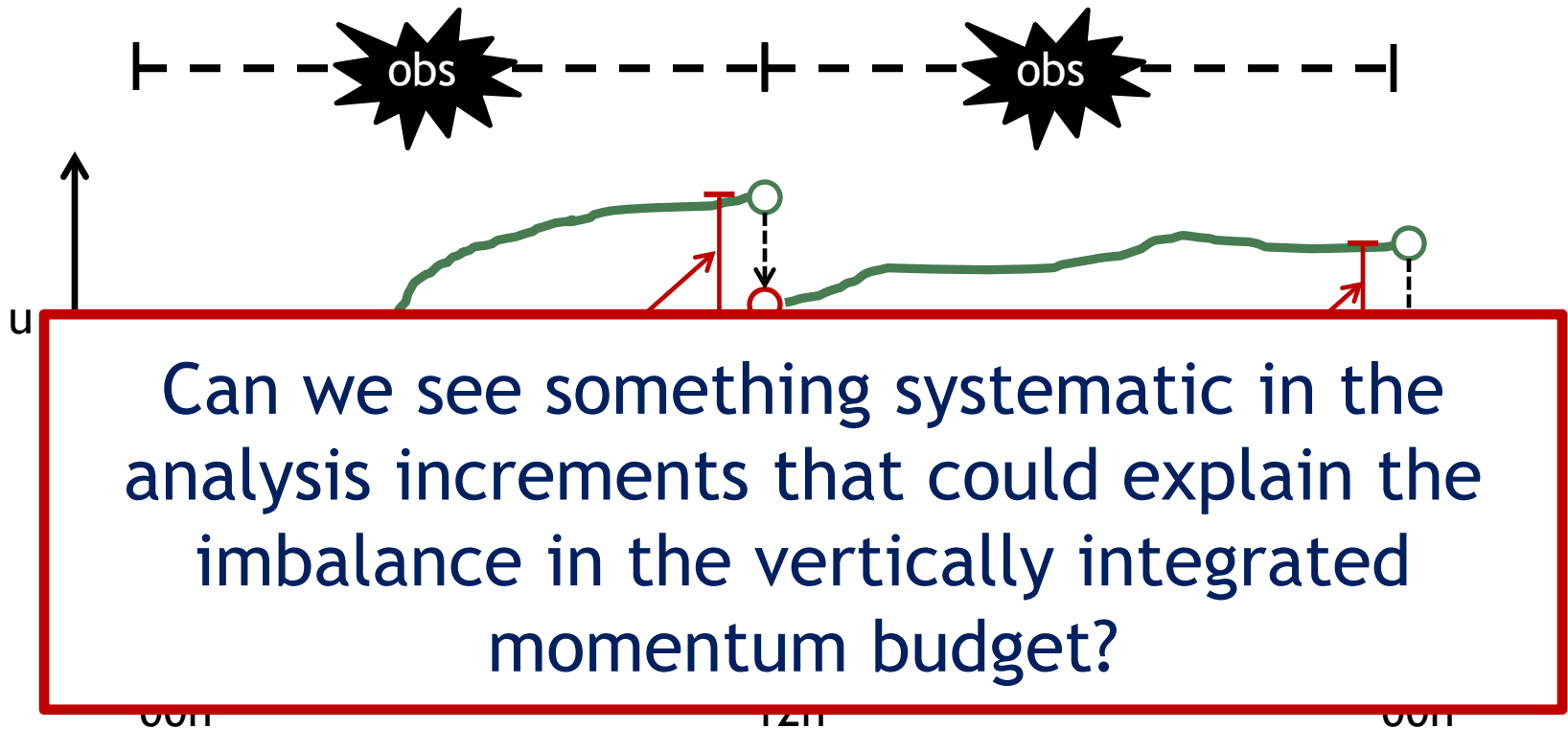
○ Forecast



○ Analyzed State

○ Forecast

$$\text{Analysis Increment} = \text{Analyzed State} - \text{Forecast}$$

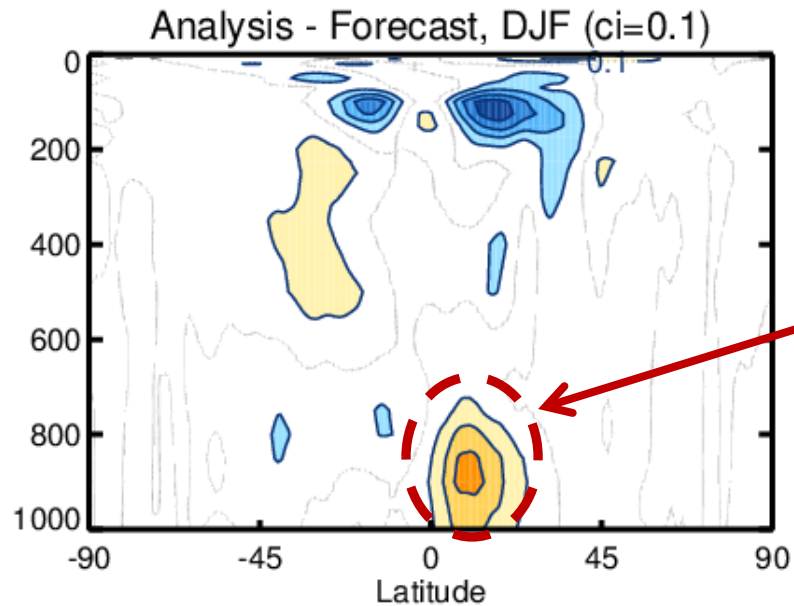
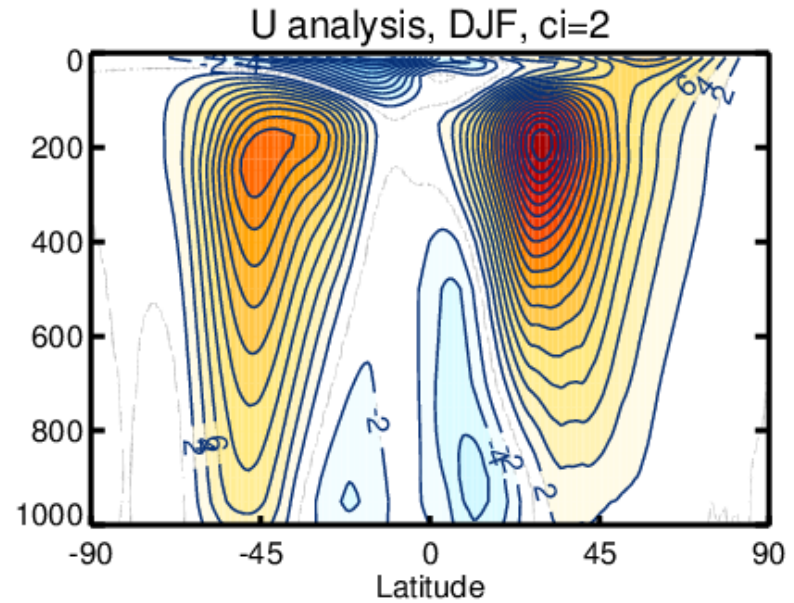
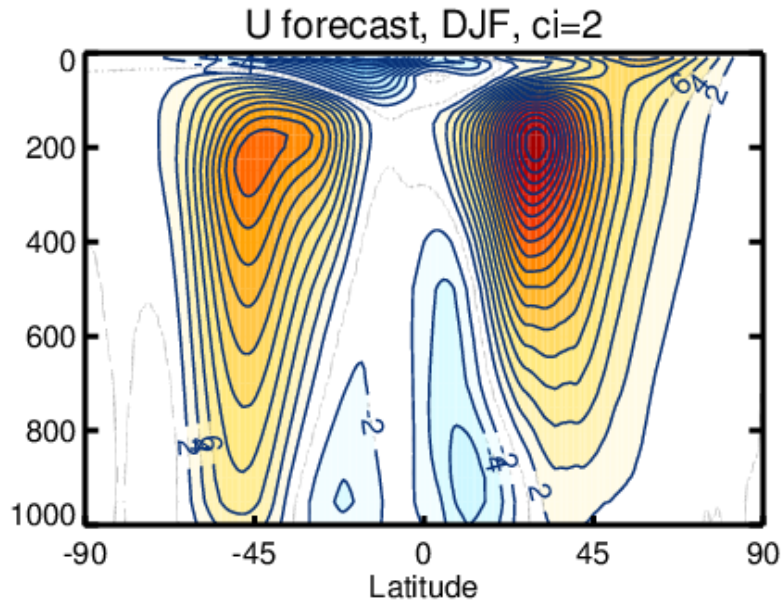


○ Analyzed State

○ Forecast

$$\text{Analysis Increment} = \text{Analyzed State} - \text{Forecast}$$

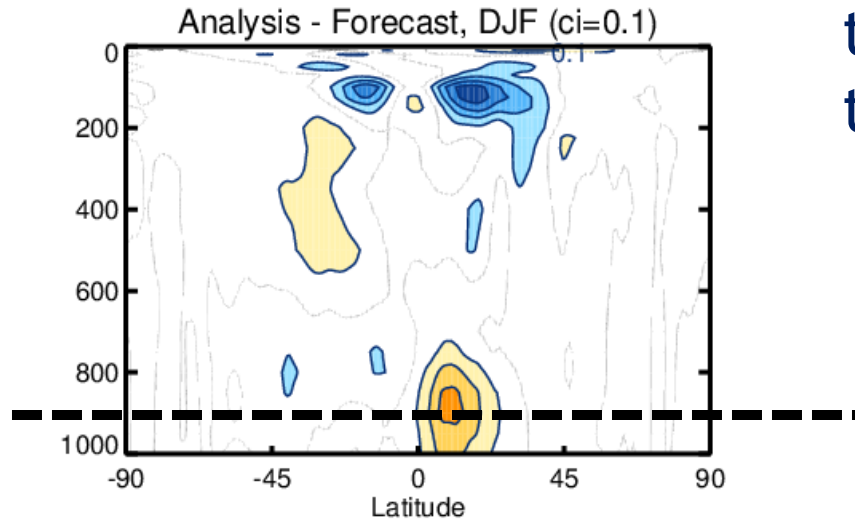
# DJF analysis increments



Assimilation acts to reduce the near surface easterly winds

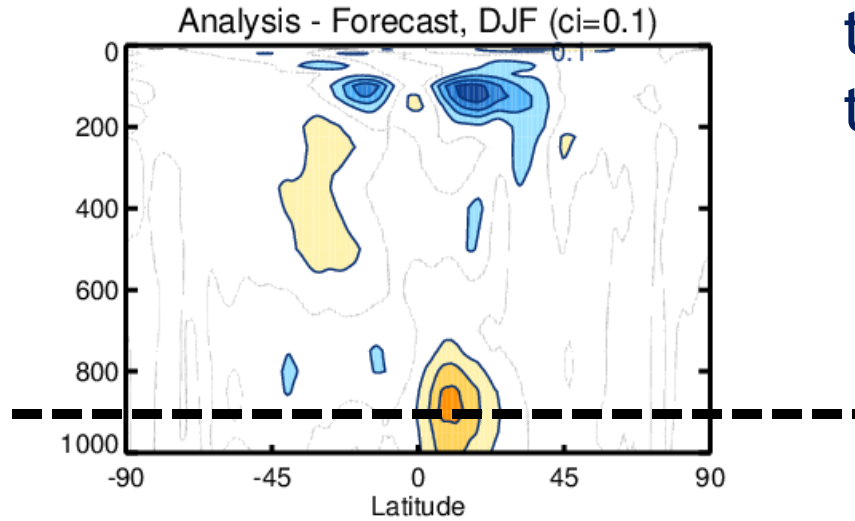


Are these increments present throughout the full 1979-2012 time period?



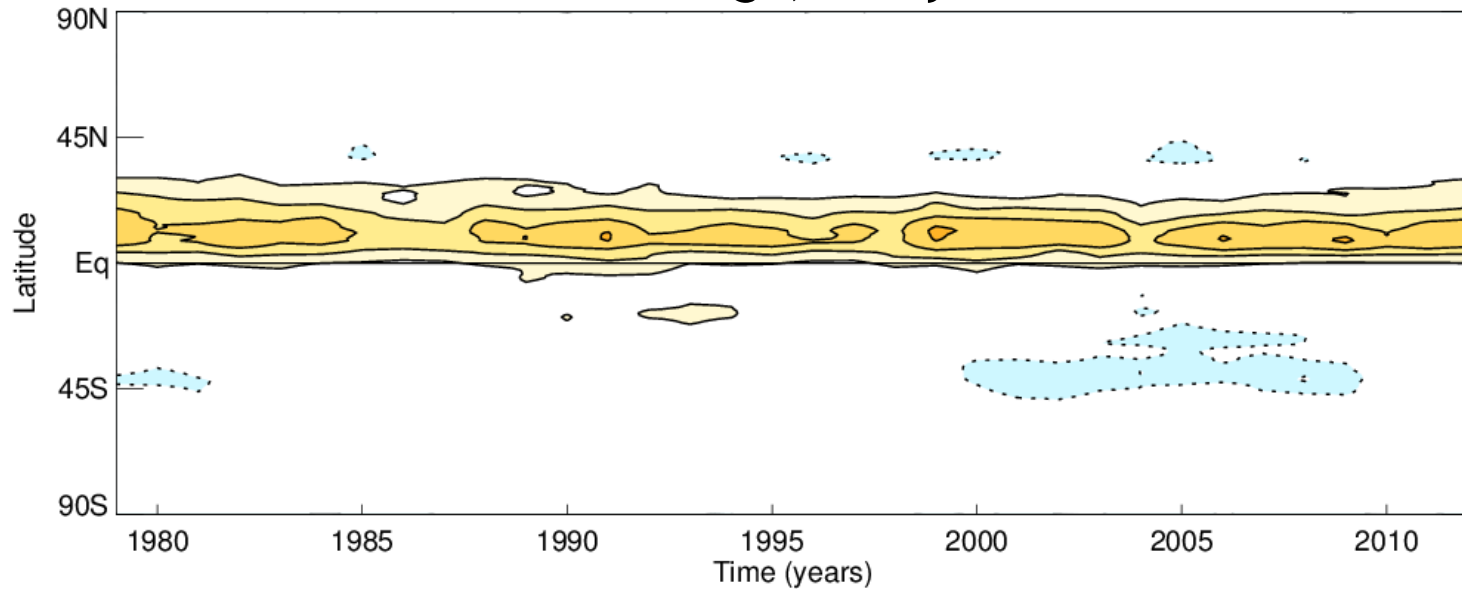
900hPa zonal mean  
zonal wind

Are these increments present throughout the full 1979-2012 time period?



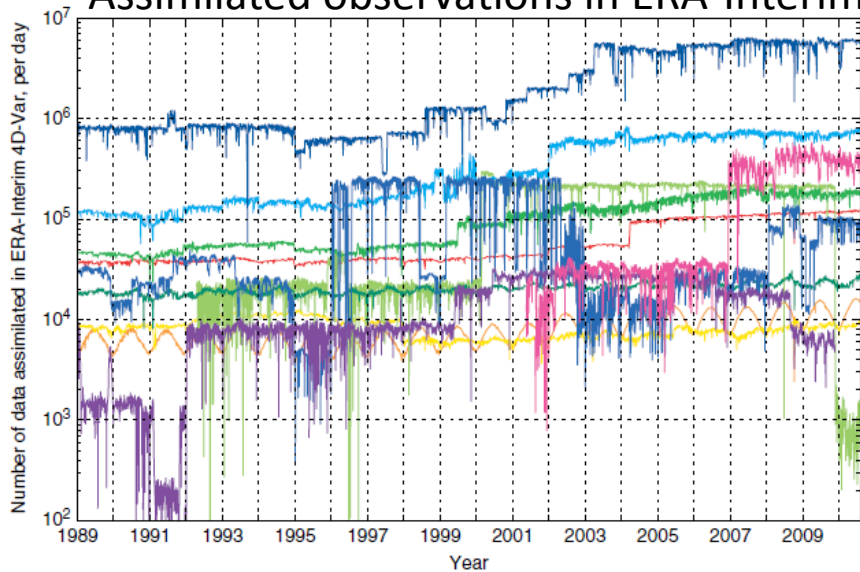
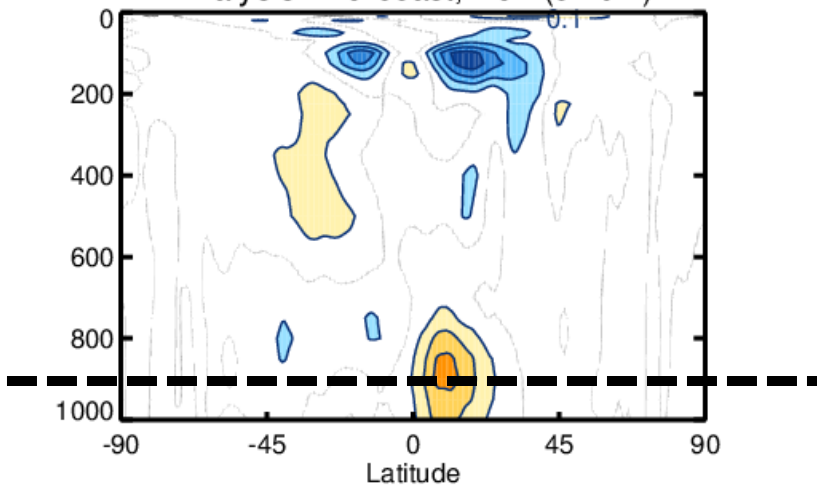
900hPa zonal mean zonal wind

DJF seasonal average, Analysis - Forecast



# Assimilated observations in ERA-Interim

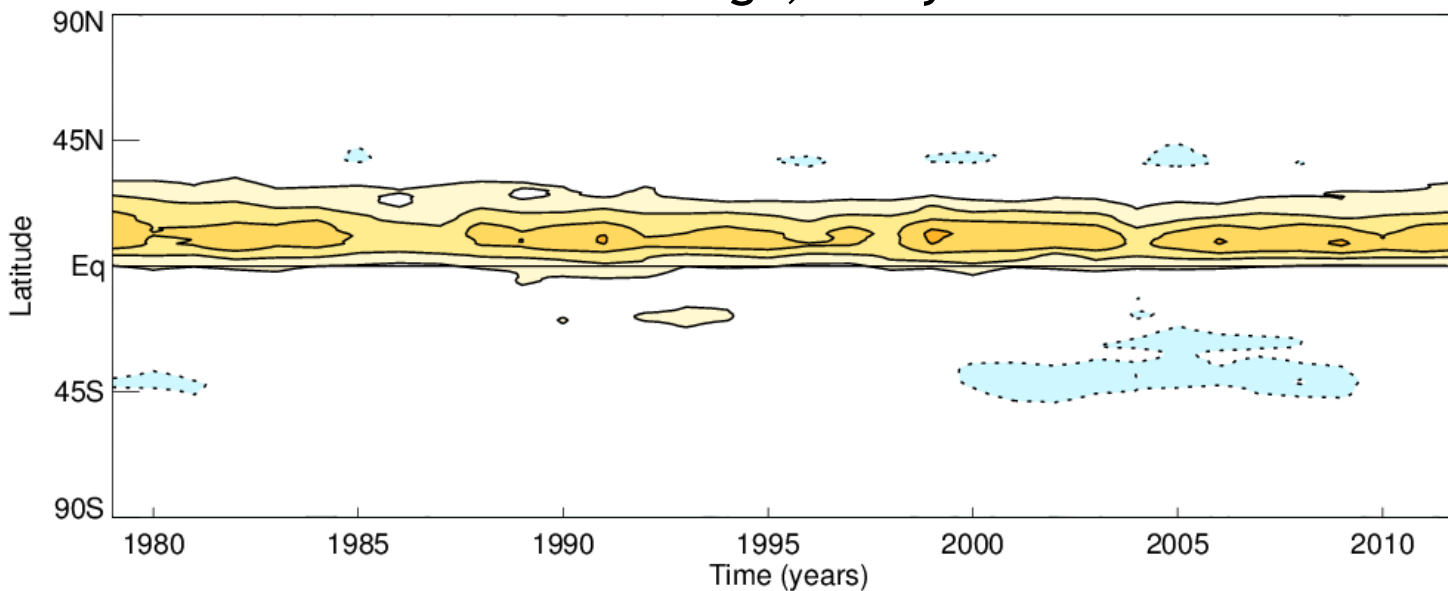
## Analysis - Forecast, DJF (ci=0.1)



- Surface pressure
- 2-m relative humidity
- 10-m wind
- Scatterometer wind
- Upper-air temperature
- Upper-air specific humidity
- Upper-air wind
- Ozone
- Brightness temperature
- Total precipitable water
- Bending angle

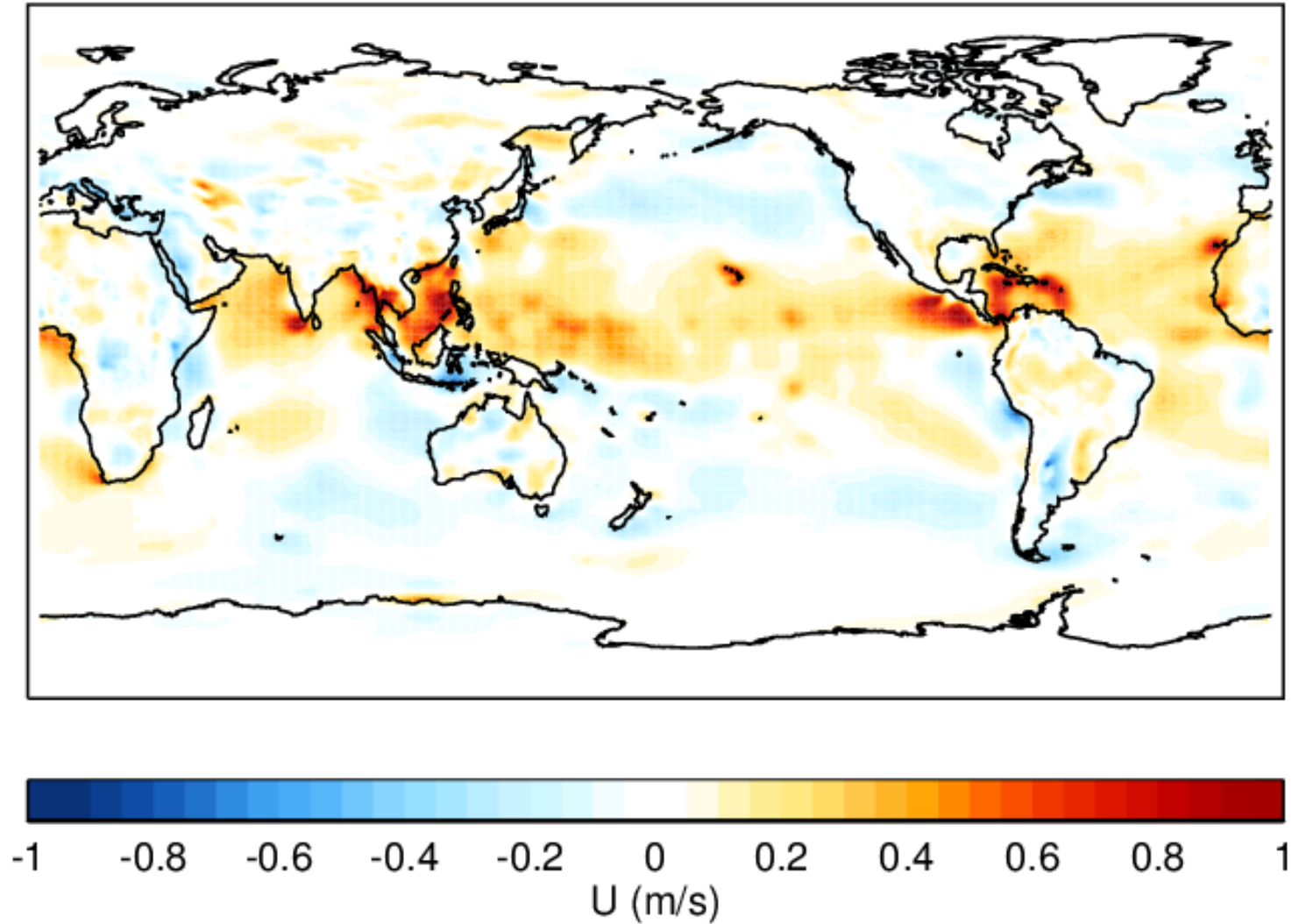
## DJF seasonal average, Analysis - Forecast

Dee et al 2011

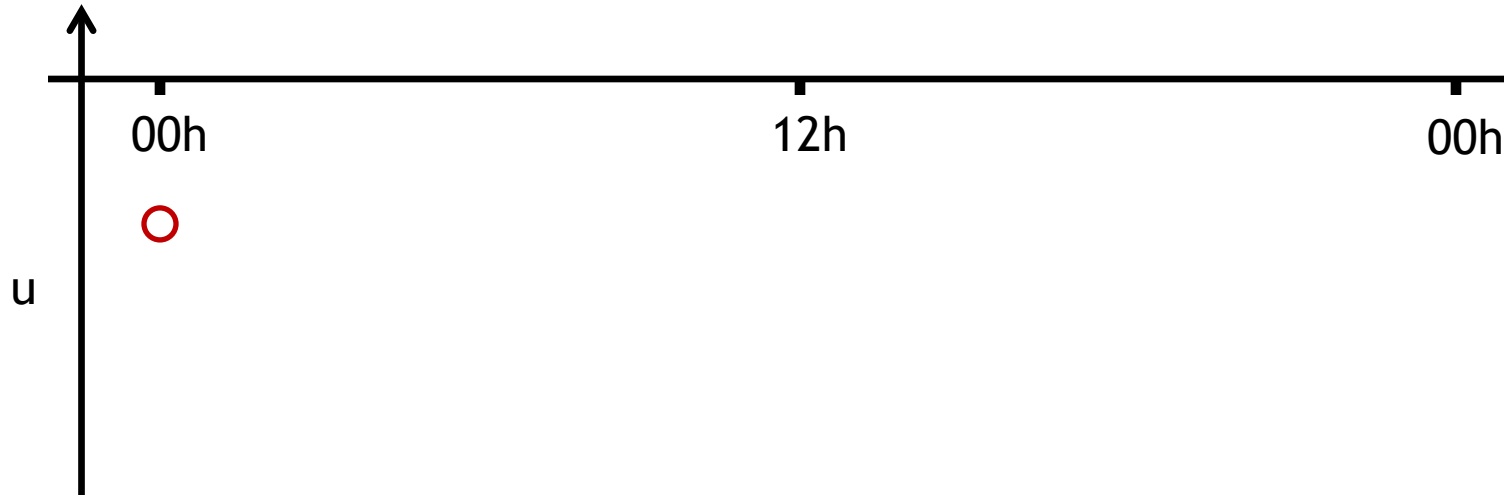


# Lat-lon structure of analysis increments in DJF

950hPa U, DJF, Analysis - Forecast

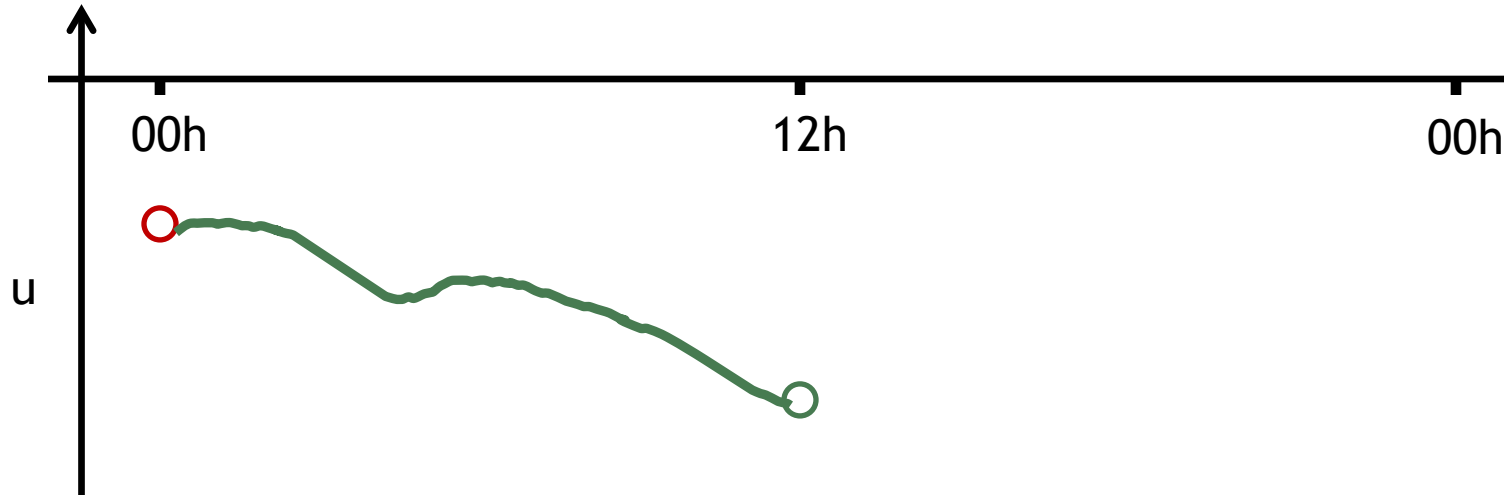


# Lower tropospheric zonal mean zonal wind



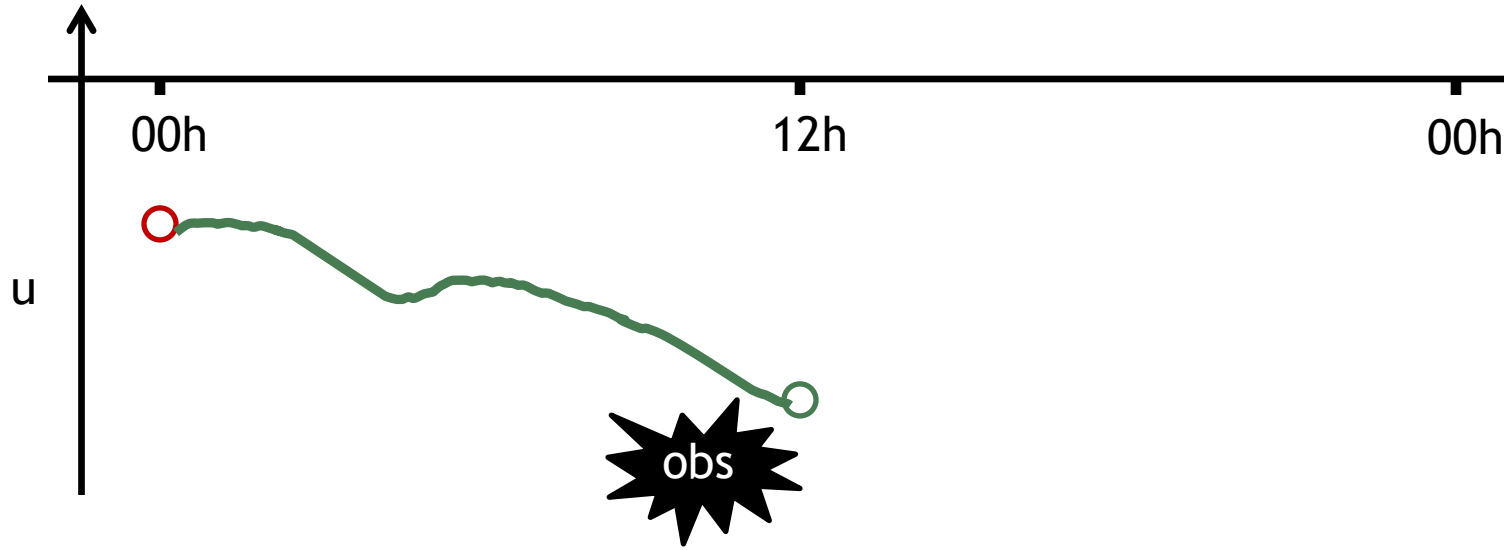
Could this increment explain our budget residual?

# Lower tropospheric zonal mean zonal wind



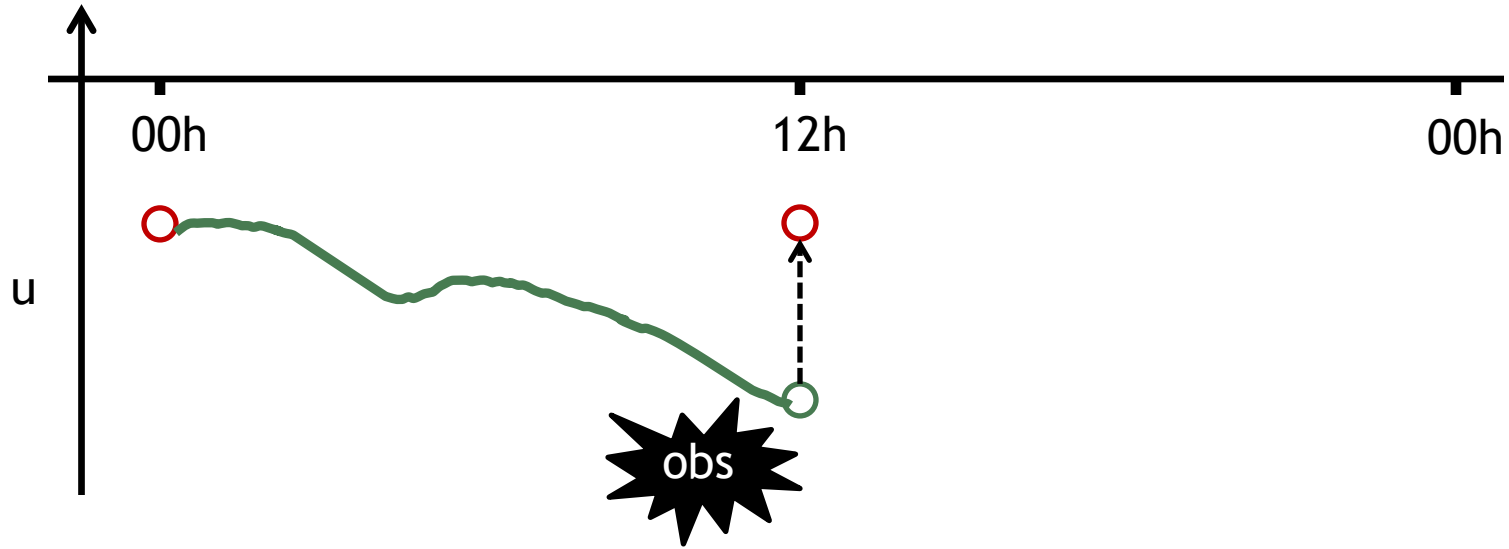
Could this increment explain our budget residual?

# Lower tropospheric zonal mean zonal wind



Could this increment explain our budget residual?

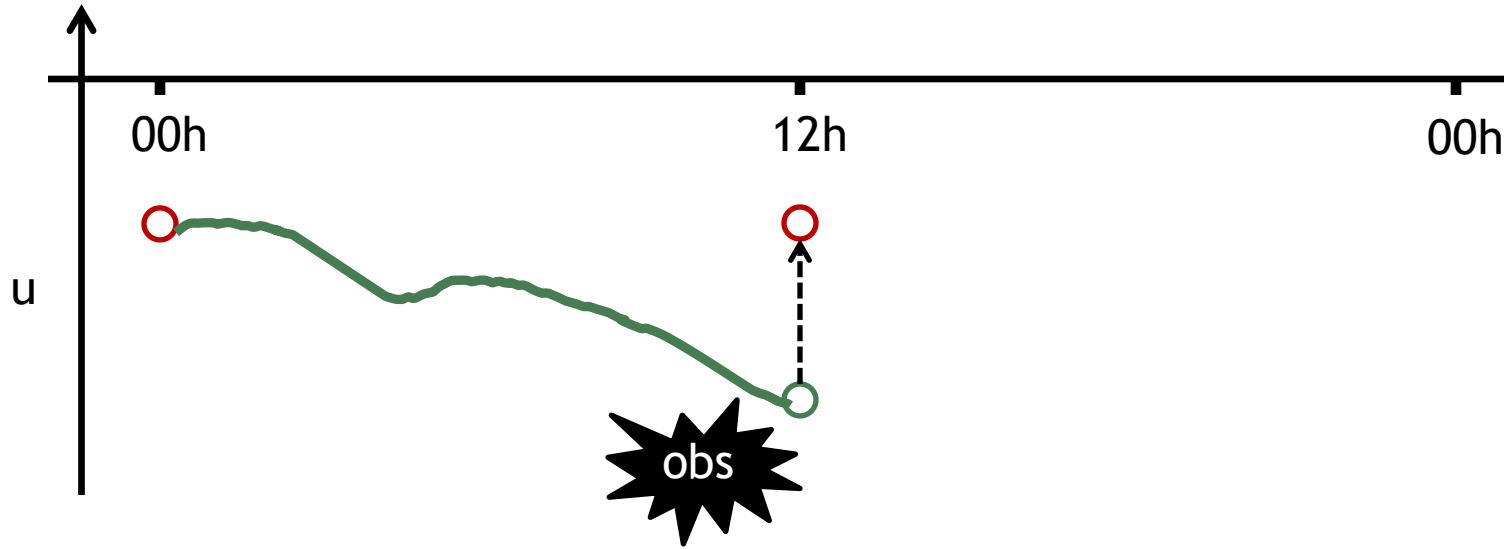
# Lower tropospheric zonal mean zonal wind



Could this increment explain our budget residual?



# Lower tropospheric zonal mean zonal wind



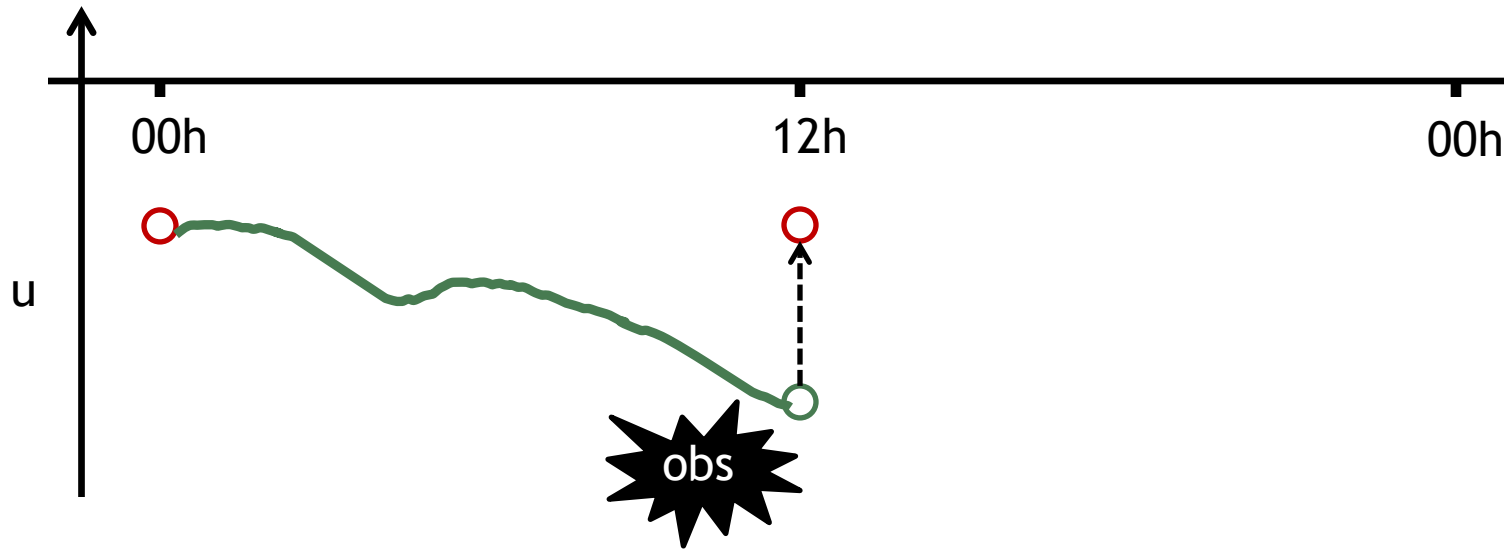
Could this increment explain our budget residual?

Surface Wind Stress

~

Lowest model level zonal wind

# Lower tropospheric zonal mean zonal wind



Could this increment explain our budget residual?

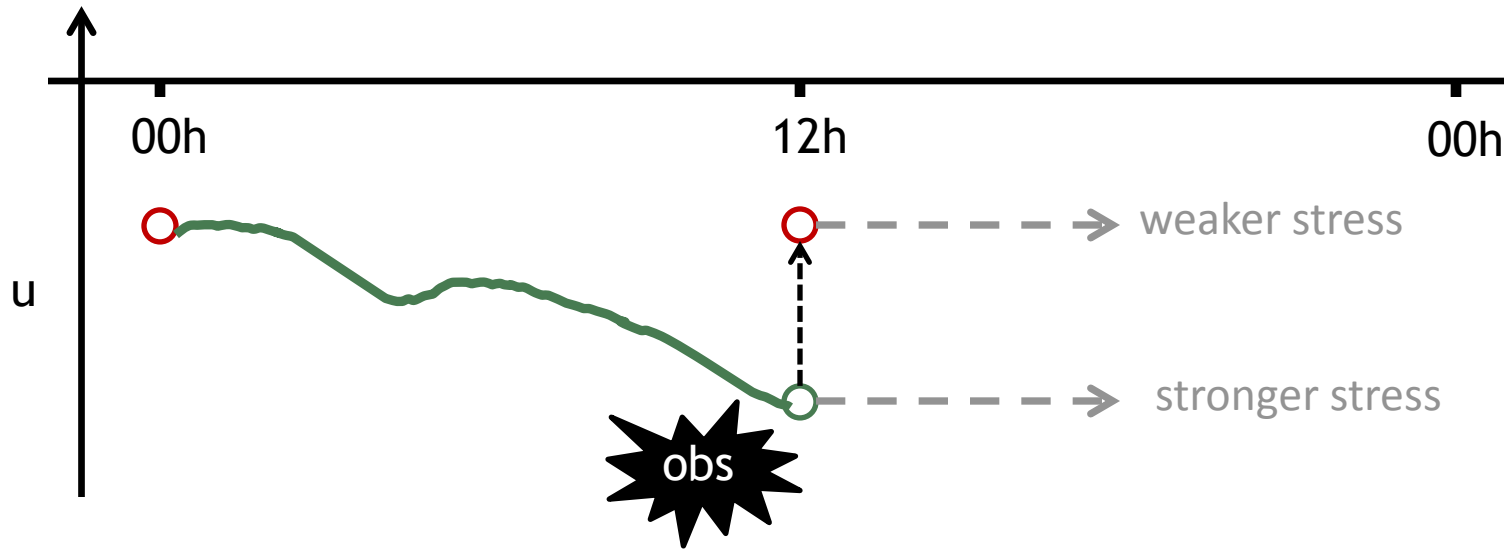
The surface stress field is accumulated over the 12h hour forecast

Surface Wind Stress

~

Lowest model level zonal wind

# Lower tropospheric zonal mean zonal wind



Could this increment explain our budget residual?

The surface stress field is accumulated over the 12h hour forecast

Surface Wind Stress

~

Lowest model level zonal wind

Assimilation of observations is providing a clear tendency to reduce the low level zonal mean easterly flow creating an imbalance in the vertically integrated momentum budget.

Assimilation of observations is providing a clear tendency to reduce the low level zonal mean easterly flow creating an imbalance in the vertically integrated momentum budget.

## Possibilities

Assimilation of observations is providing a clear tendency to reduce the low level zonal mean easterly flow creating an imbalance in the vertically integrated momentum budget.

## Possibilities

- The assimilation is incorrectly constraining the low level zonal mean flow.

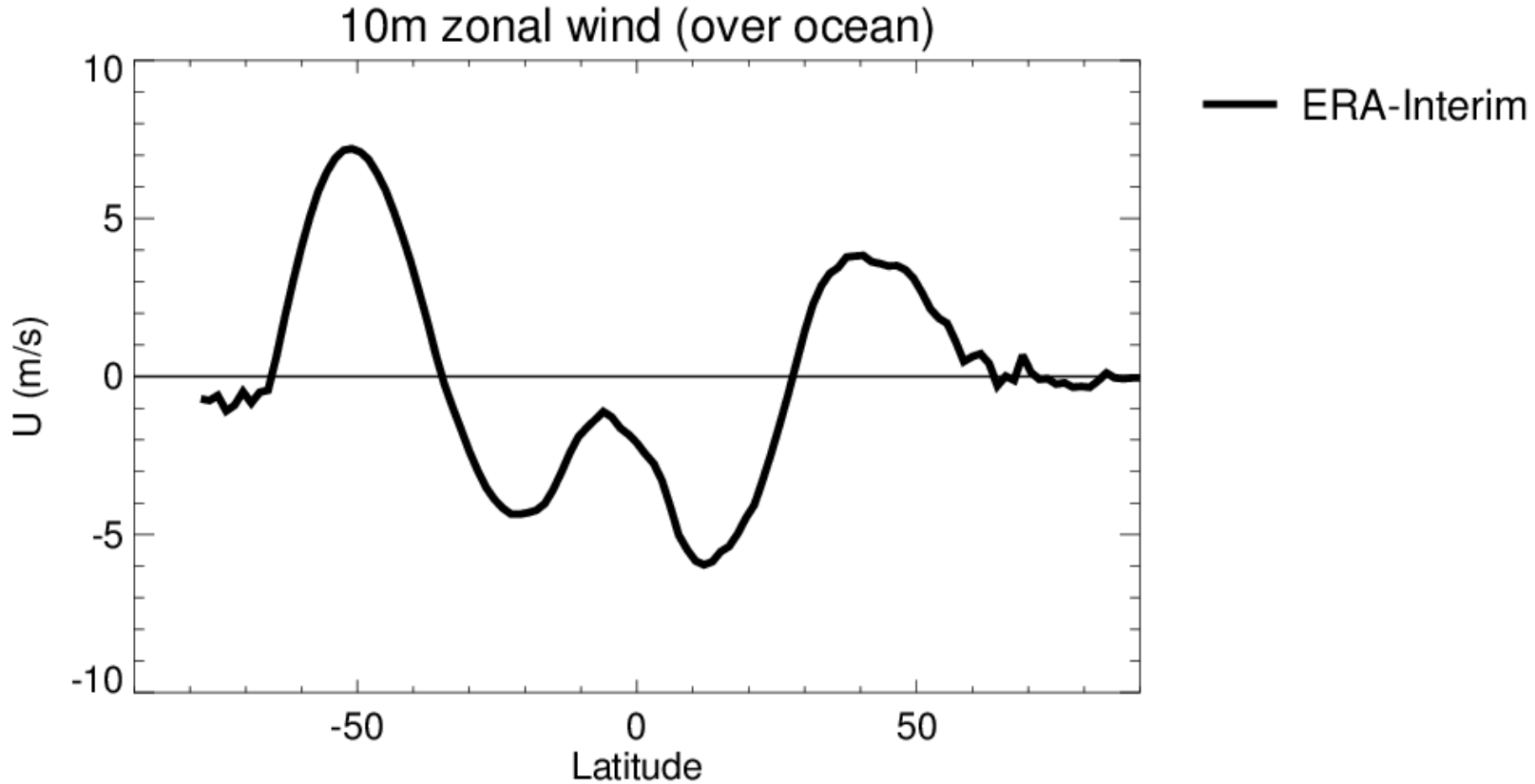
Assimilation of observations is providing a clear tendency to reduce the low level zonal mean easterly flow creating an imbalance in the vertically integrated momentum budget.

## Possibilities

- The assimilation is incorrectly constraining the low level zonal mean flow.
- The assimilation is correctly constraining the flow at low levels and is accounting for something going wrong in the forecast model.

# Is the low level flow in ERA-Interim correct?

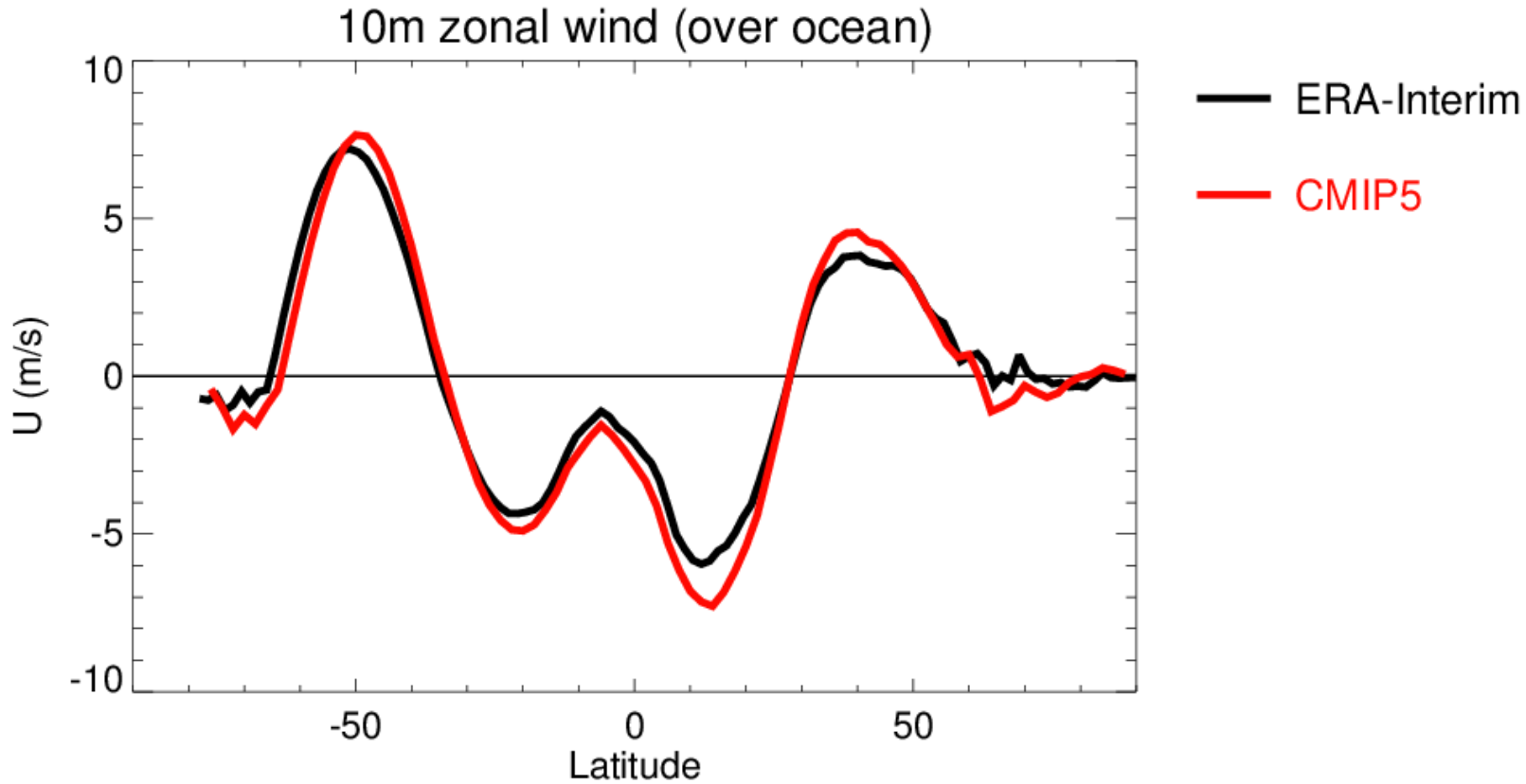
- A comparison of 10m wind products over the ocean





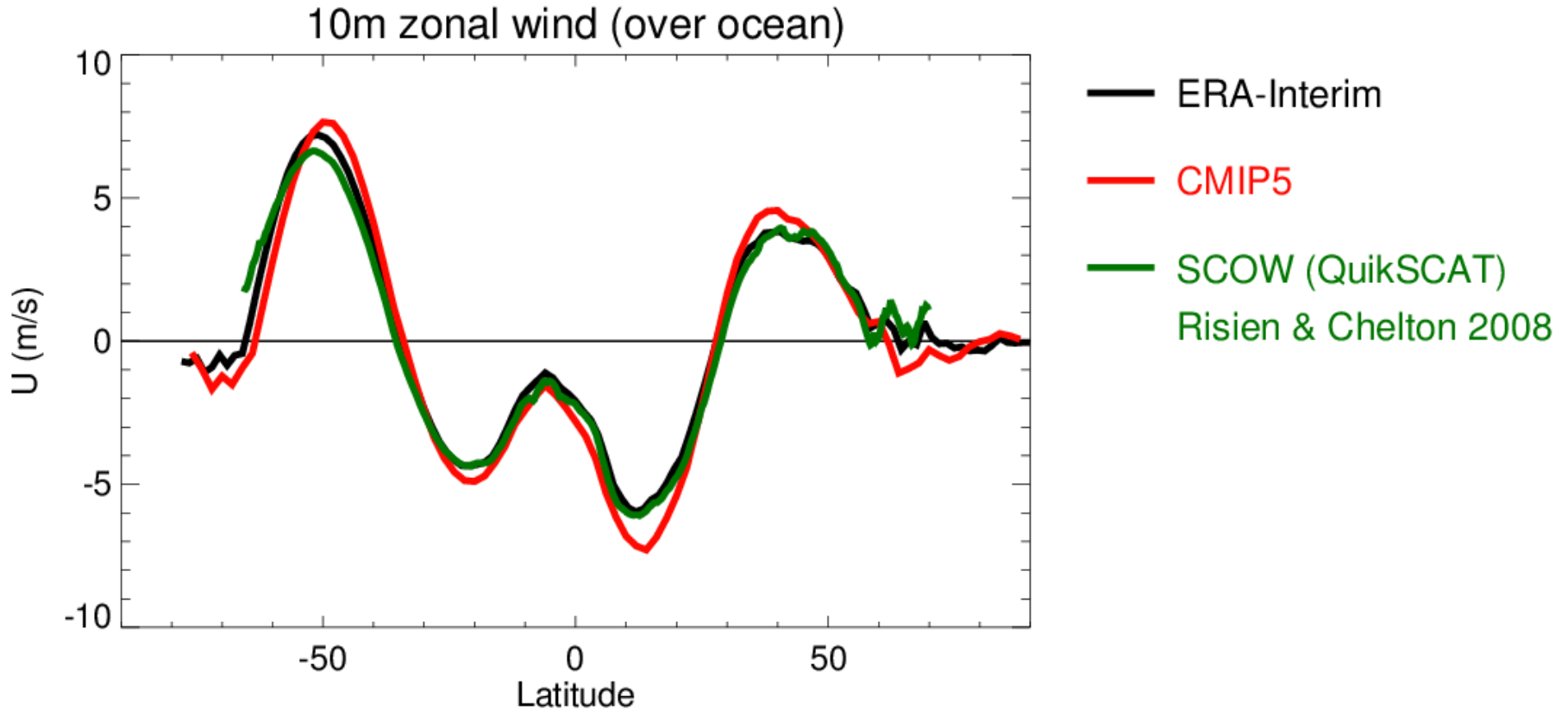
# Is the low level flow in ERA-Interim correct?

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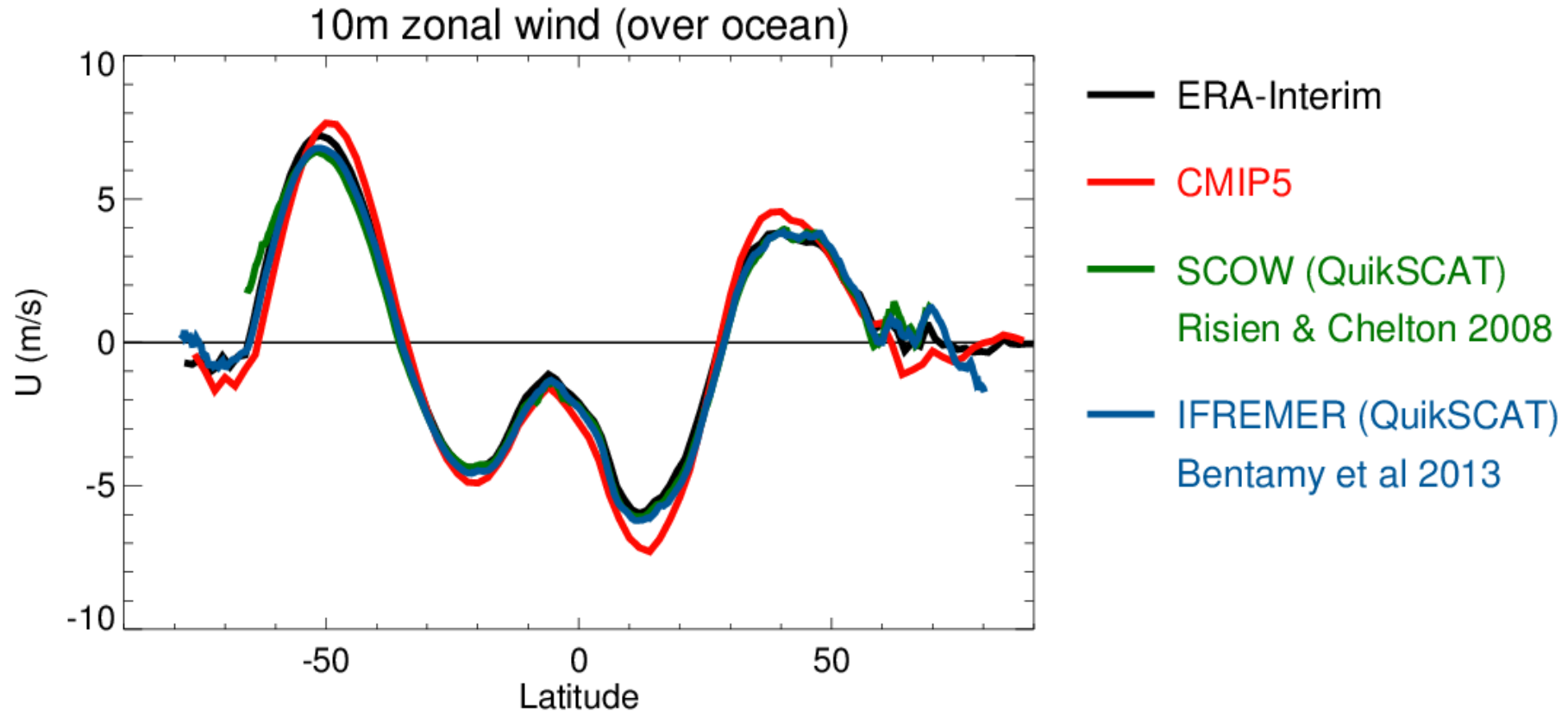
# Is the low level flow in ERA-Interim correct?

- A comparison of 10m wind products over the ocean



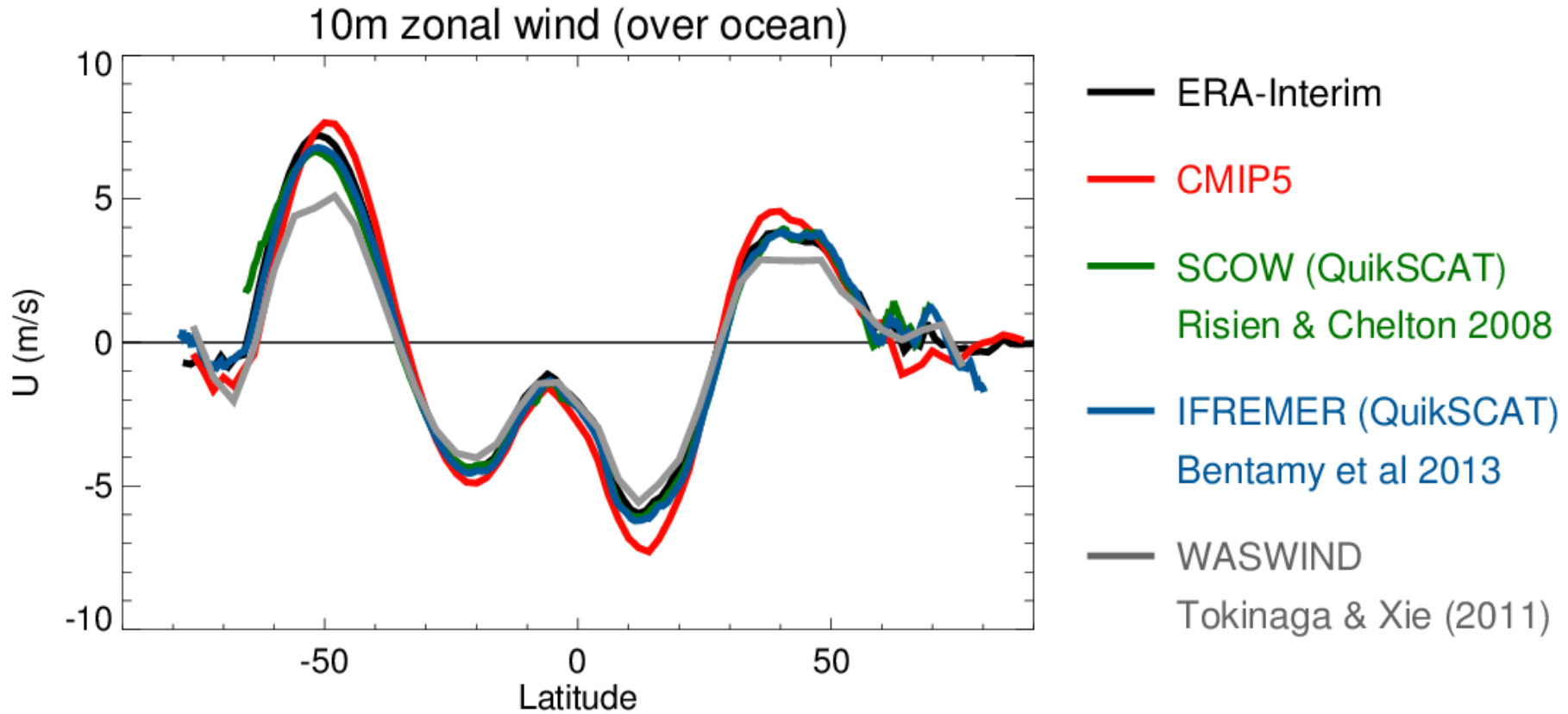
# Is the low level flow in ERA-Interim correct?

- A comparison of 10m wind products over the ocean





# Is the low level flow in ERA-Interim correct?

- A comparison of 10m wind products over the ocean





Assimilation of observations is providing a clear tendency to reduce the low level zonal mean easterly flow creating an imbalance in the vertically integrated momentum budget.

## Possibilities

- The assimilation is incorrectly constraining the low level zonal mean flow. 
- The assimilation is correctly constraining the flow at low levels. The increments are, therefore, accounting for something going wrong in the forecast model. 

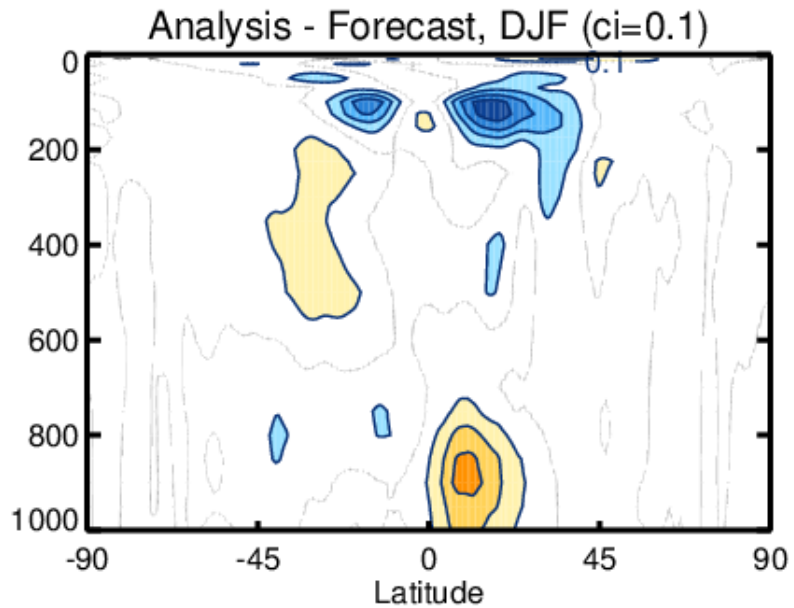
Assimilation of observations is providing a clear tendency to reduce the low level zonal mean easterly flow creating an imbalance in the vertically integrated momentum budget.

## Possibilities

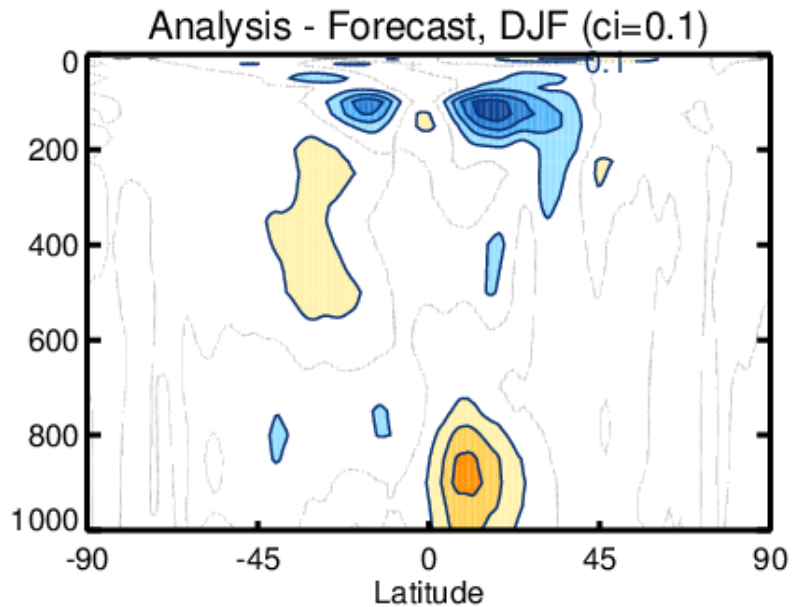
- The assimilation is incorrectly constraining the low level zonal mean flow. 
- The assimilation is correctly constraining the flow at low levels. The increments are, therefore, accounting for something going wrong in the forecast model. 

An understanding of this may help to understand issues in the CMIP models as well.

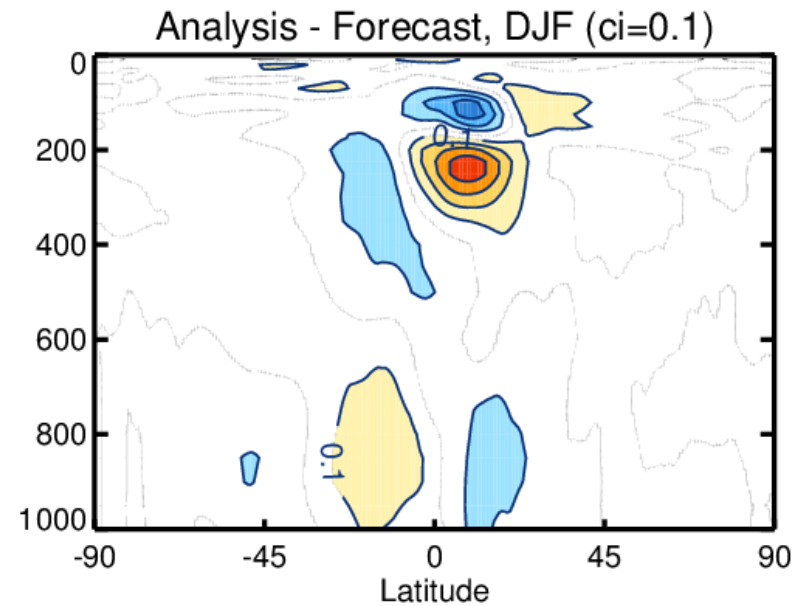
Zonal mean U  
(Analysis - Forecast)



Zonal mean U  
(Analysis - Forecast)

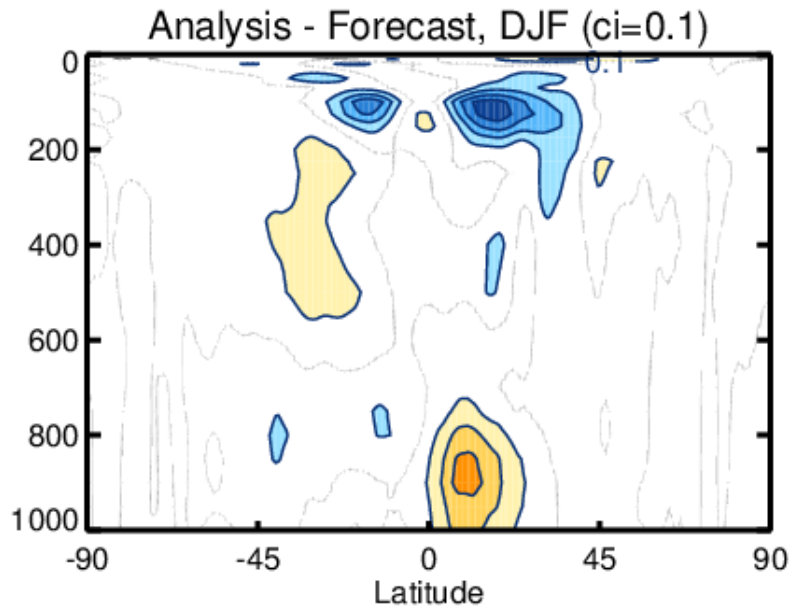


Zonal mean V  
(Analysis - Forecast)

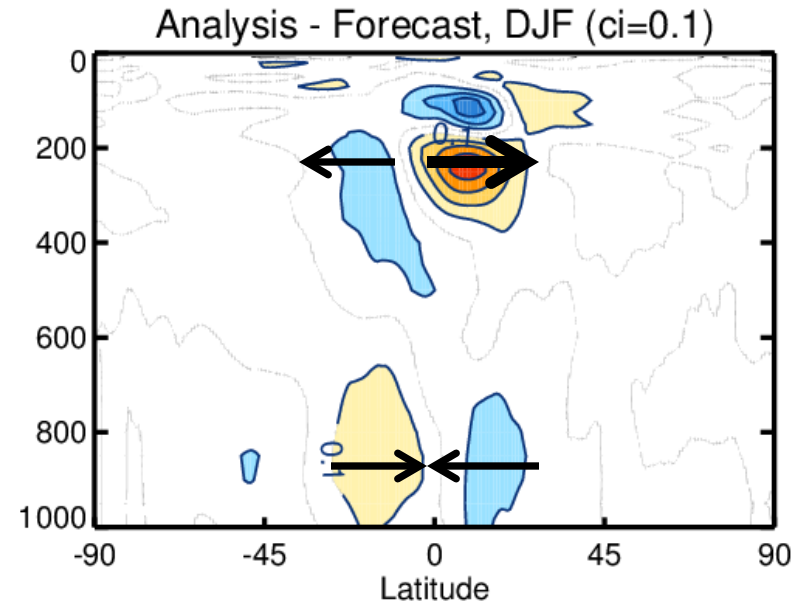




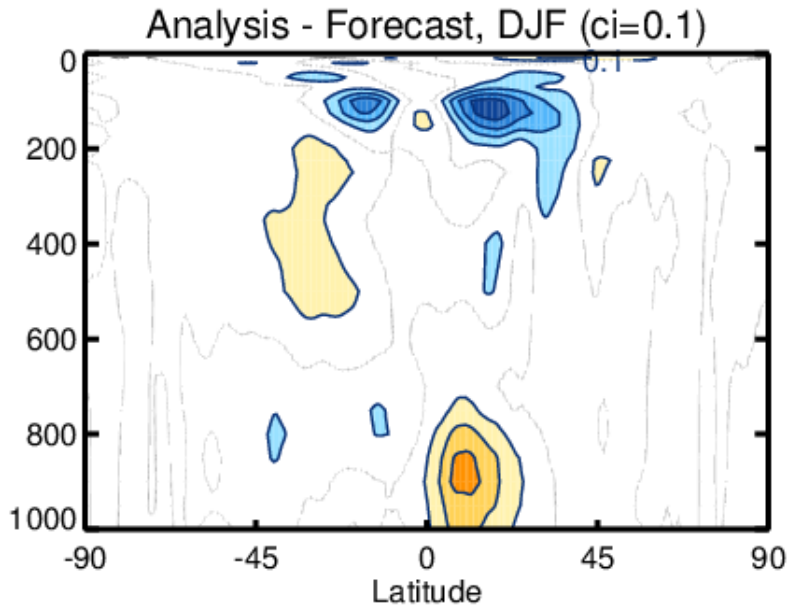
Zonal mean U  
(Analysis - Forecast)



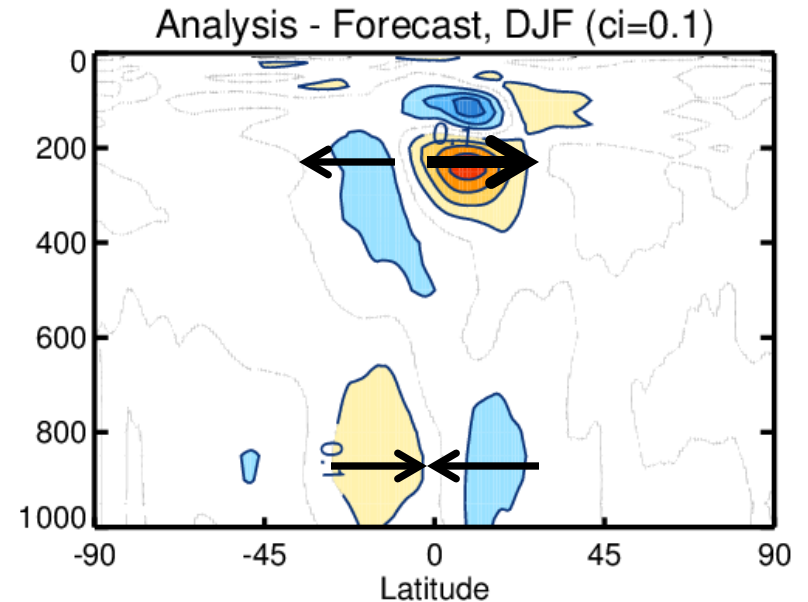
Zonal mean V  
(Analysis - Forecast)



Zonal mean U  
(Analysis - Forecast)



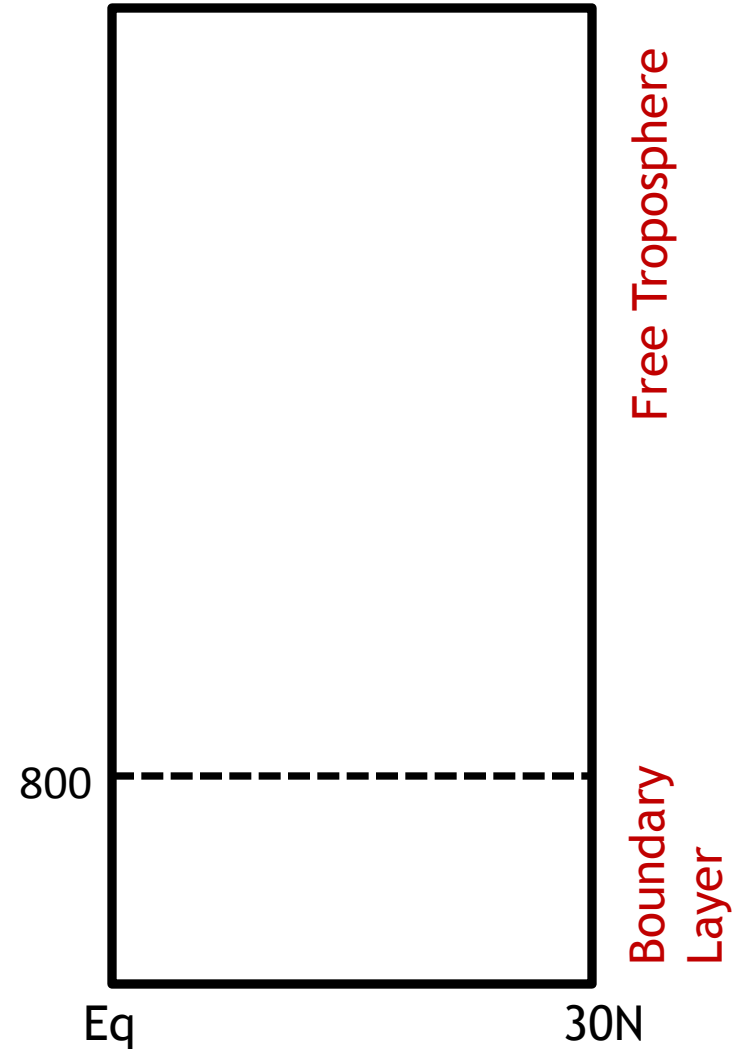
Zonal mean V  
(Analysis - Forecast)



Assimilation weakens the low level easterlies, but strengthens the Hadley circulation

# Local Zonal Momentum Balances

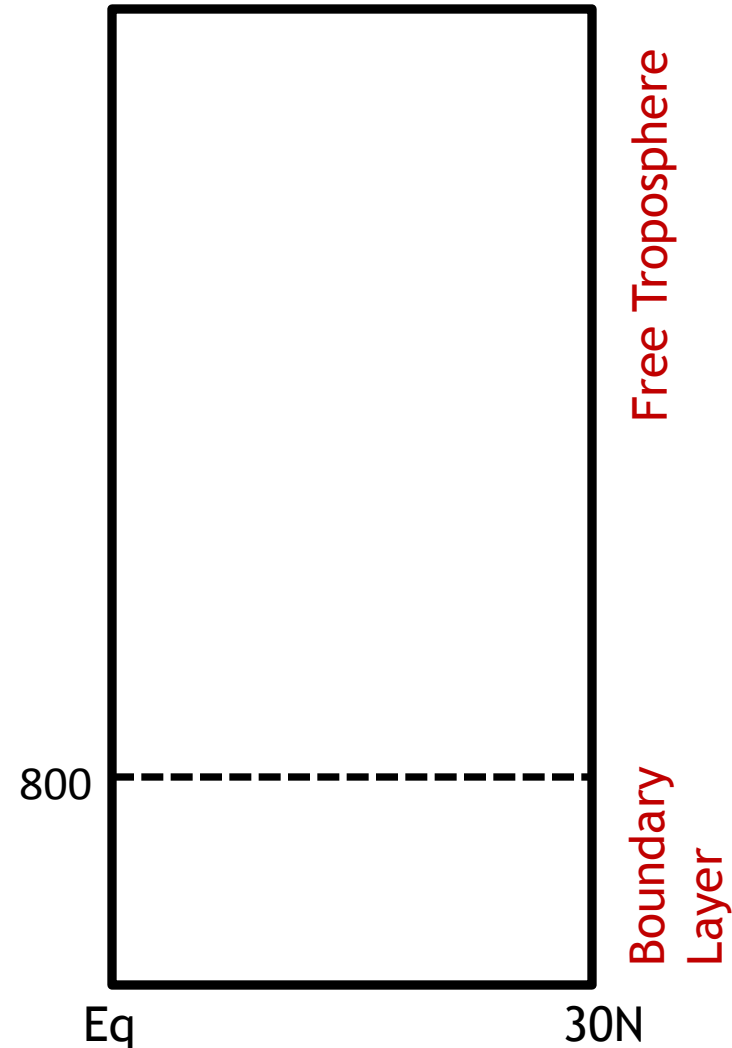
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# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

$$\frac{\partial u}{\partial t} = fv + UV_{conv}$$

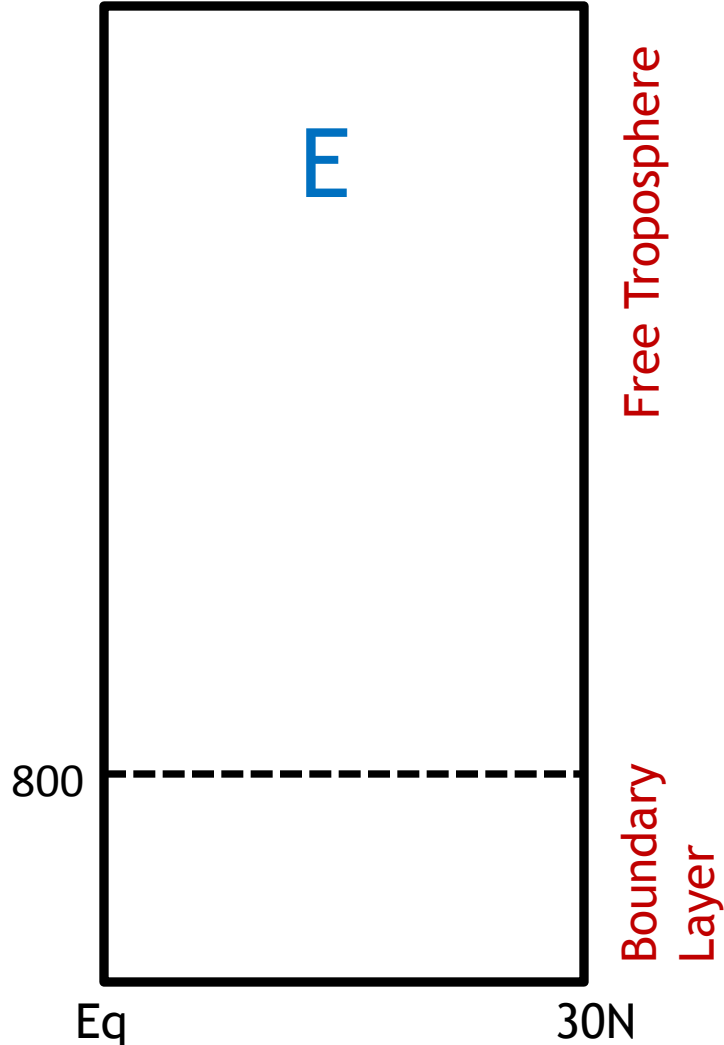


# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

$$\frac{\partial u}{\partial t} = fv + \textcircled{UV_{conv}}$$

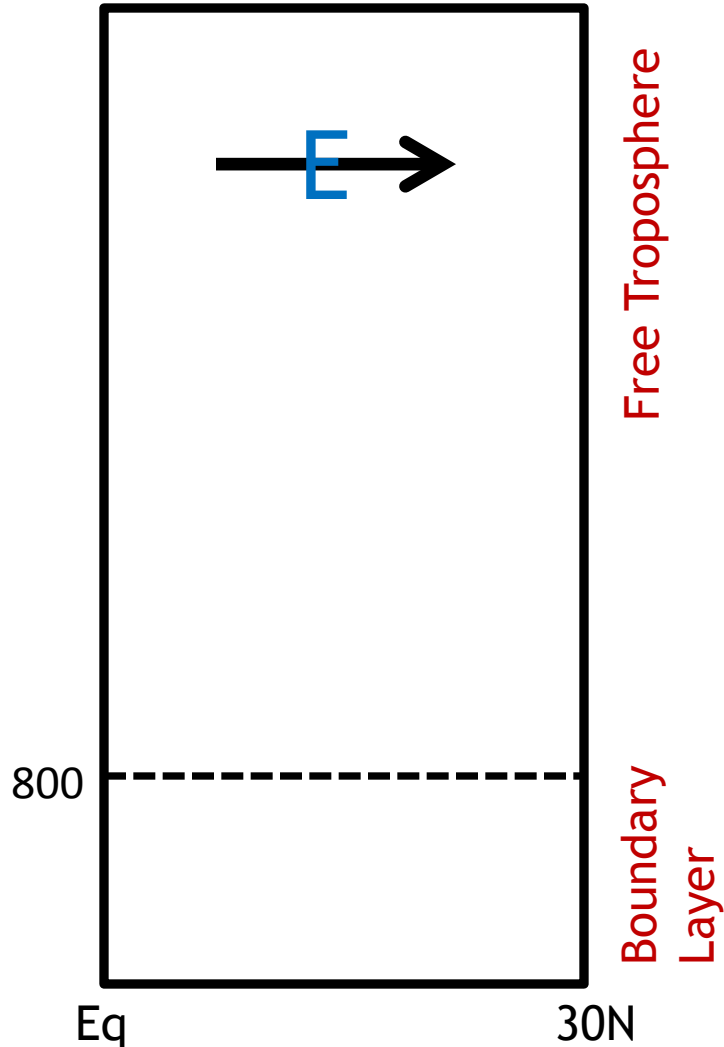
E



# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

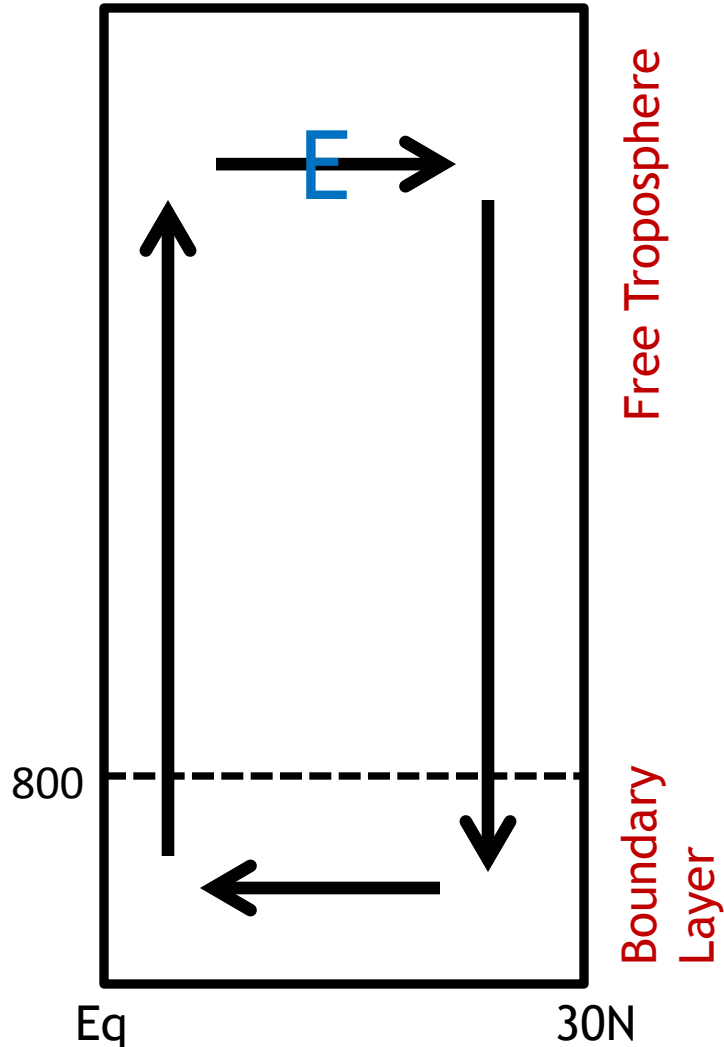
$$\frac{\partial u}{\partial t} = \underbrace{fv}_W + \underbrace{UV_{conv}}_E$$



# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

$$\frac{\partial u}{\partial t} = \underbrace{fv}_{W} + \underbrace{UV_{conv}}_{E}$$



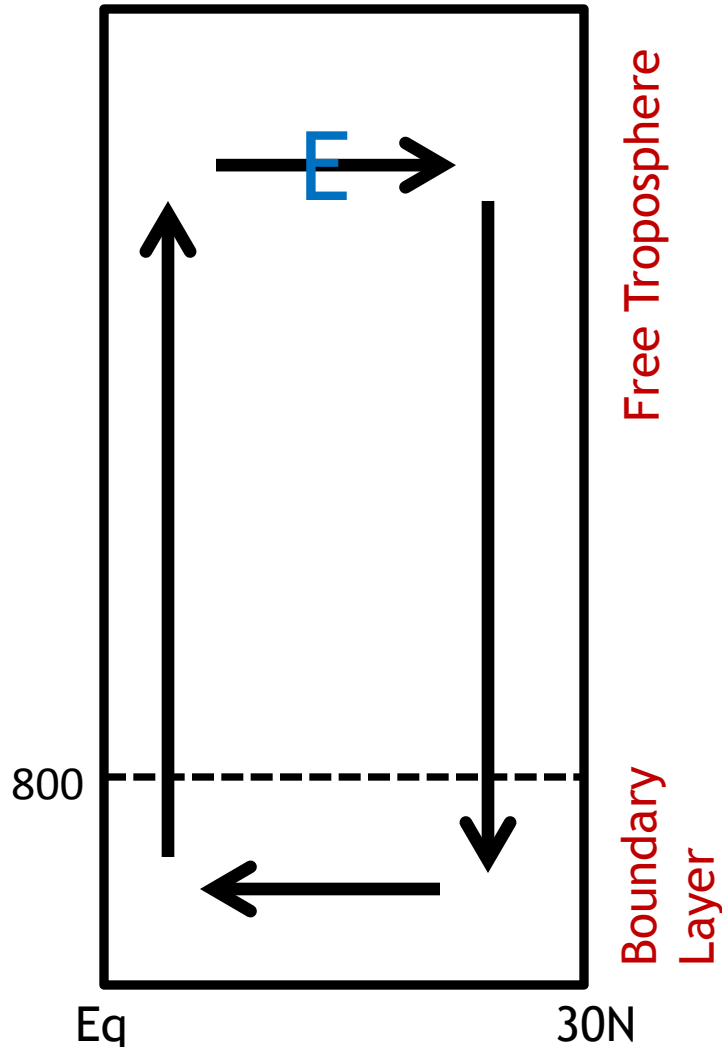
# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

$$\frac{\partial u}{\partial t} = \underbrace{fv}_{W} + \underbrace{UV_{conv}}_{E}$$

Dominant Balance in the Boundary Layer:

$$\frac{\partial u}{\partial t} = fv + UV_{conv} + M + F_u$$





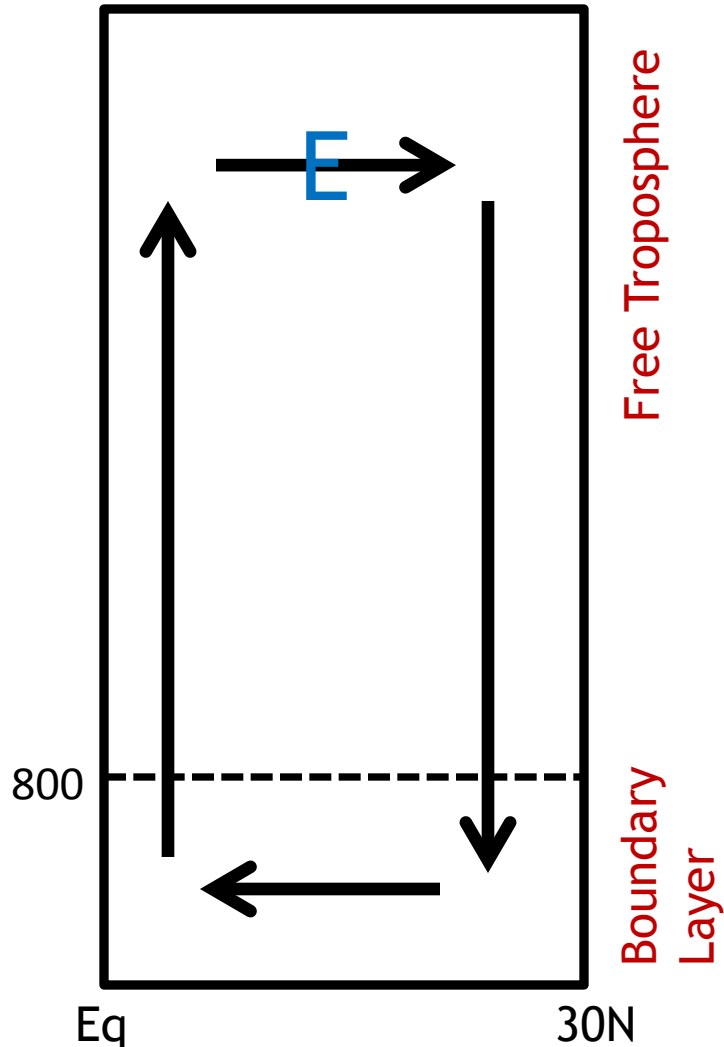
# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

$$\frac{\partial u}{\partial t} = \underbrace{fv}_{W} + \underbrace{UV_{conv}}_{E}$$

Dominant Balance in the Boundary Layer:

$$\frac{\partial u}{\partial t} = \underbrace{fv}_{E} + UV_{conv} + M + F_u$$



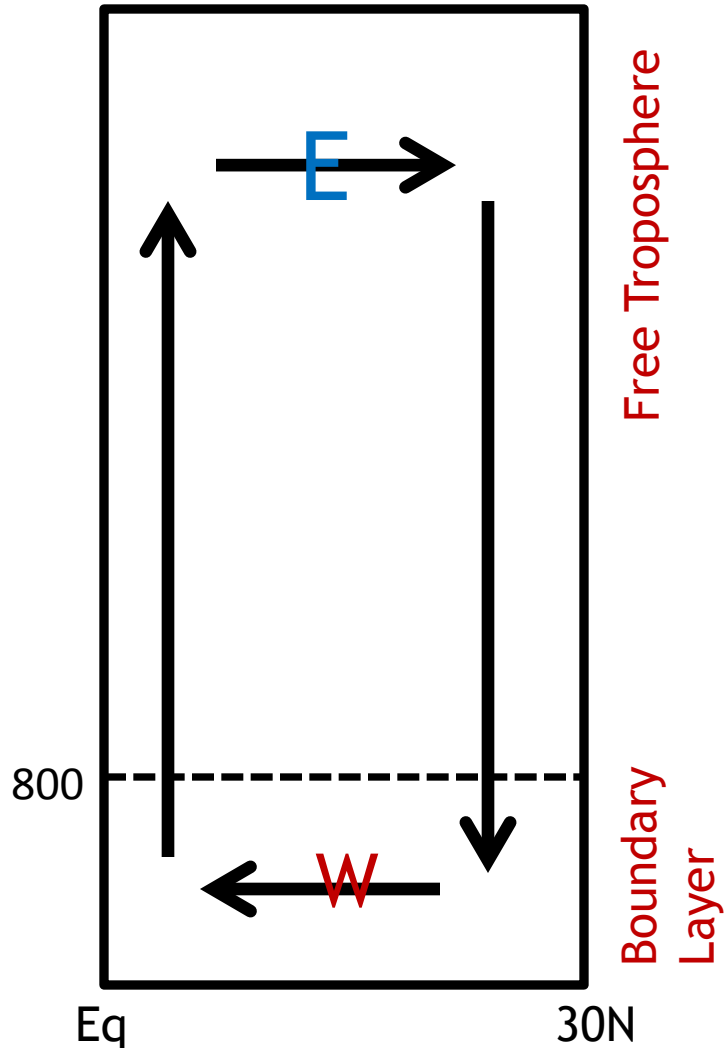
# Local Zonal Momentum Balances

Dominant Balance in the Free troposphere:

$$\frac{\partial u}{\partial t} = \underbrace{fv}_{W} + \underbrace{UV_{conv}}_{E}$$

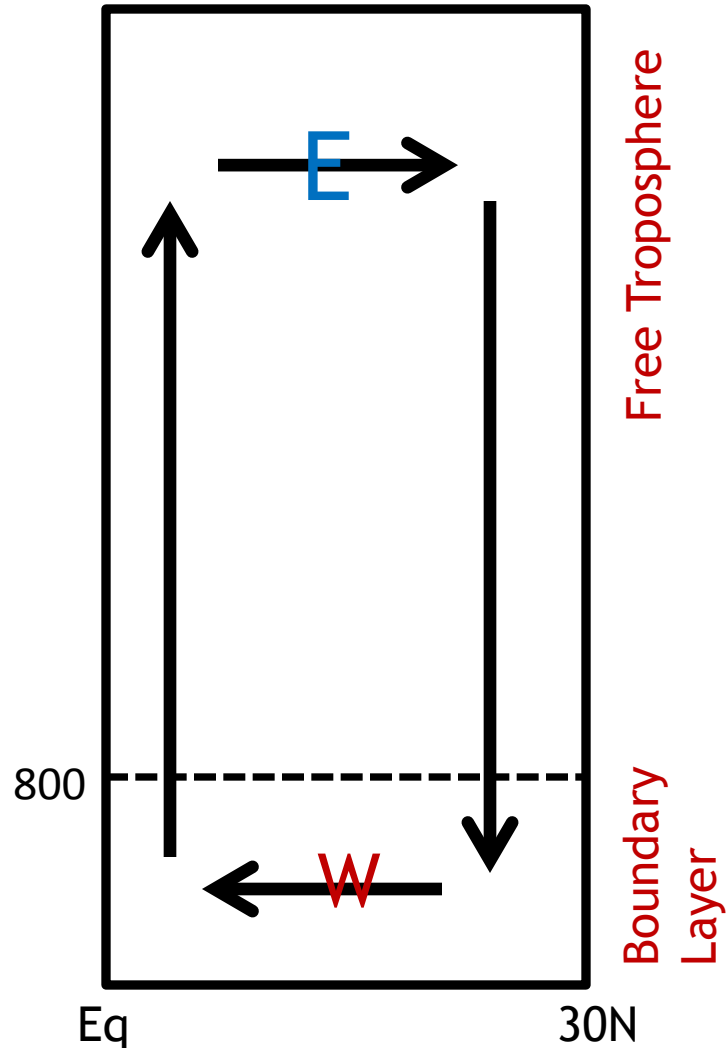
Dominant Balance in the Boundary Layer:

$$\frac{\partial u}{\partial t} = \underbrace{fv}_{E} + UV_{conv} + \underbrace{M + F_u}_{W}$$

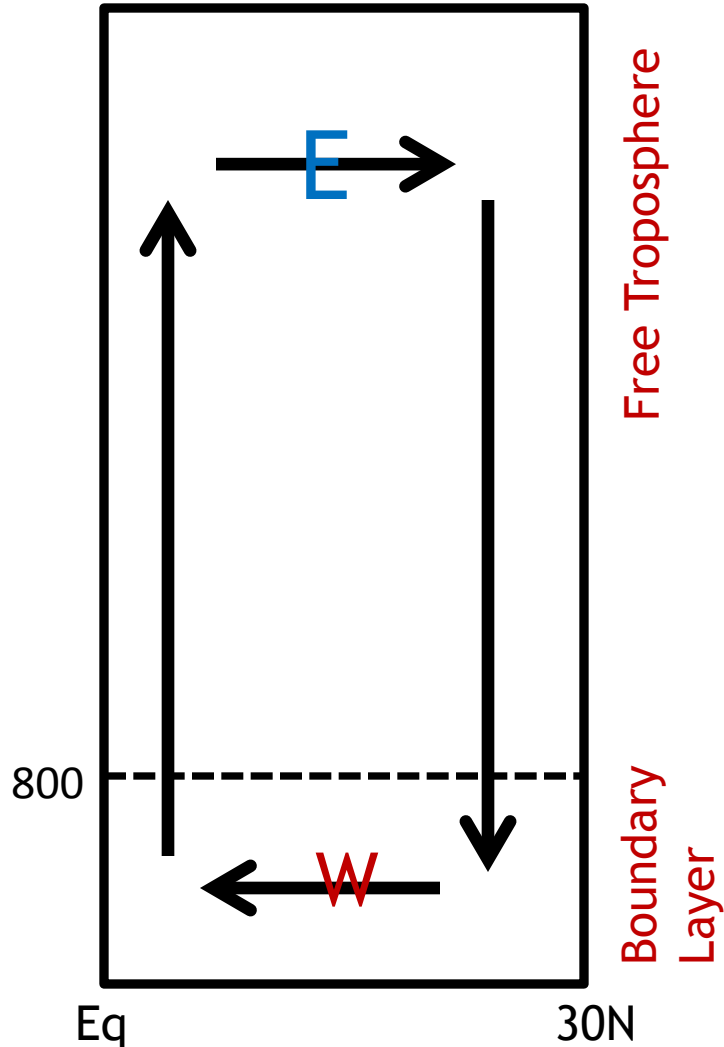


# Local Zonal Momentum Balances

Where might things be going wrong?  
Free troposphere or Boundary Layer?



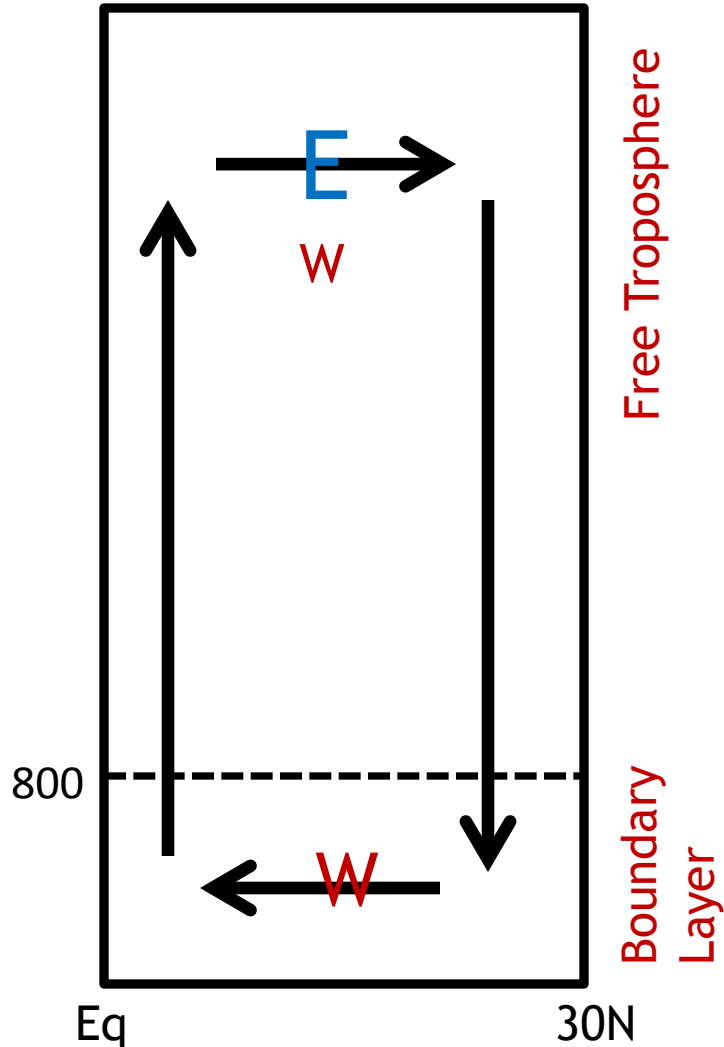
# Local Zonal Momentum Balances



Where might things be going wrong?  
Free troposphere or Boundary Layer?

Could be missing a westerly forcing in the free troposphere e.g., missing physics, incorrect resolved dynamics.

# Local Zonal Momentum Balances



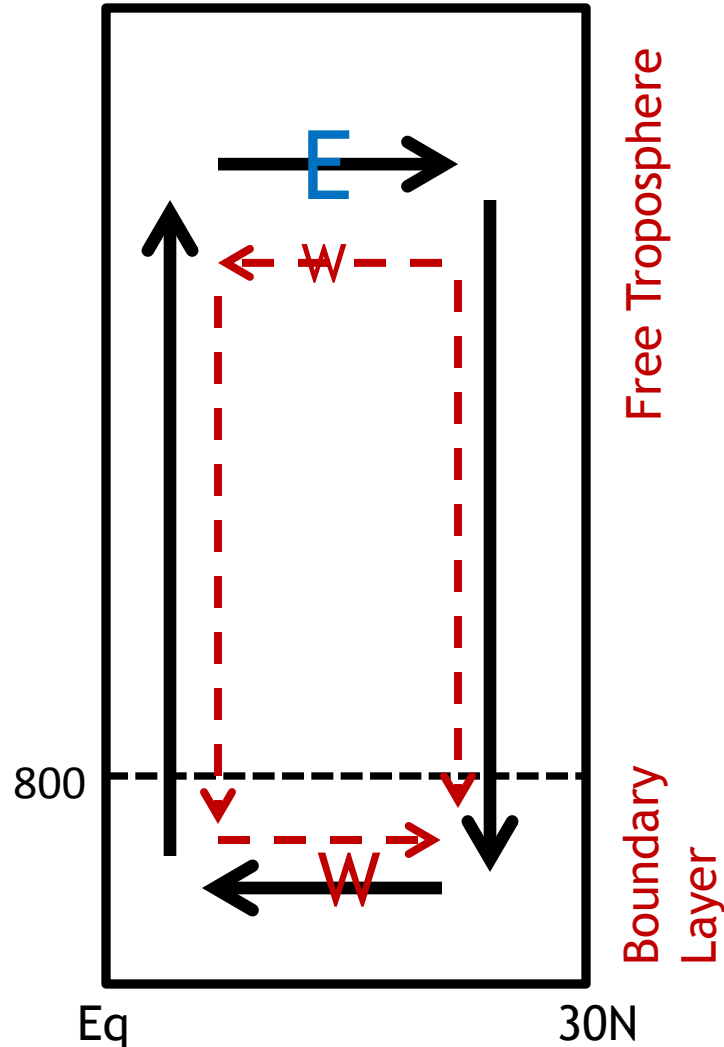
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# Local Zonal Momentum Balances

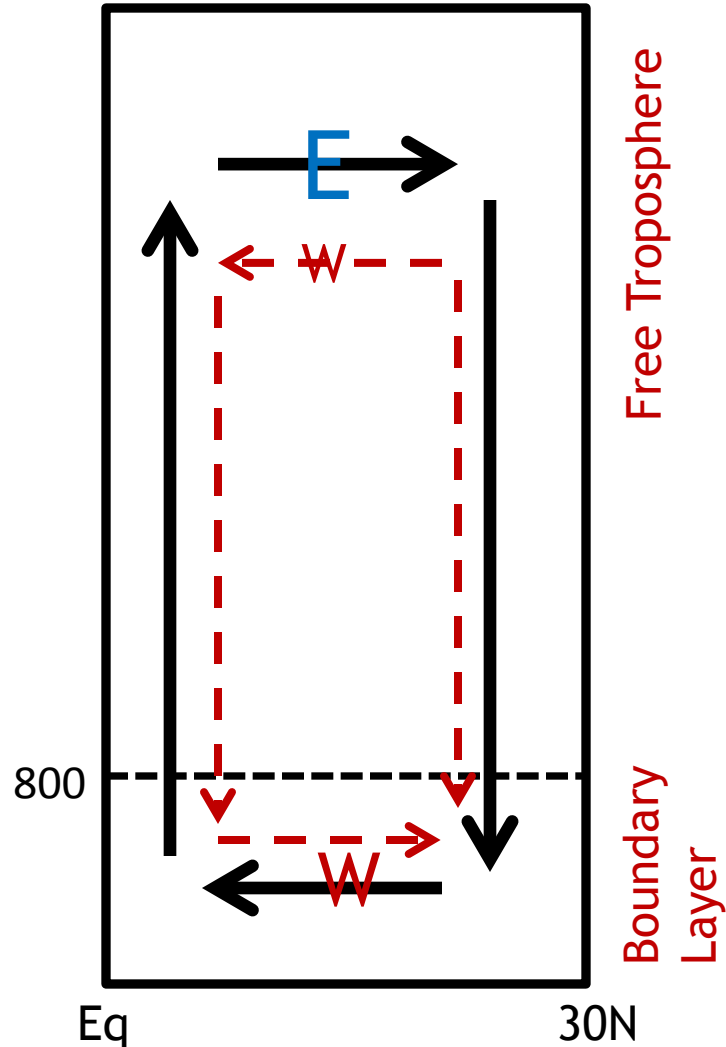
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Free troposphere or Boundary Layer?

Could be missing a westerly forcing in the free troposphere e.g., missing physics, incorrect resolved dynamics.

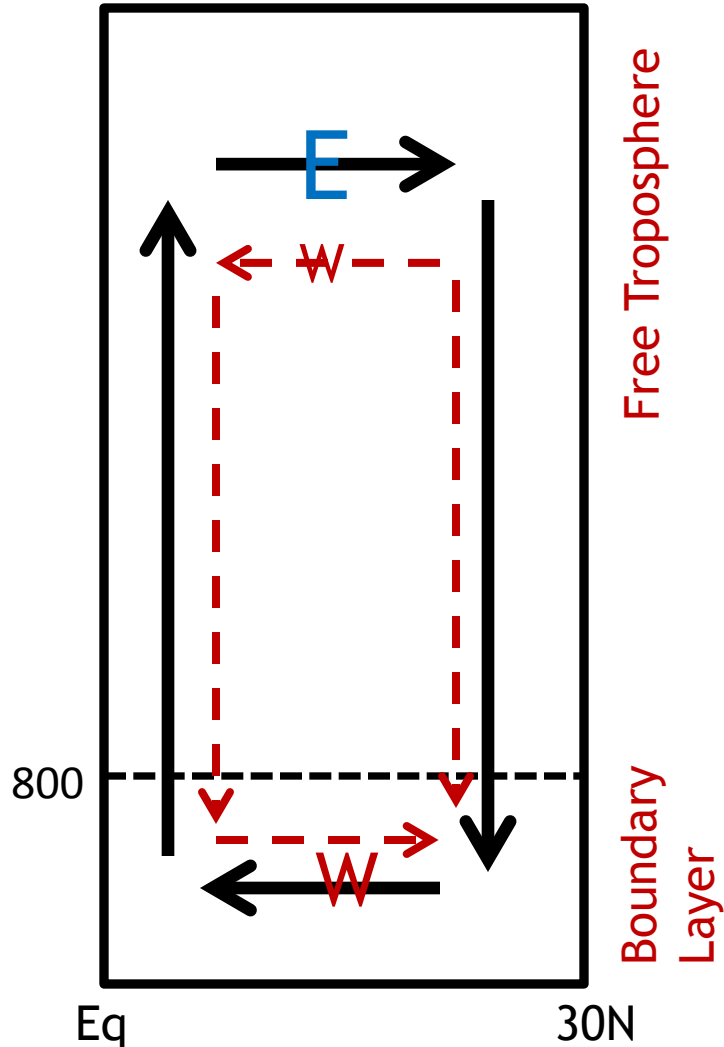


# Local Zonal Momentum Balances

If we are missing a westerly forcing in the upper troposphere...



# Local Zonal Momentum Balances



If we are missing a westerly forcing in the upper troposphere...

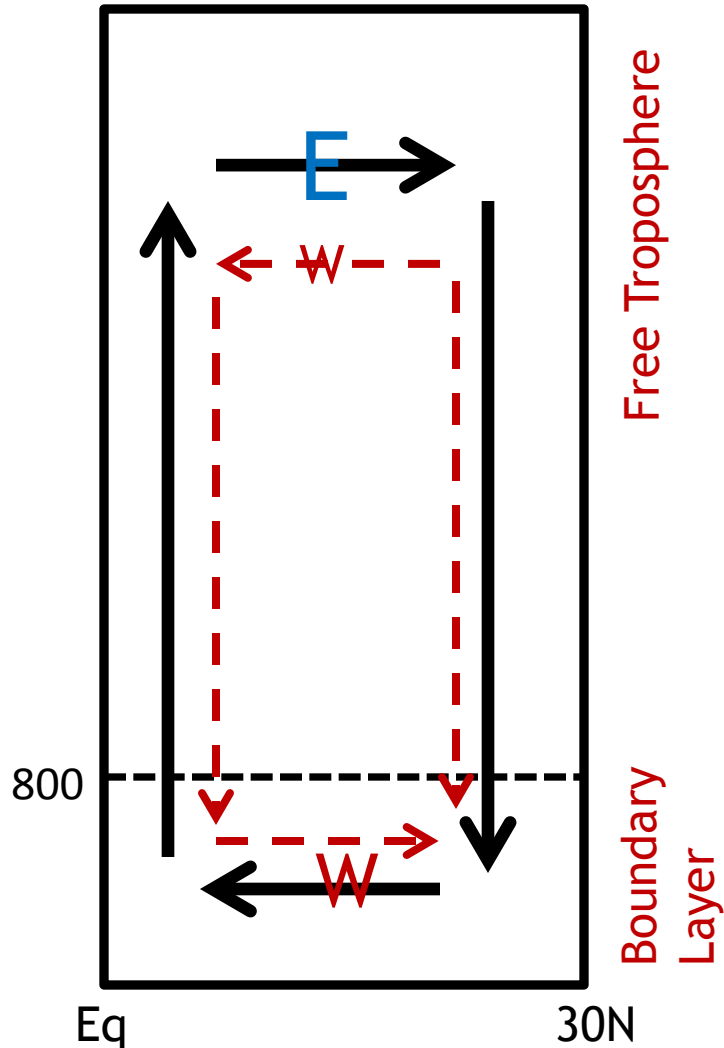
How would we expect things to evolve over the forecast?

$$\frac{\partial u}{\partial t} = f v + UV_{conv} + Z$$

0      W      E      W



# Local Zonal Momentum Balances



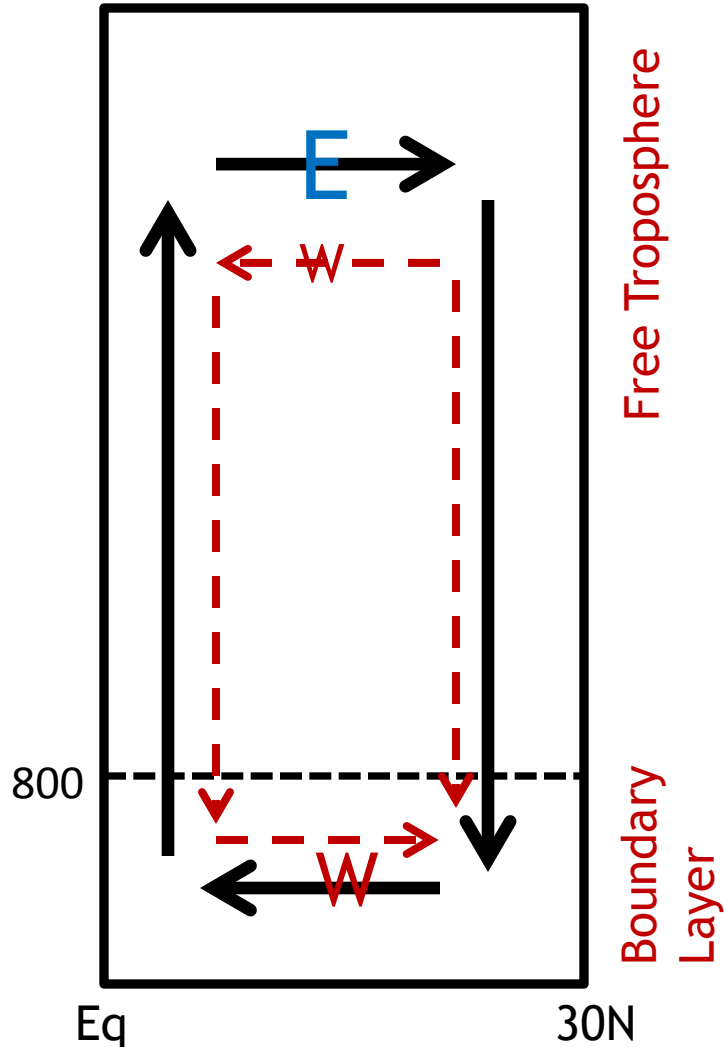
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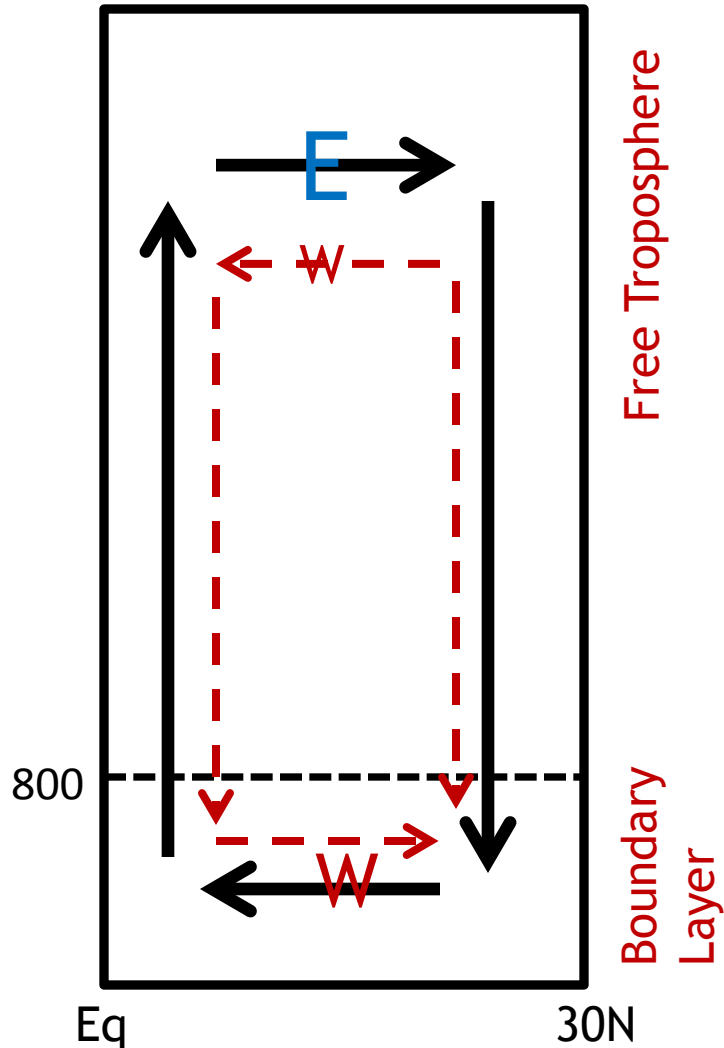
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0      W      E      ~~W~~

Imbalance → E ↑

# Local Zonal Momentum Balances



If we are missing a westerly forcing in the upper troposphere...

How would we expect things to evolve over the forecast?

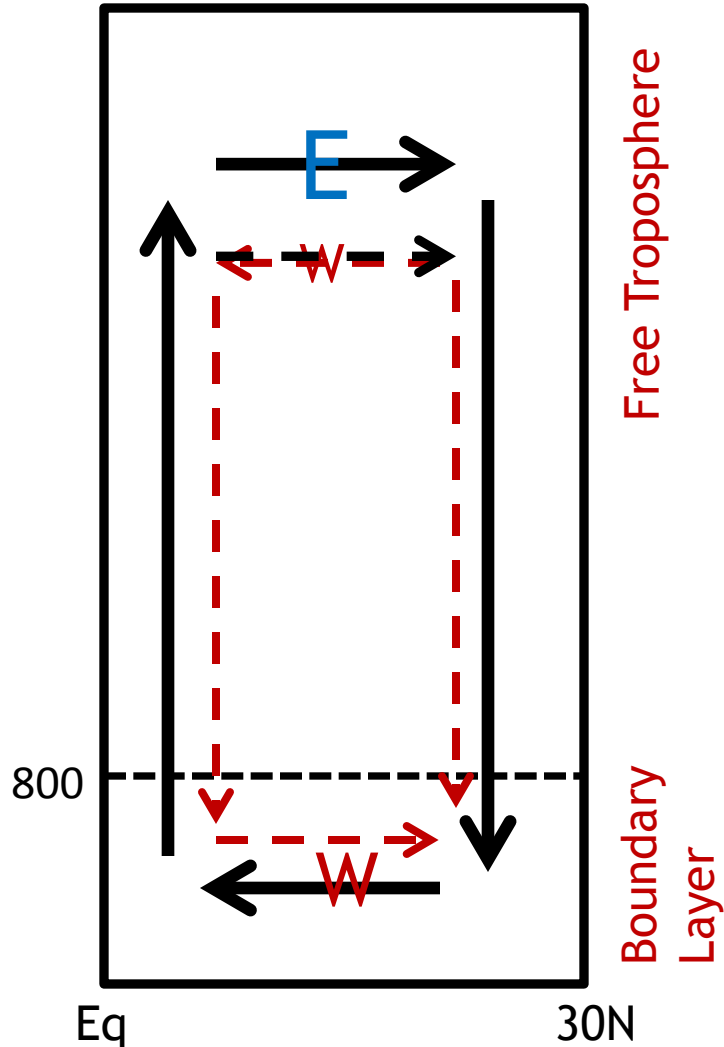
We'd expect...

An easterly acceleration in the upper troposphere

$$\frac{\partial u}{\partial t} = f v + UV_{conv} + Z$$

0	W	E	<del>W</del>
E ↑			<del>W</del> ↑

# Local Zonal Momentum Balances



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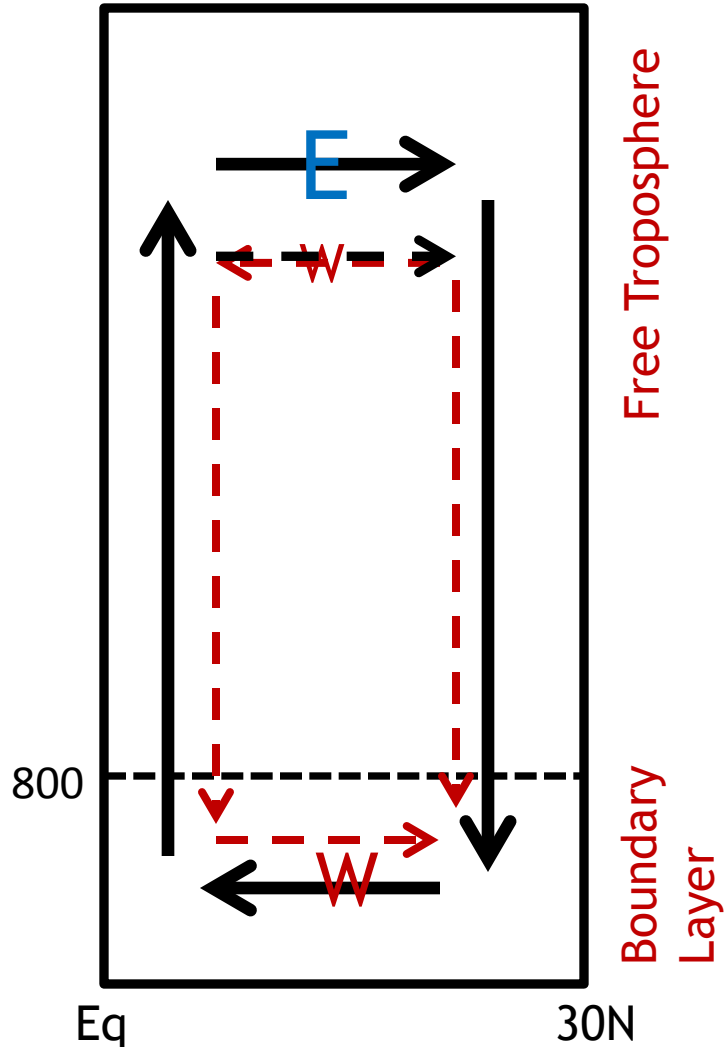
and/or

The upper level Southerlies to strengthen

$$\frac{\partial u}{\partial t} = f v + UV_{conv} + Z$$

0	W	E	<del>W</del>
E ↑	W ↑		E ↑

# Local Zonal Momentum Balances



If we are missing a westerly forcing in the upper troposphere...

How would we expect things to evolve over the forecast?

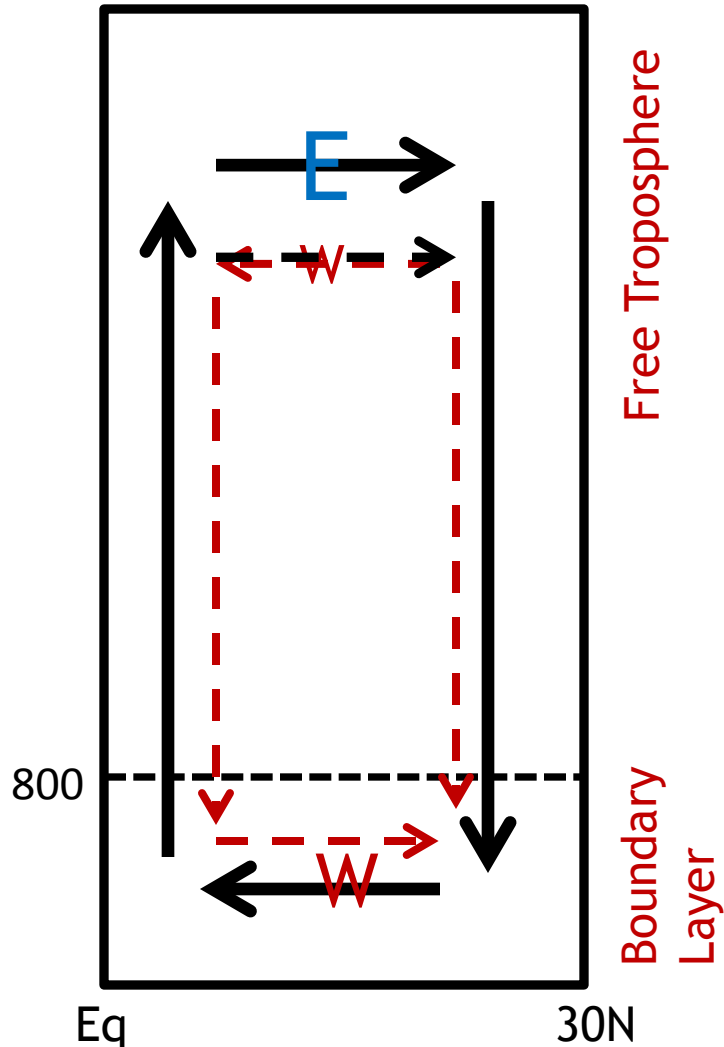
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# Local Zonal Momentum Balances



If we are missing a westerly forcing in the upper troposphere...

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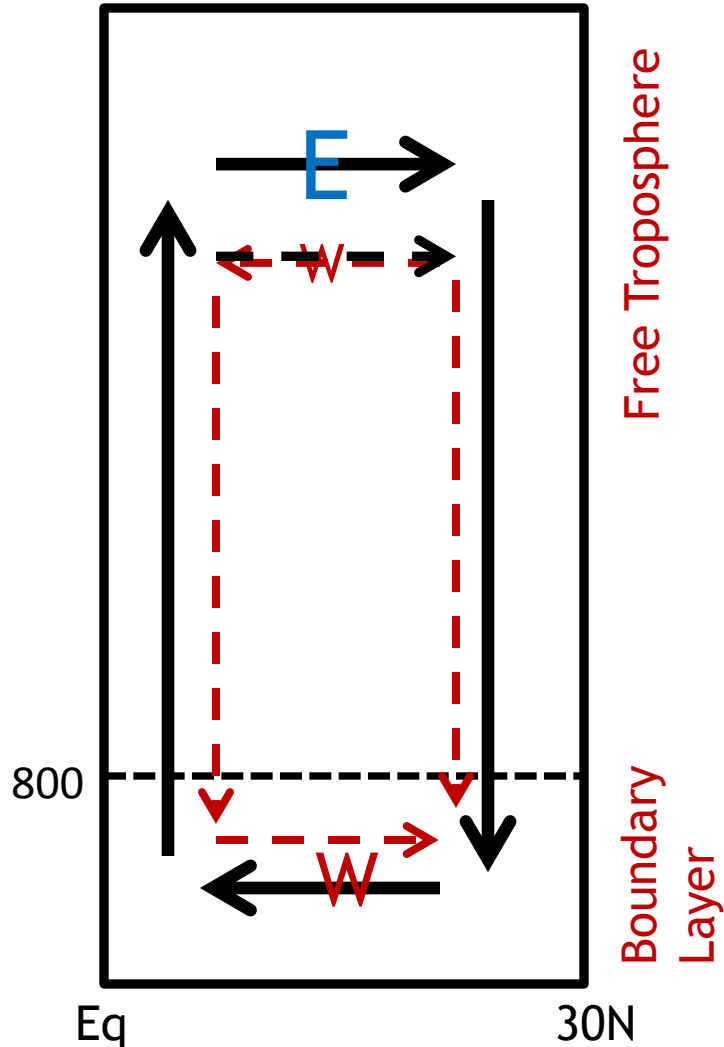
An easterly acceleration in the upper troposphere

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The analysis increments would be expected to...

# Local Zonal Momentum Balances



If we are missing a westerly forcing in the upper troposphere...

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An easterly acceleration in the upper troposphere

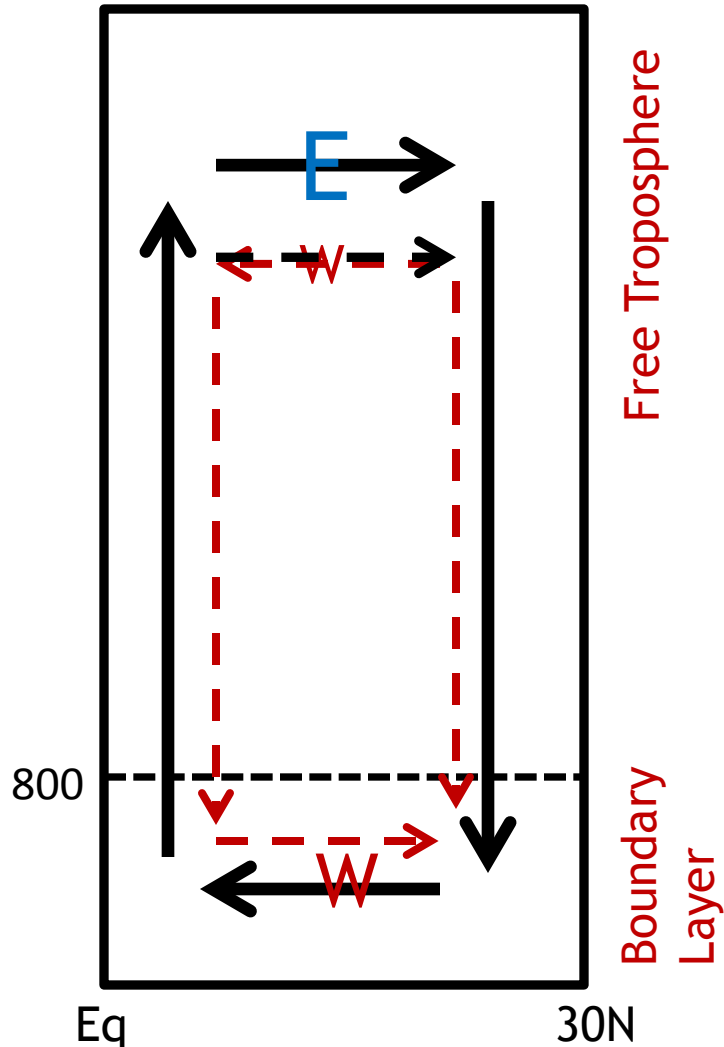
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The analysis increments would be expected to...

Provide a westerly zonal wind anomaly in the upper troposphere

# Local Zonal Momentum Balances



If we are missing a westerly forcing in the upper troposphere...

How would we expect things to evolve over the forecast?

We'd expect...

An easterly acceleration in the upper troposphere

and/or

The upper level Southerlies to strengthen

The analysis increments would be expected to...

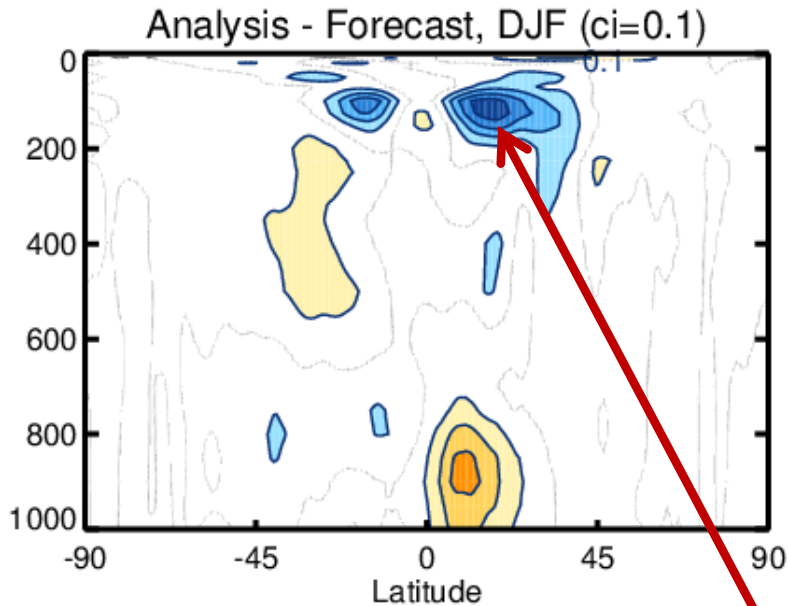
Provide a westerly zonal wind anomaly in the upper troposphere

and/or

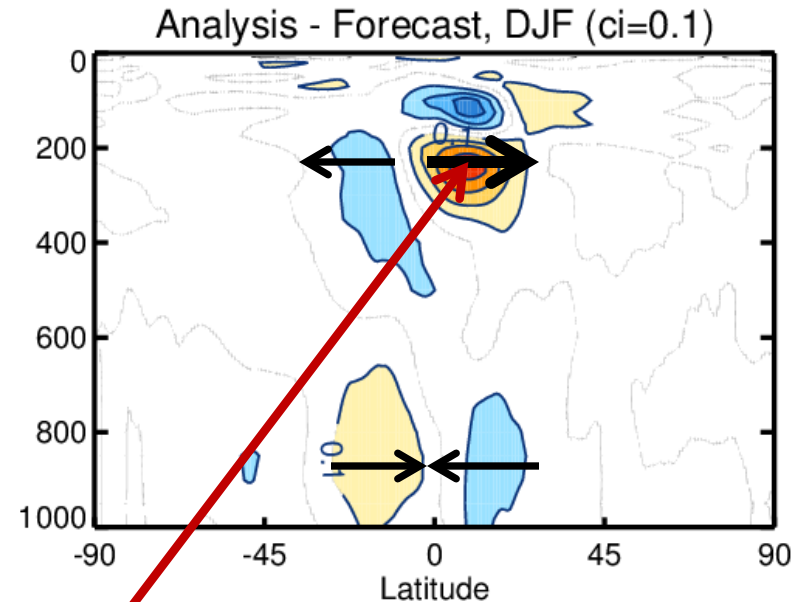
Weaken the upper level Southerlies



Zonal mean U  
(Analysis - Forecast)



Zonal mean V  
(Analysis - Forecast)

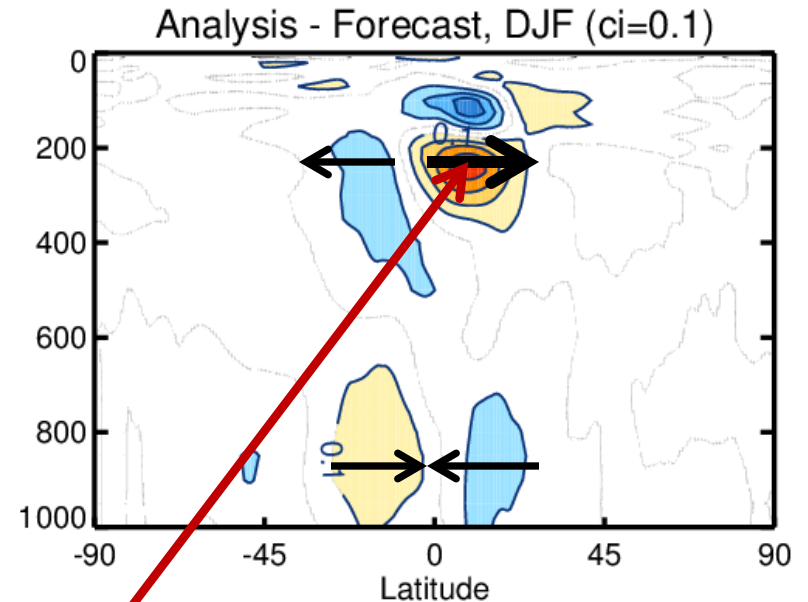
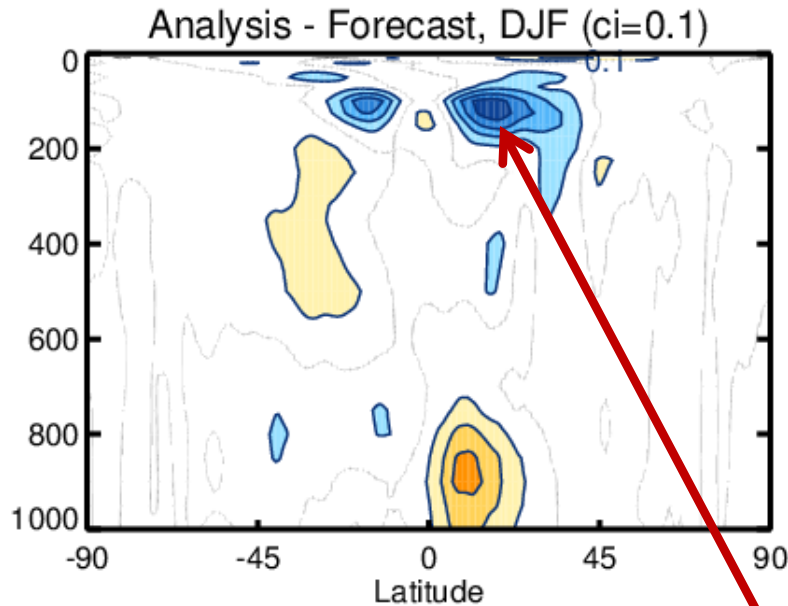


The opposite of what you'd expect in the absence of a westerly forcing in the upper troposphere

The increments are not consistent with the missing westerly forcing being in the upper troposphere

Zonally  
(Analysis)

(Forecast)

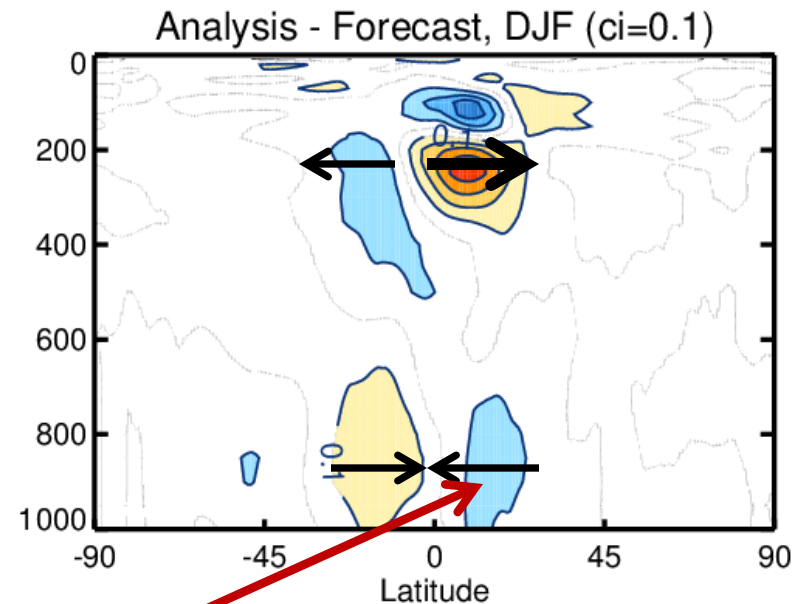
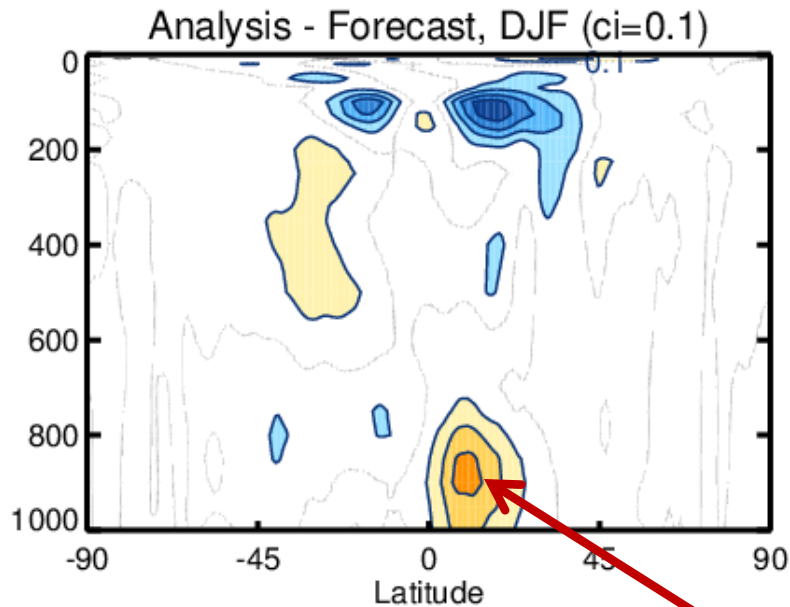


The opposite of what you'd expect in the absence of a westerly forcing in the upper troposphere

The increments are not consistent with the missing westerly forcing being in the upper troposphere

Zonally  
(Analysis)

(Forecast)



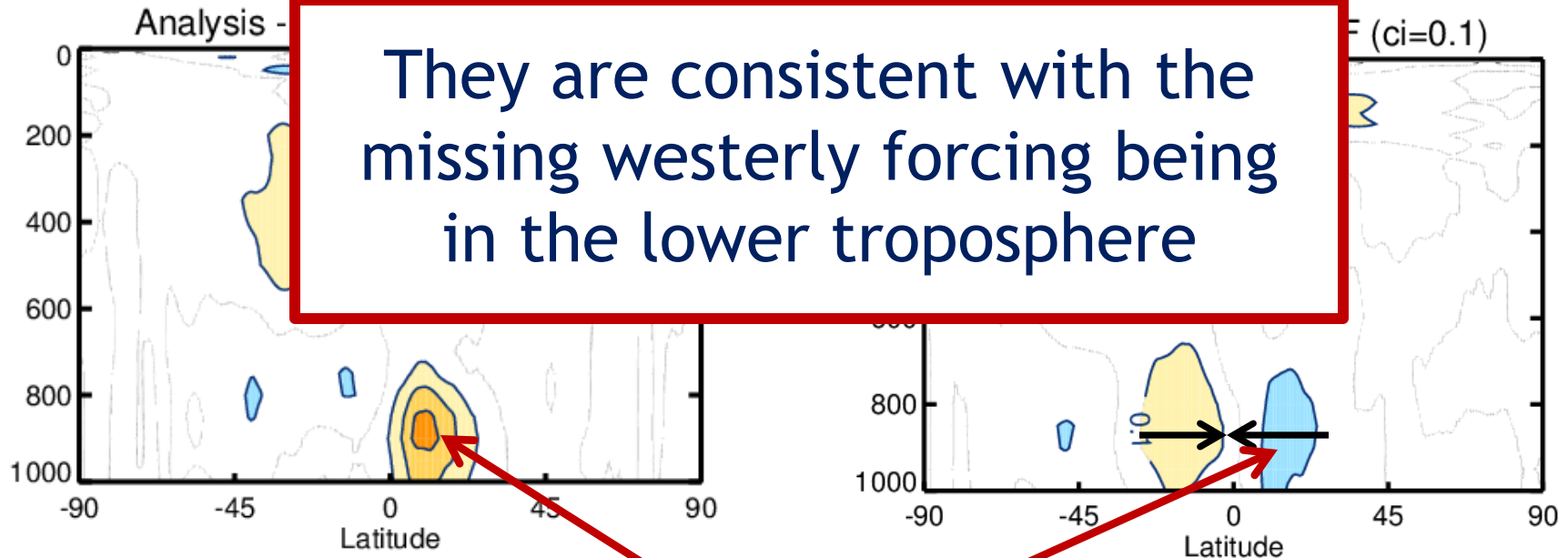
What you'd expect in the absence of a westerly forcing in the lower troposphere

The increments are not consistent with the missing westerly forcing being in the upper troposphere

Zonally  
(Analysis)

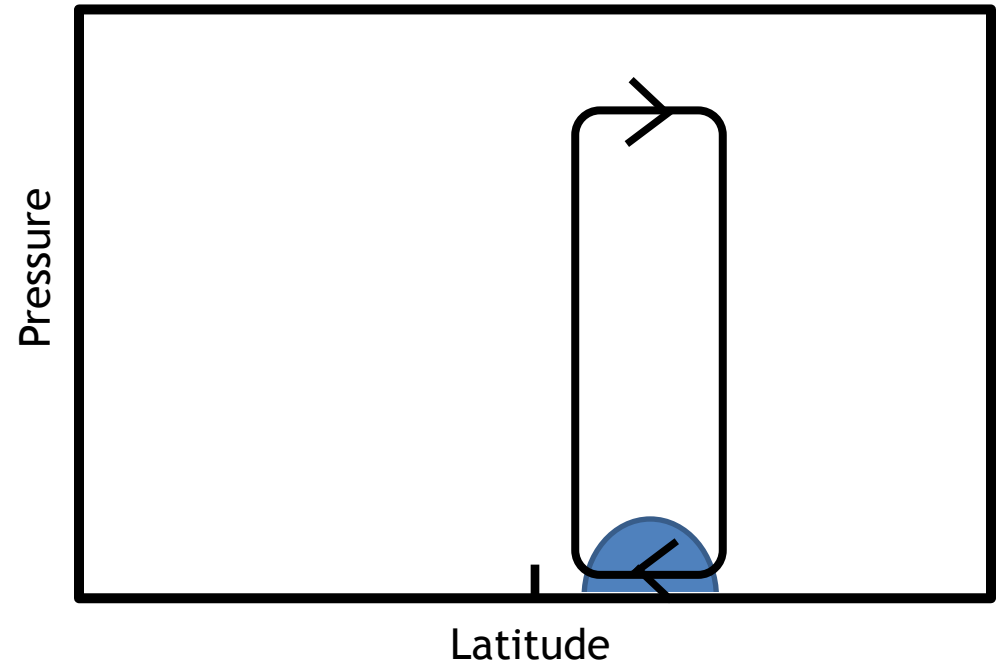
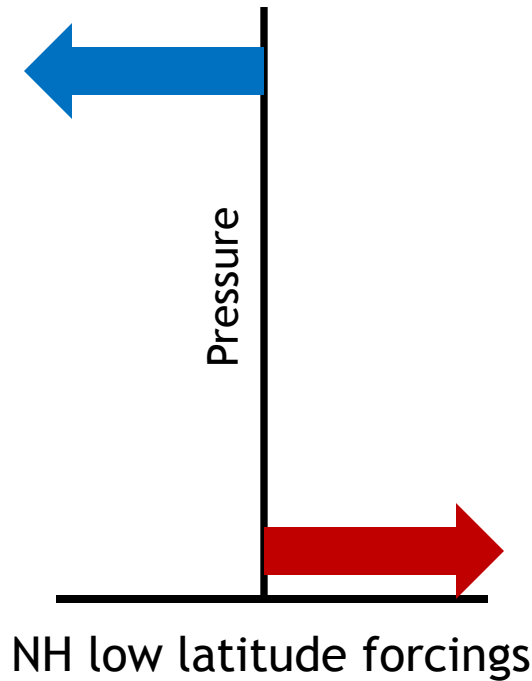
(Forecast)

They are consistent with the missing westerly forcing being in the lower troposphere

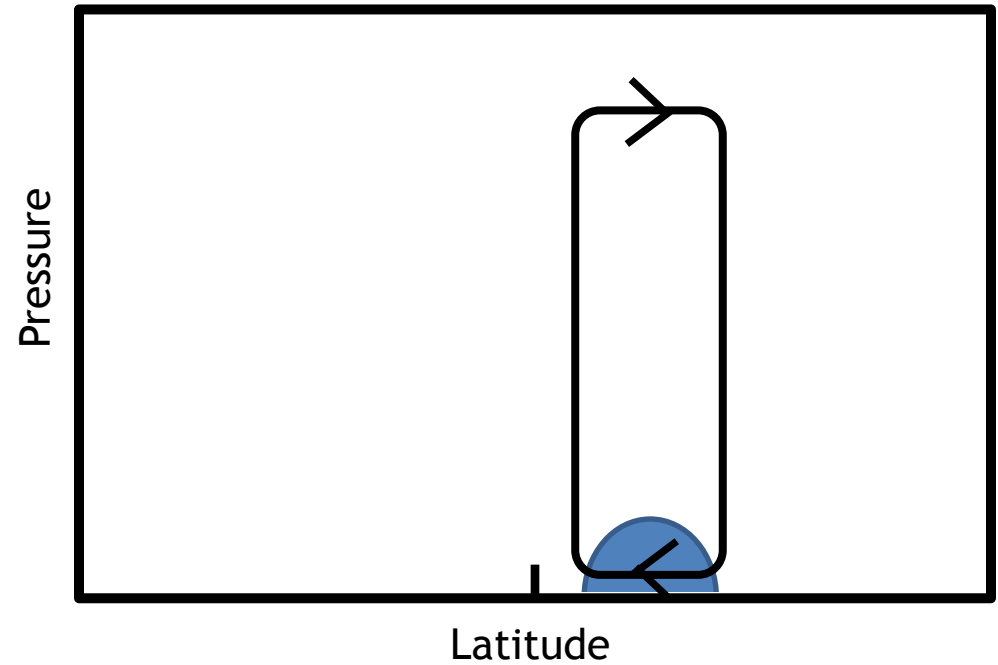
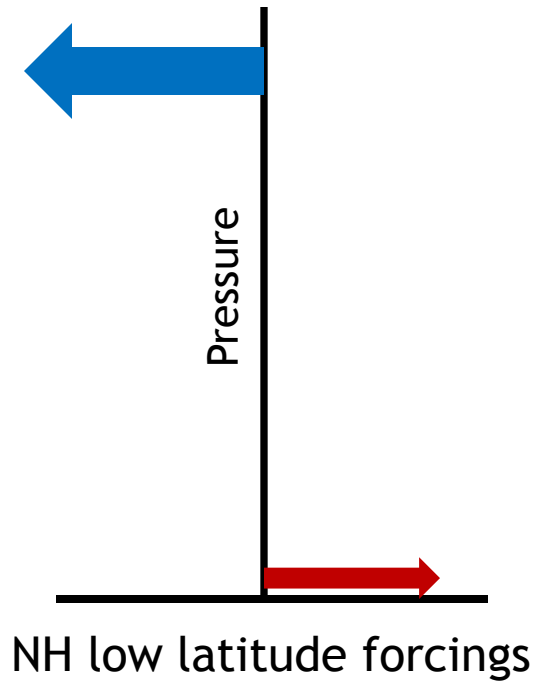


What you'd expect in the absence of a westerly forcing in the lower troposphere

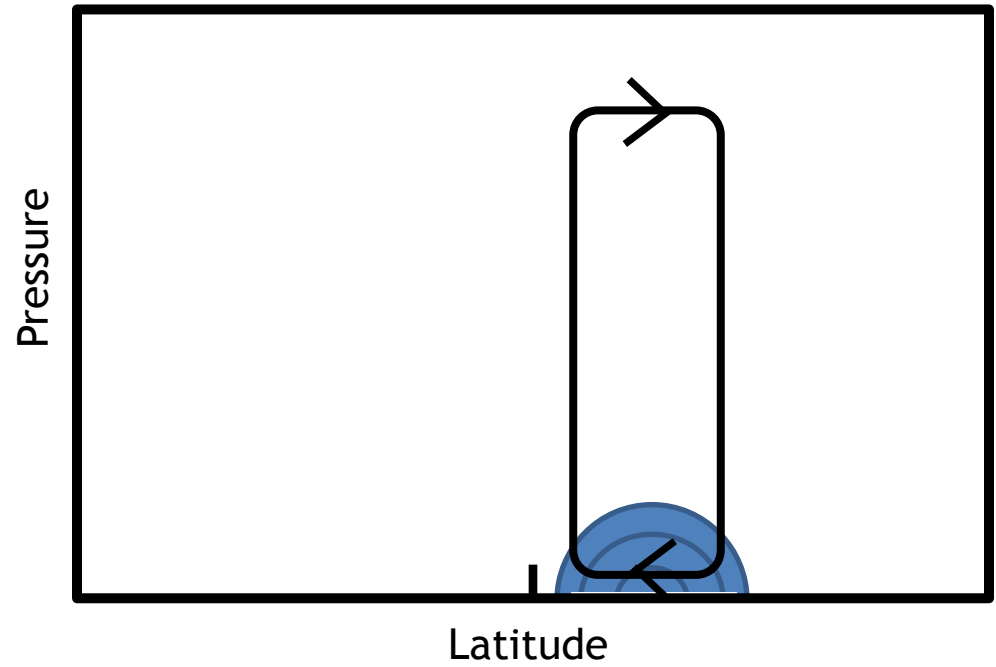
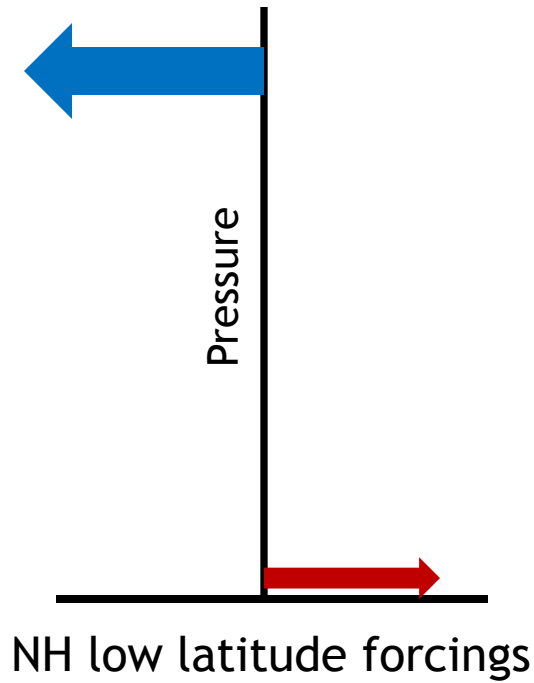
# Schematic depiction of the influence of a missing low level westerly tendency in the NH low latitudes



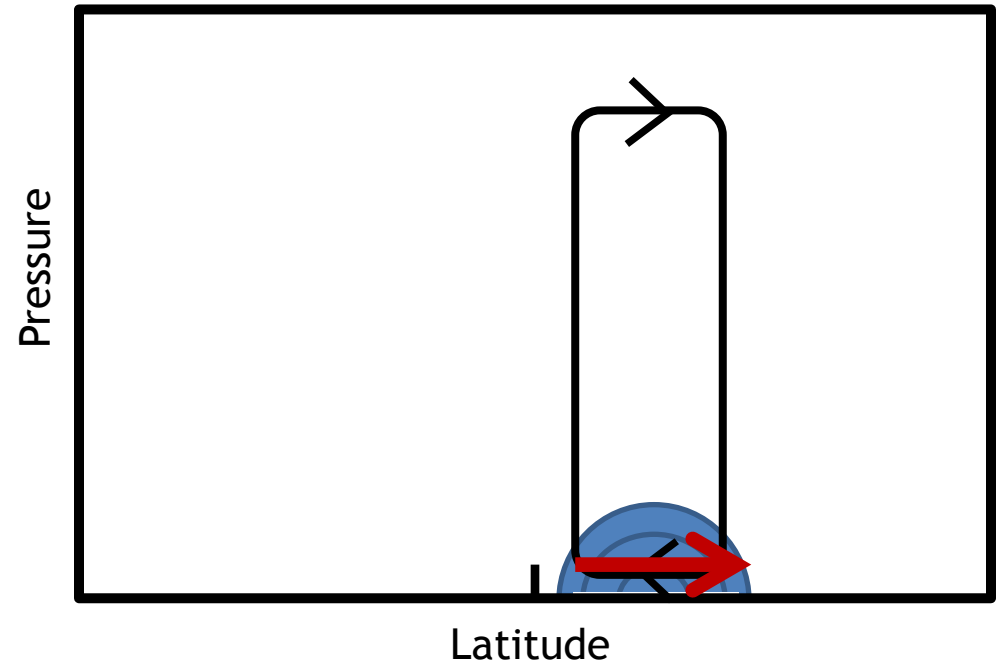
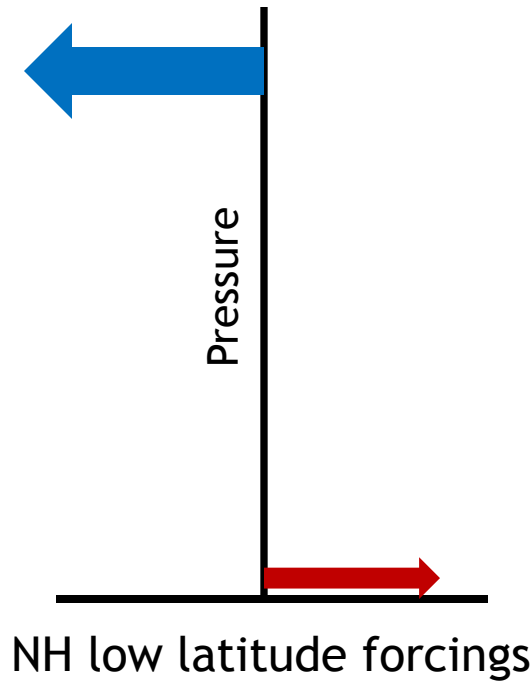
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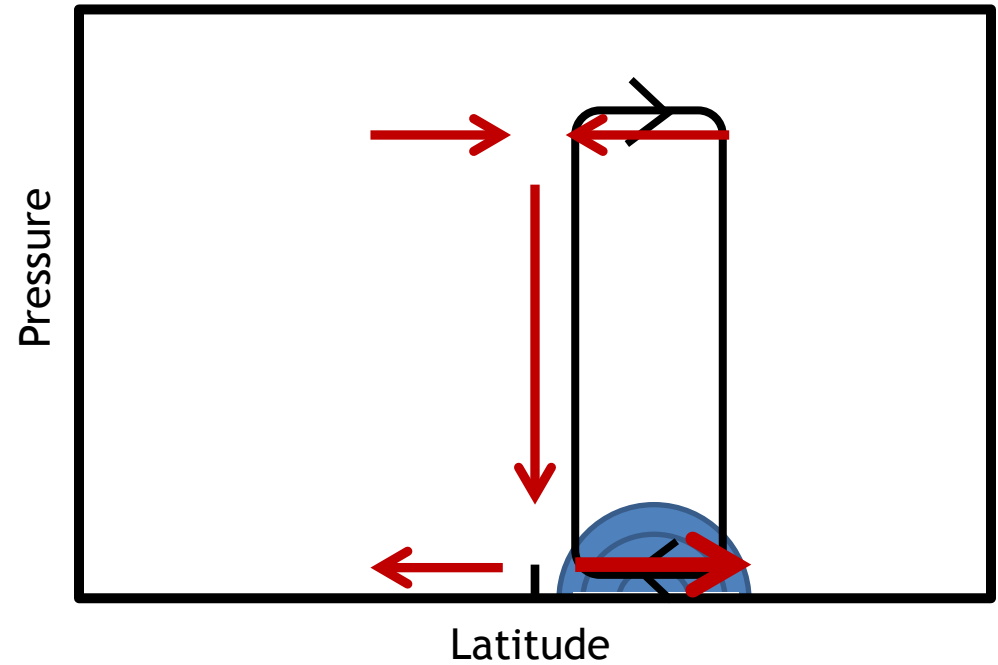
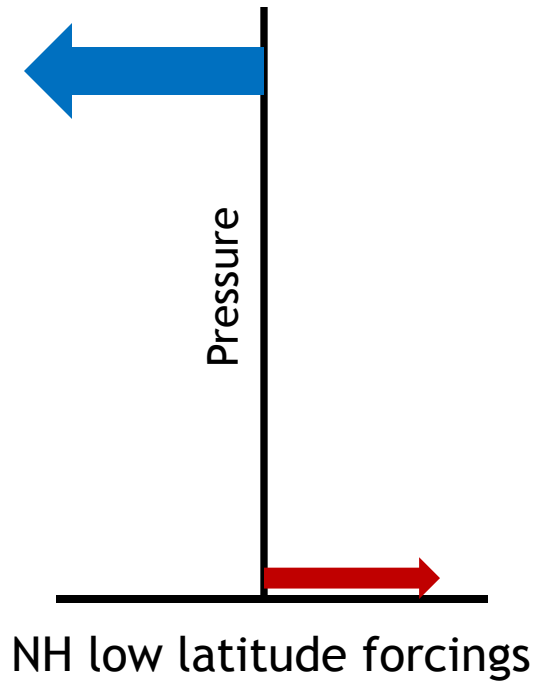


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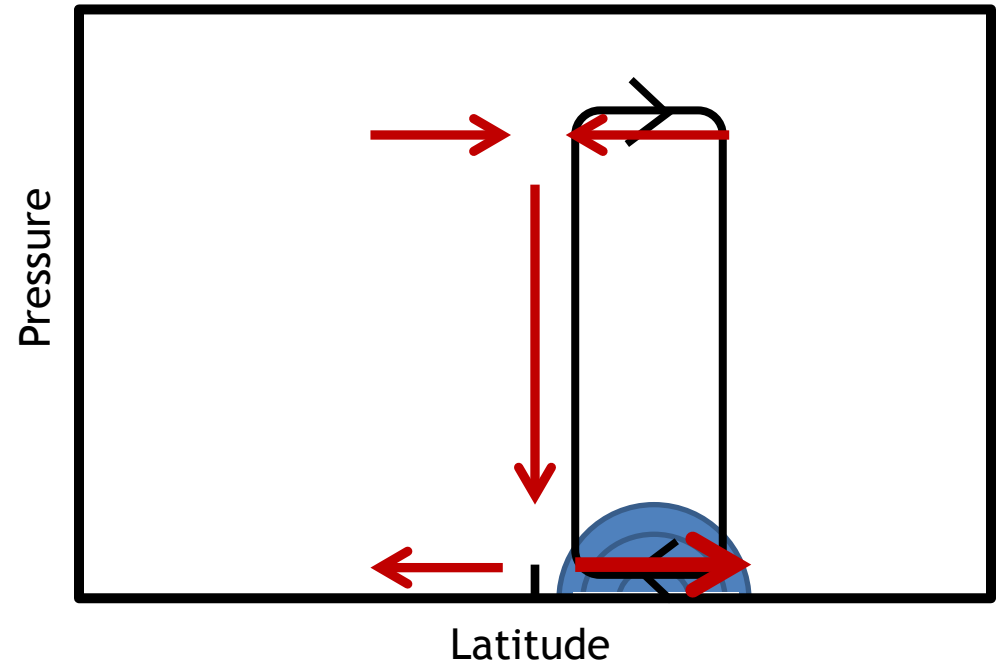
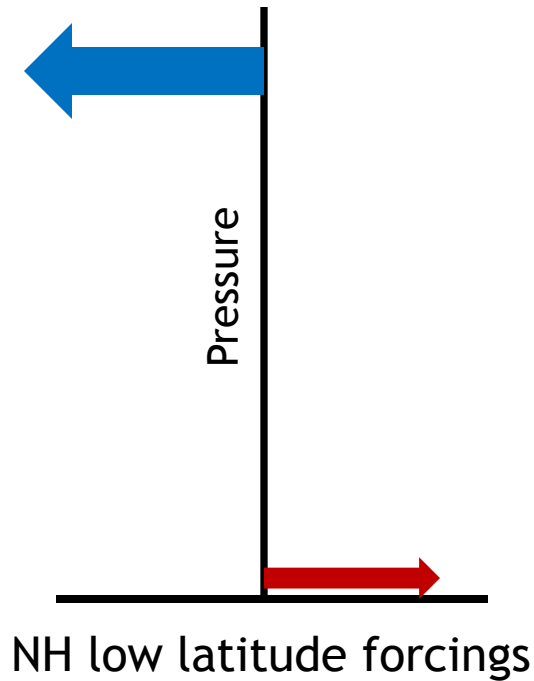




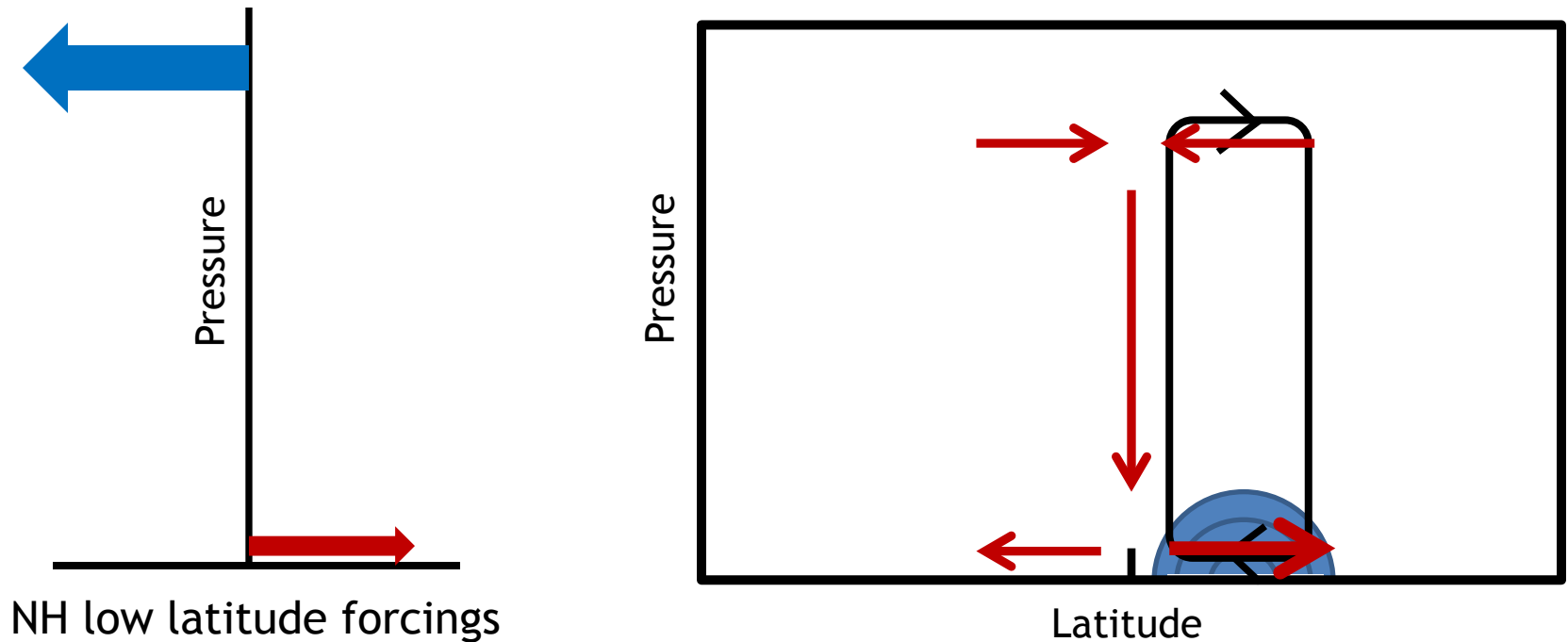
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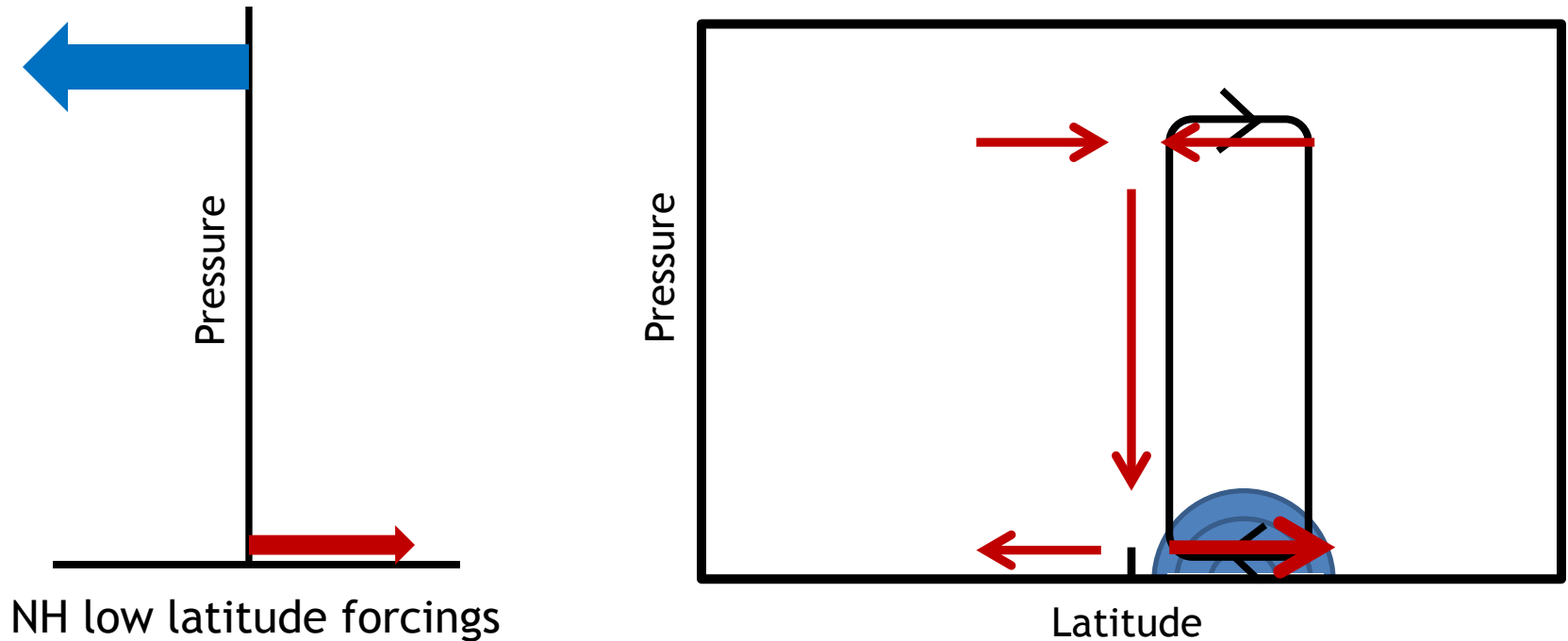


# Schematic depiction of the influence of a missing low level westerly tendency in the NH low latitudes



Analysis increments are needed to weaken the low level easterlies and strengthen the Hadley circulation again.

# Schematic depiction of the influence of a missing low level westerly tendency in the NH low latitudes



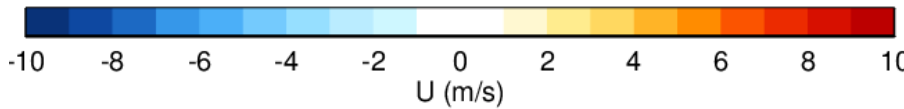
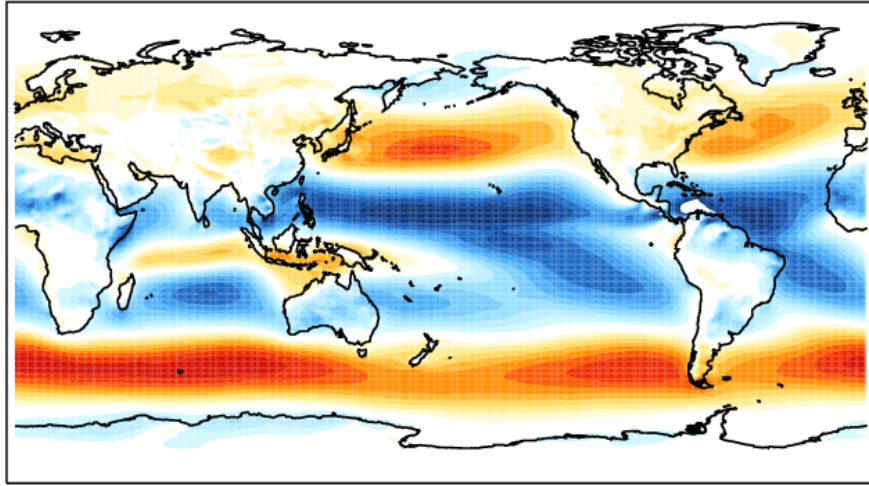
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# Lat-Lon structure of the analysis increments

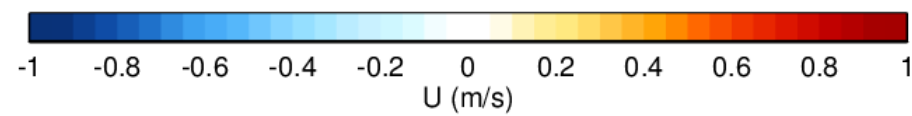
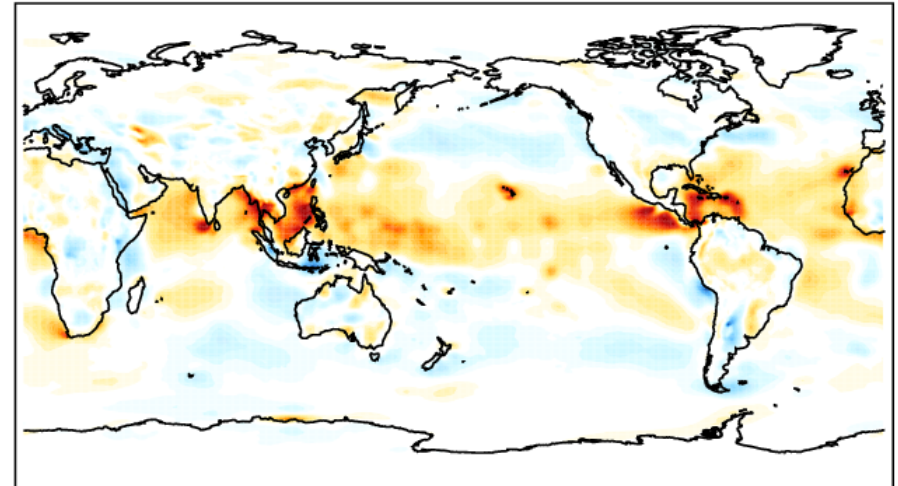
Is there something special about the NH low latitudes in winter?

Assimilation acts to reduce the easterly winds in the NH low latitudes almost everywhere. Perhaps more so in regions with observations

950hPa U, DJF, Analysis

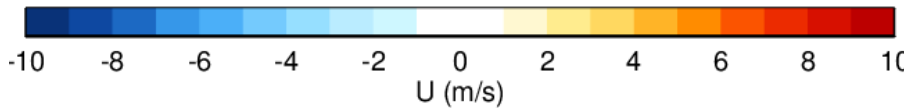
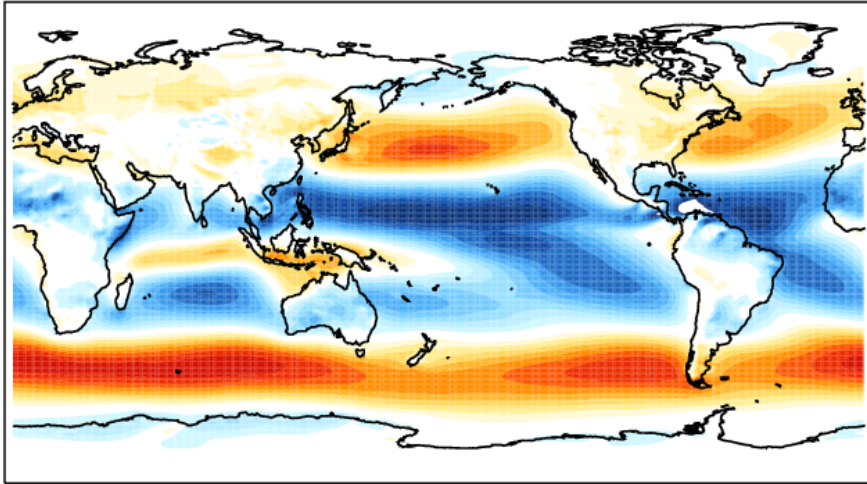


950hPa U, DJF, Analysis - Forecast

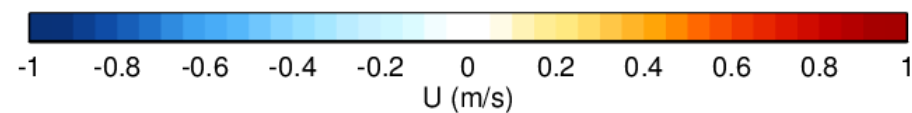
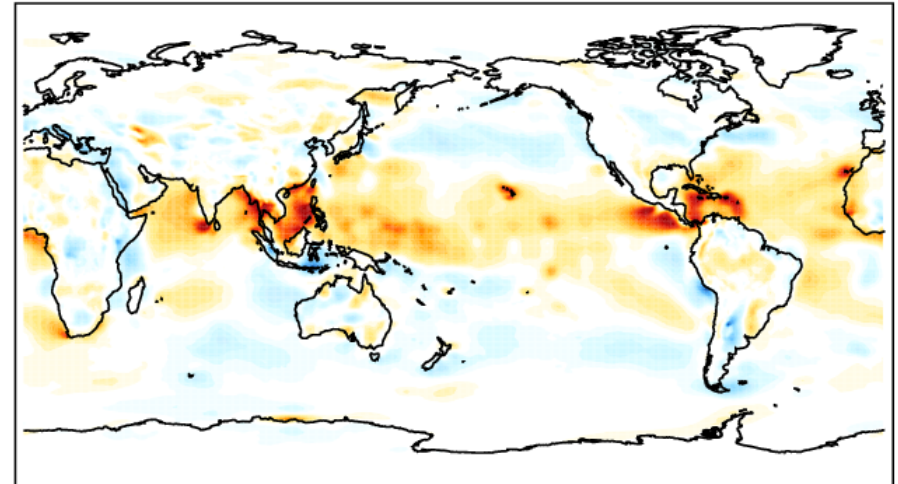


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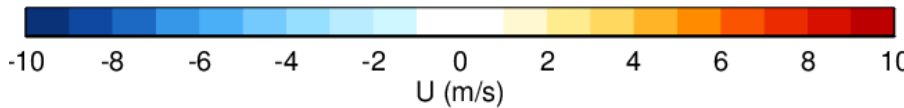
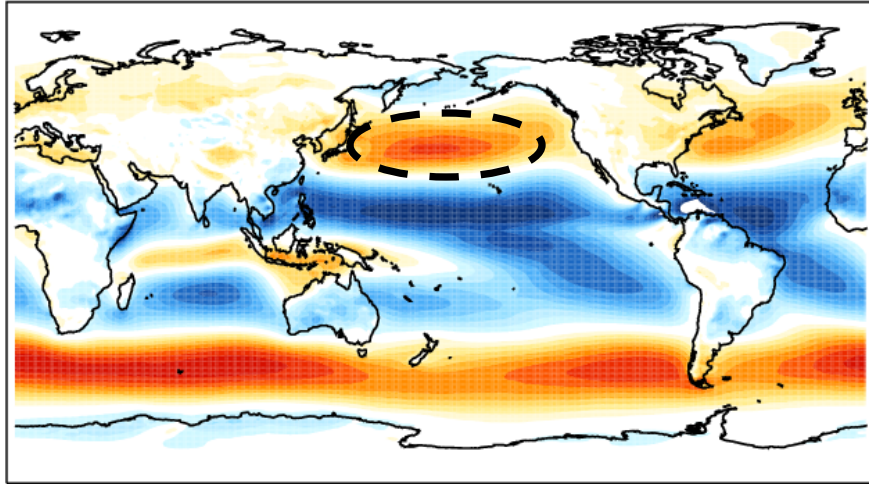
950hPa U, DJF, Analysis - Forecast



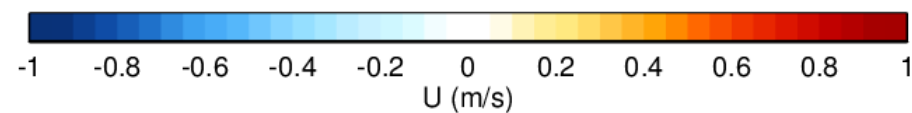
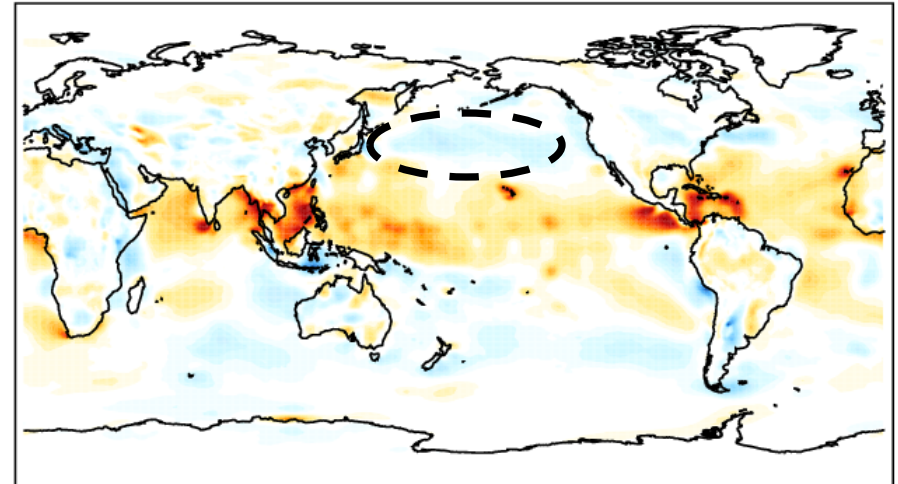
Also a general tendency to oppose the climatological winds in other regions.

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950hPa U, DJF, Analysis



950hPa U, DJF, Analysis - Forecast

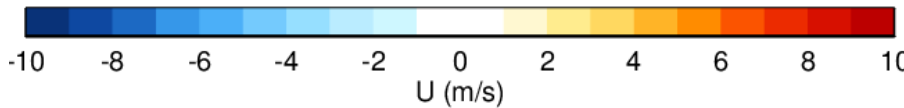
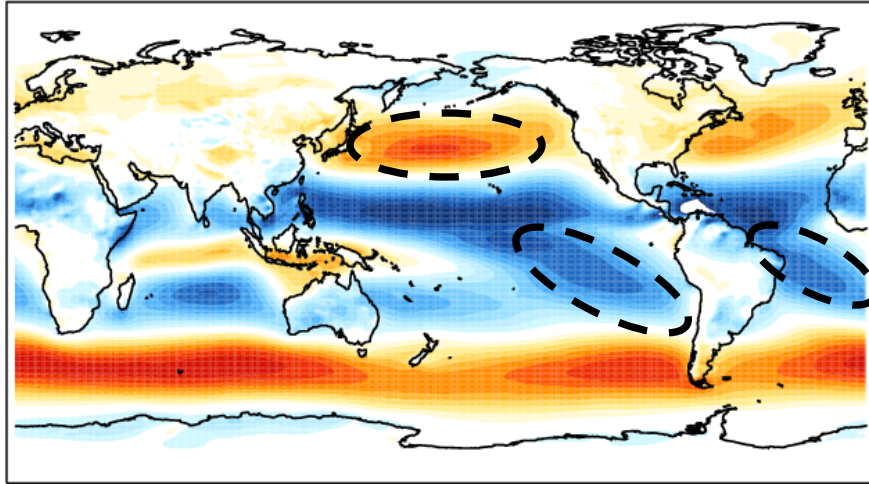


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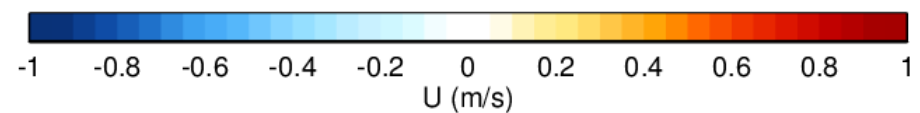
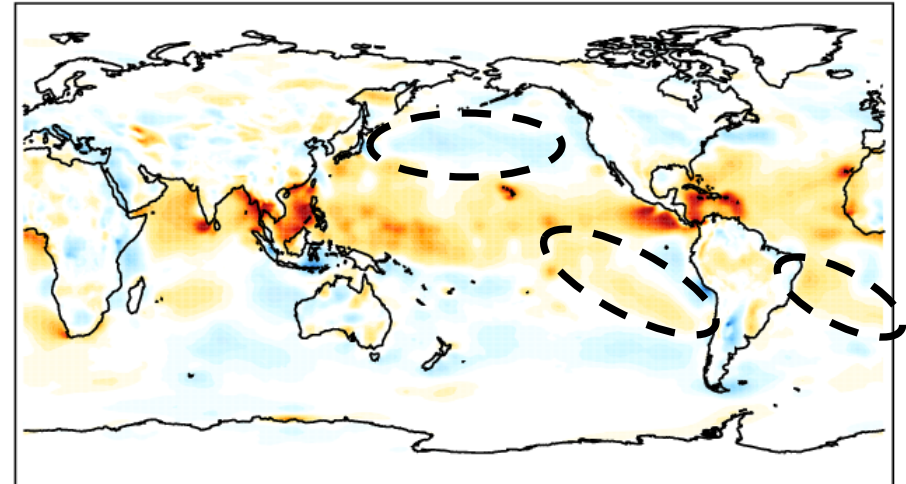


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950hPa U, DJF, Analysis



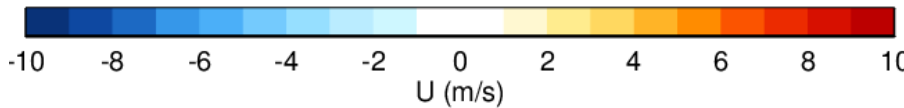
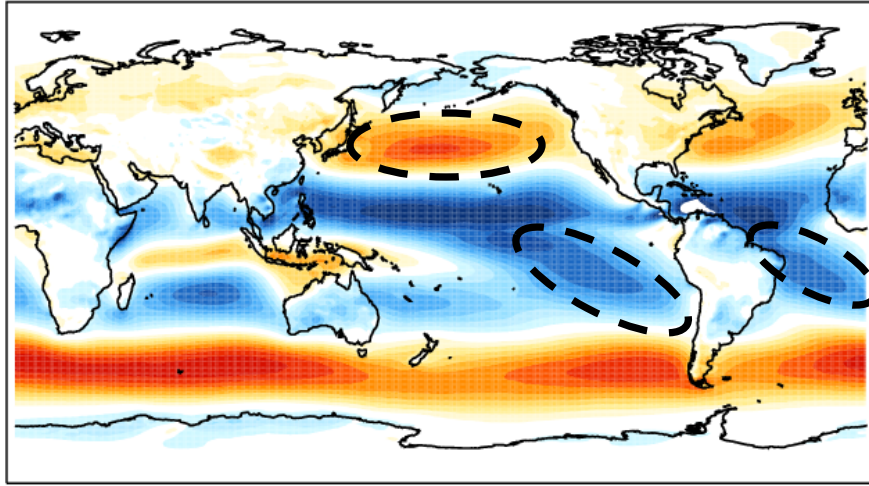
950hPa U, DJF, Analysis - Forecast



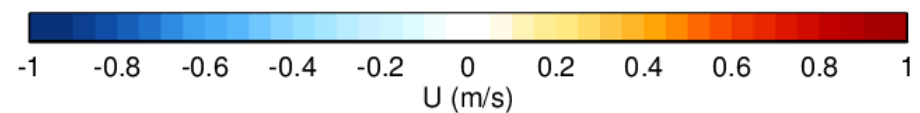
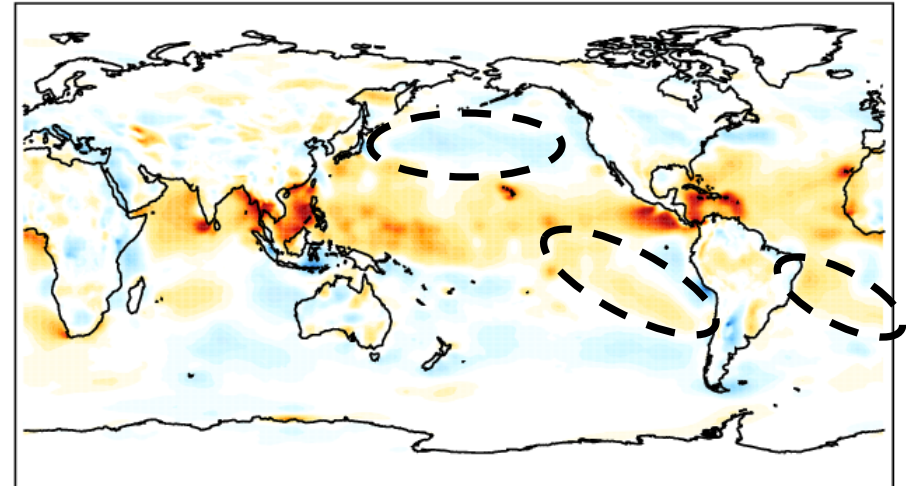
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950hPa U, DJF, Analysis



950hPa U, DJF, Analysis - Forecast

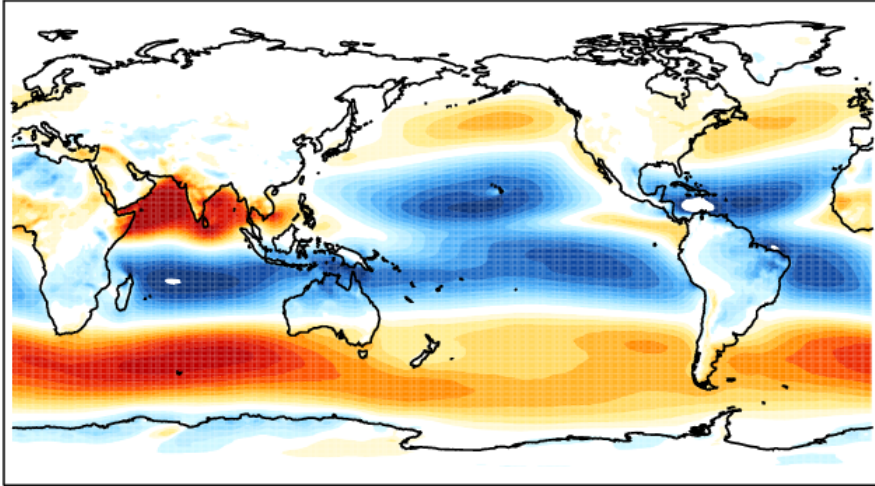


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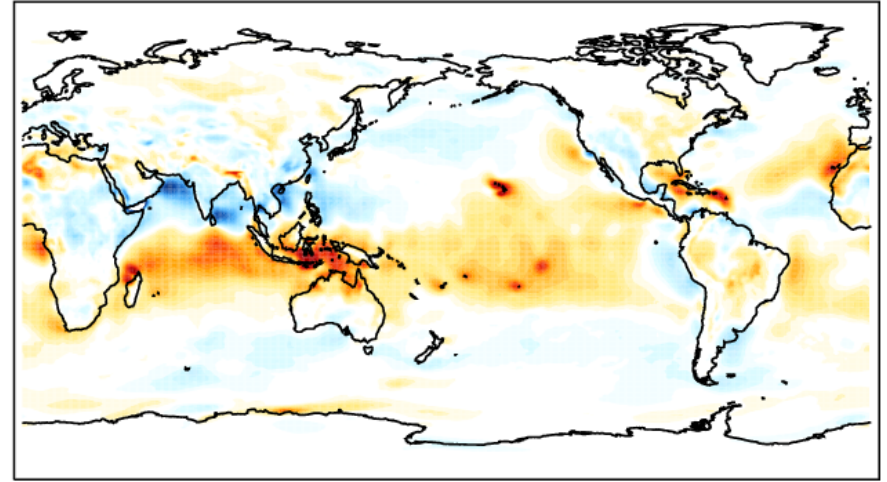
But not in the SH higher latitudes, maybe a lack of observations?

# What about in JJA?

950hPa U, JJA, Analysis

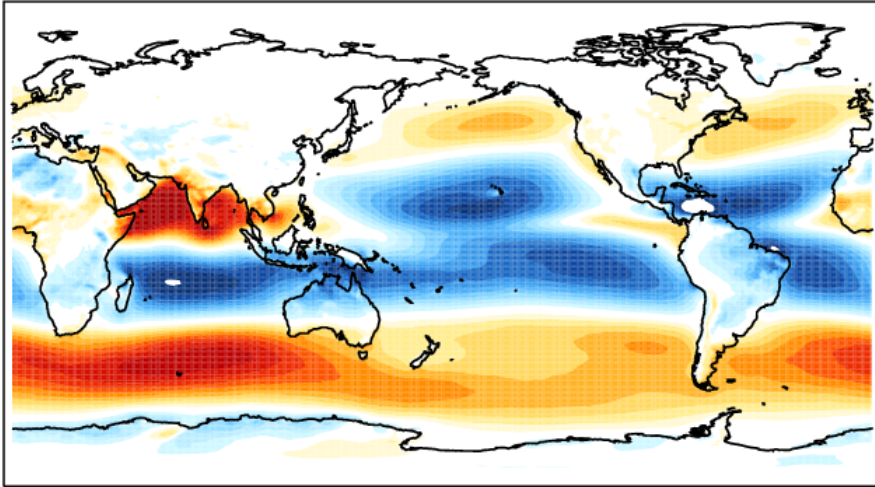


950hPa U, JJA, Analysis - Forecast

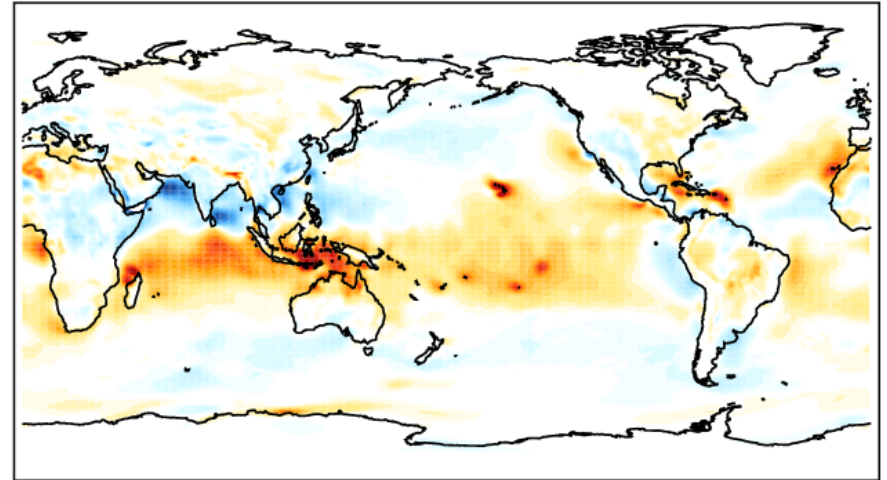


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950hPa U, JJA, Analysis



950hPa U, JJA, Analysis - Forecast

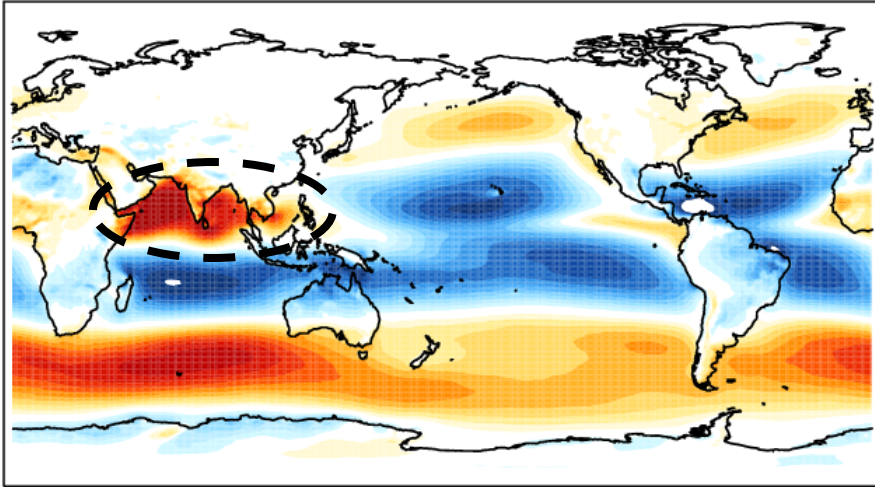


Less zonal symmetry in the NH low latitudes, but still a tendency for the increments to oppose the climatological flow.

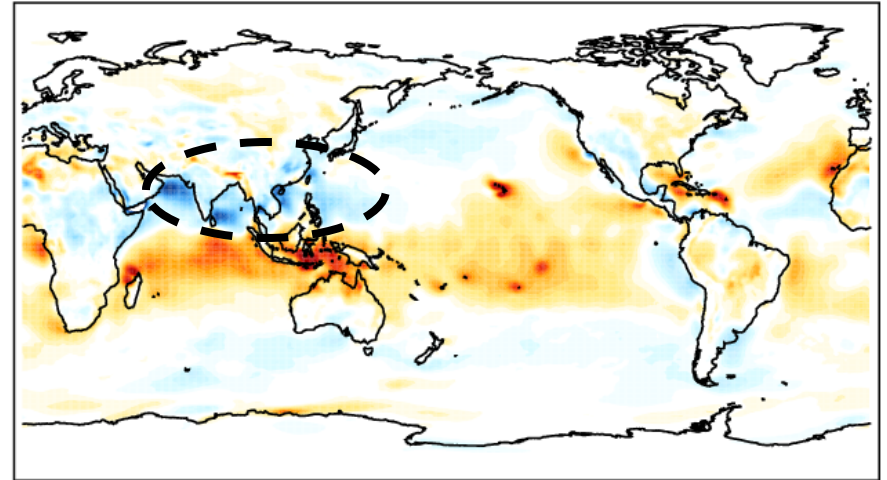


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950hPa U, JJA, Analysis



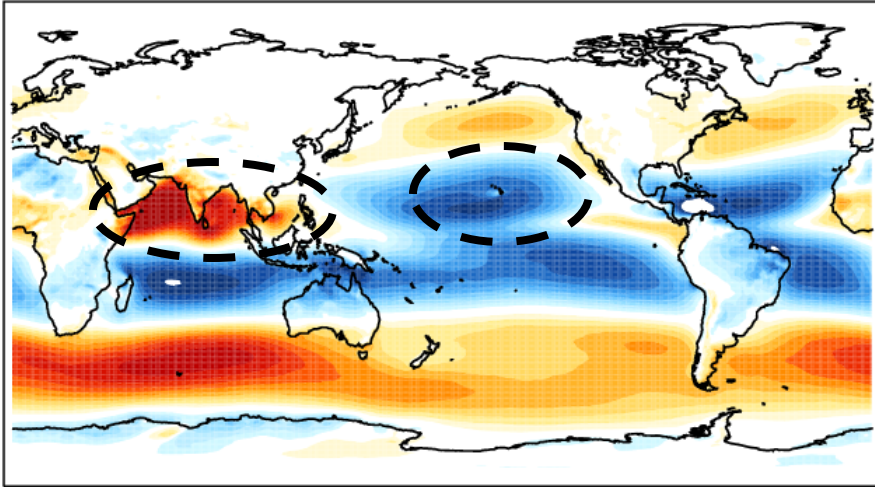
950hPa U, JJA, Analysis - Forecast



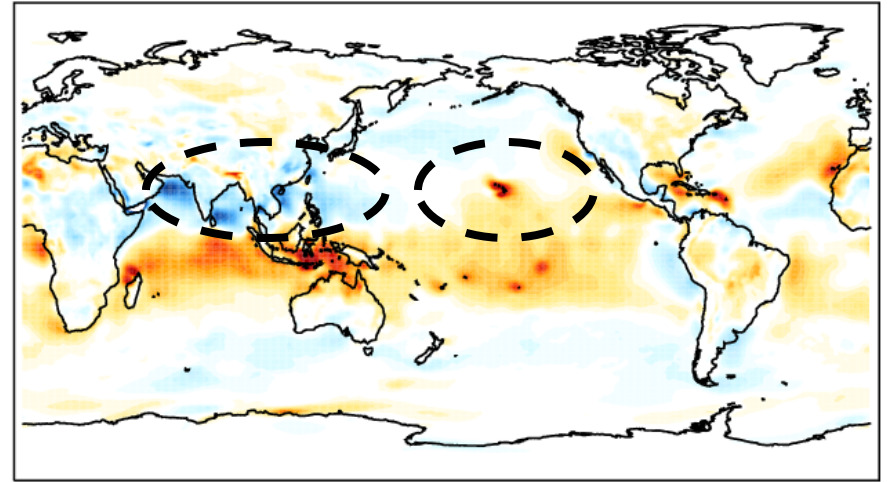
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950hPa U, JJA, Analysis



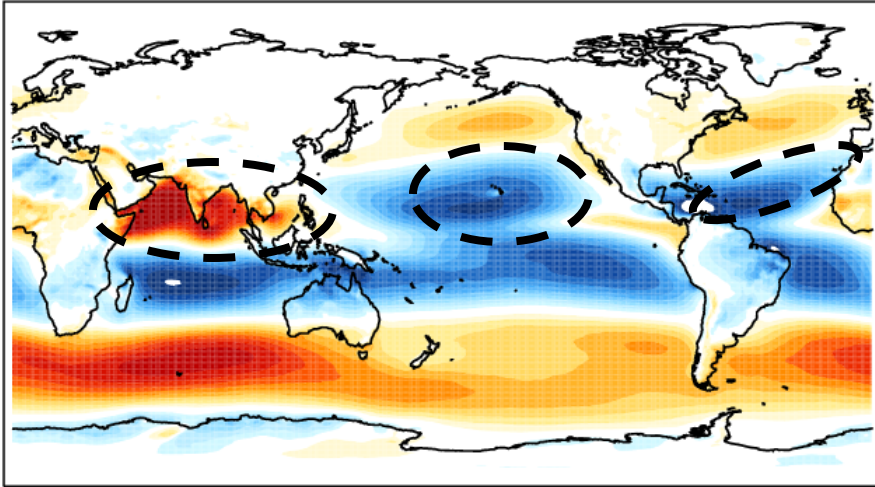
950hPa U, JJA, Analysis - Forecast



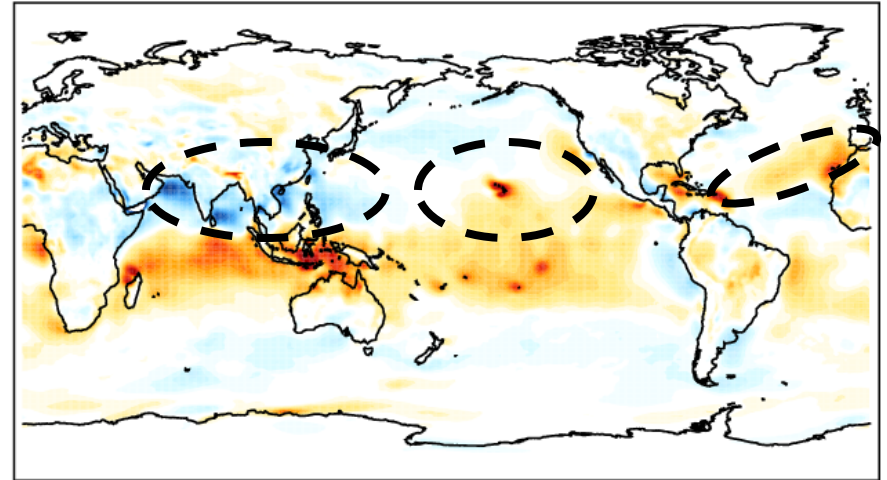
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950hPa U, JJA, Analysis



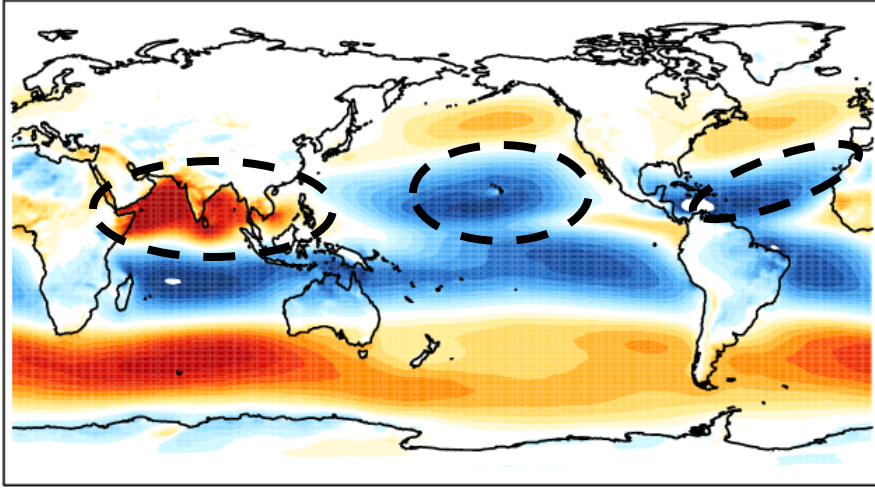
950hPa U, JJA, Analysis - Forecast



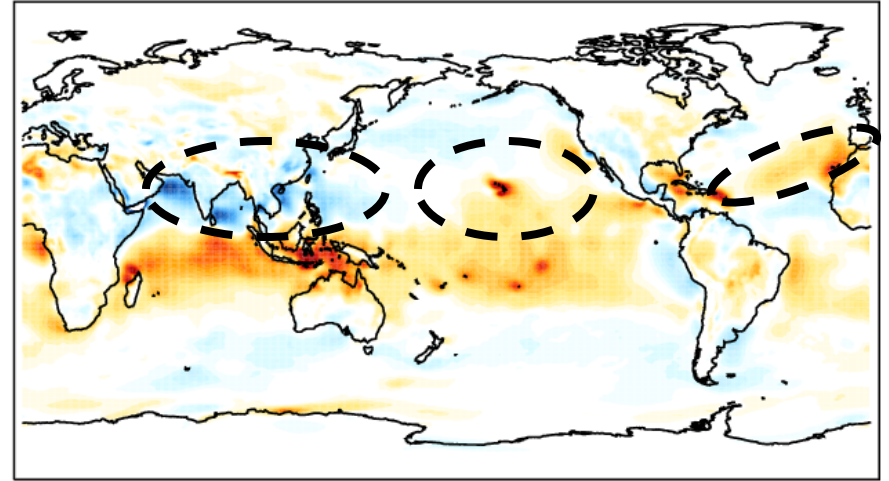
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# What about in JJA?

950hPa U, JJA, Analysis



950hPa U, JJA, Analysis - Forecast



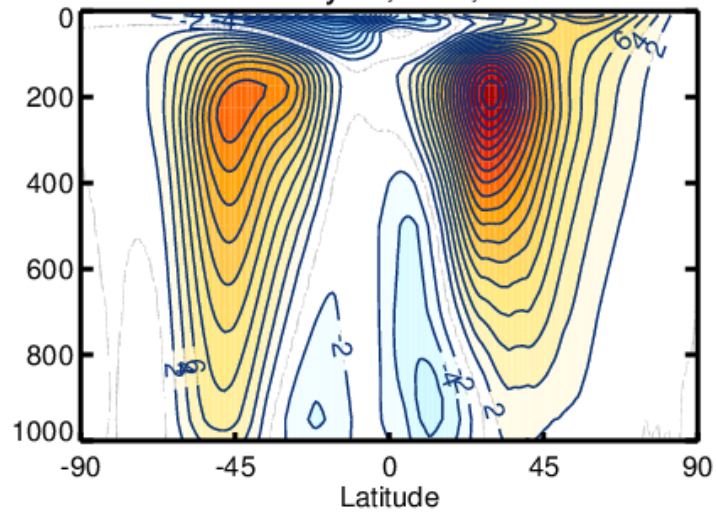
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Increments oppose the SH zonally symmetric low latitude easterlies.

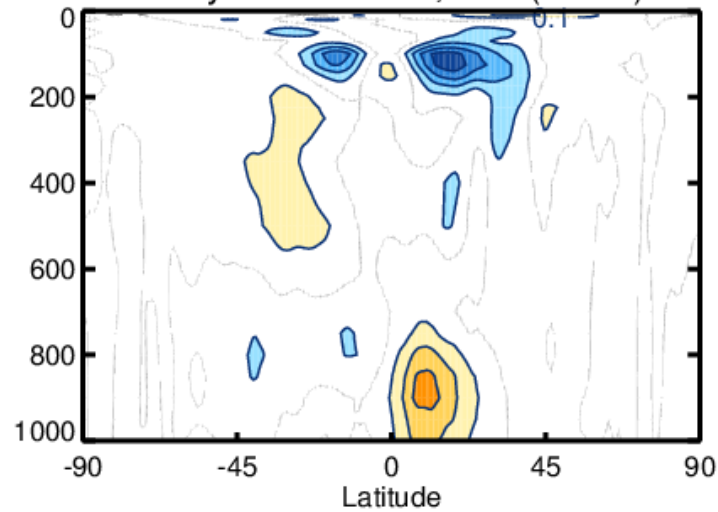


DJF

U analysis, DJF, ci=2

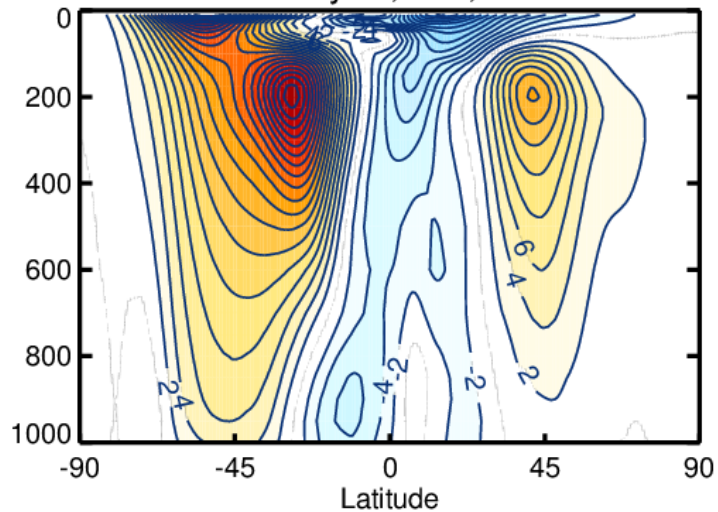


Analysis - Forecast, DJF (ci=0.1)

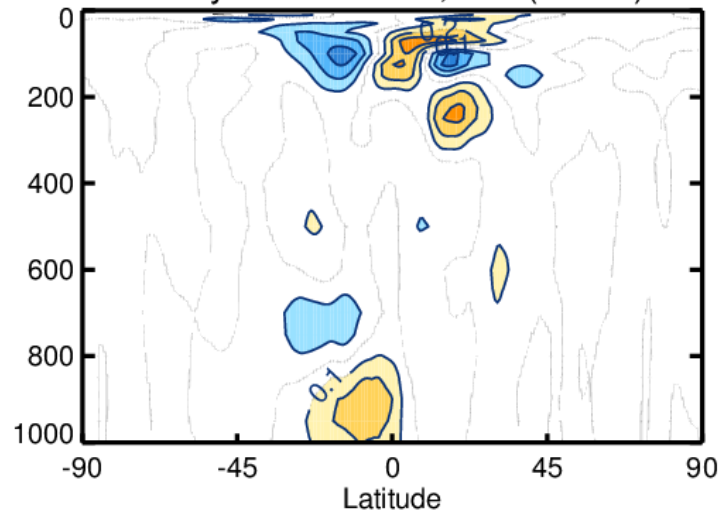


JJA

U analysis, JJA, ci=2



Analysis - Forecast, JJA (ci=0.1)



# Lat-Lon structure of the analysis increments

Is there something special about the NH low latitudes in winter?

No, the increments act to oppose the low level flow in general.

# Two Possibilities?

(1) An incorrect formulation of the surface drag. Should have a stronger surface drag for a given low level flow.

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**BUT**

This would mean that the surface drag output from the reanalysis is incorrect. It should be more easterly in the NH low latitudes.

# Two Possibilities?

(1) An incorrect formulation of the surface drag. Should have a stronger surface drag for a given low level flow.

The increments would no longer be needed to reduce the strength of the low level easterlies. The drag would do it.

The budget would add up because the surface stress obtained with the reanalysis low level winds would be greater

**BUT**

This would mean that the surface drag output from the reanalysis is incorrect. It should be more easterly in the NH low latitudes.

The surface drag in the CMIP models would be more correct, but they're getting it for the wrong reasons. They're getting it with a low level flow that's too strong.

# Two Possibilities?

(2) We are missing some other physics near the surface that should act to decelerate the flow, maybe some kind of horizontal diffusive process?



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We're just compensating for this missing process with the analysis increments.

In that case, both the near surface winds and the surface drag in the CMIP models would be incorrect.

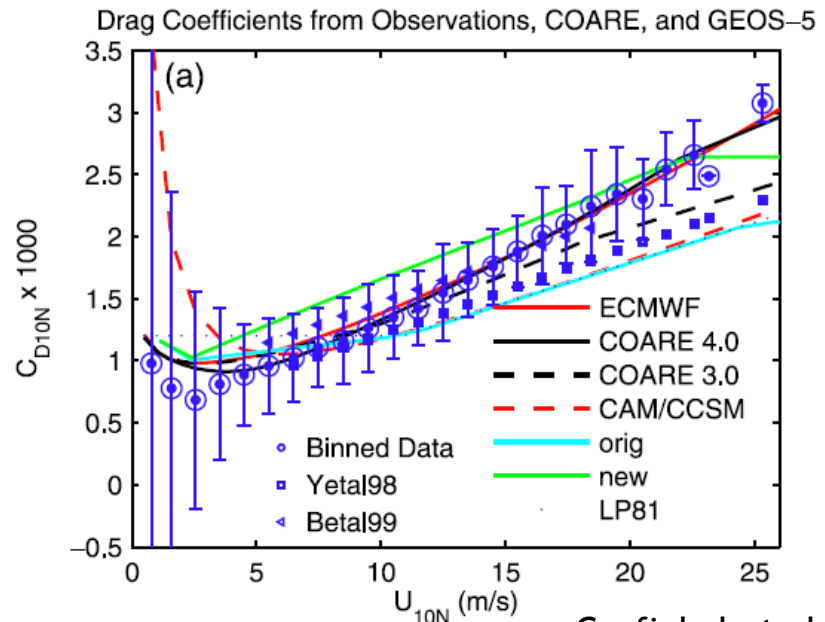
All (?) global estimates of surface stress rely on assumptions about the drag coefficient.

$$\tau = \rho C_D \vec{v}_{10} |\vec{v}_{10}|$$

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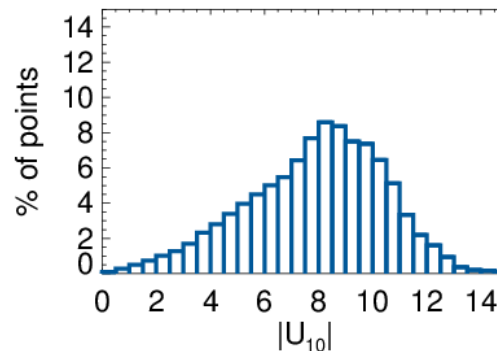
$$\tau = \rho C_D \vec{v}_{10} |\vec{v}_{10}|$$

How confident are we in the drag coefficient?



Garfinkel et al (2011)

West Pacific



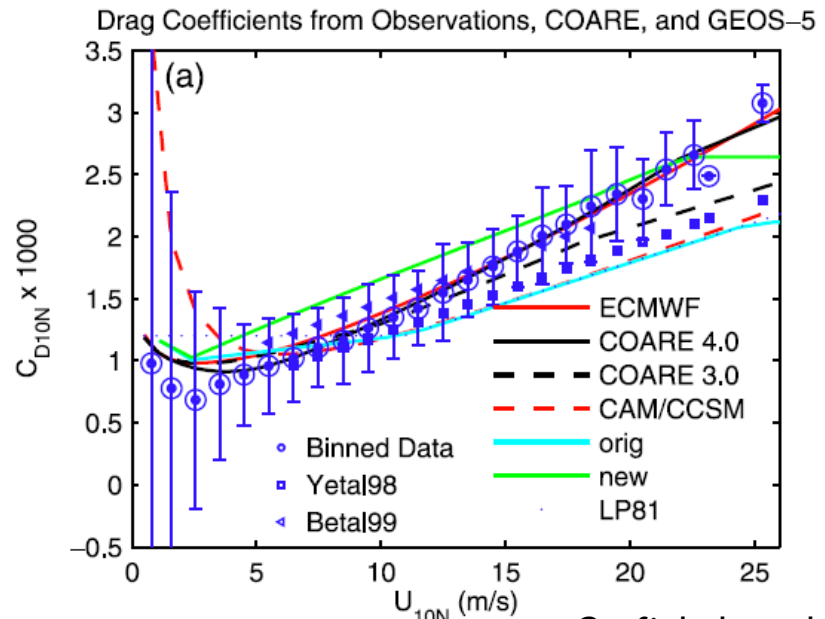
← Instantaneous 10m wind magnitudes

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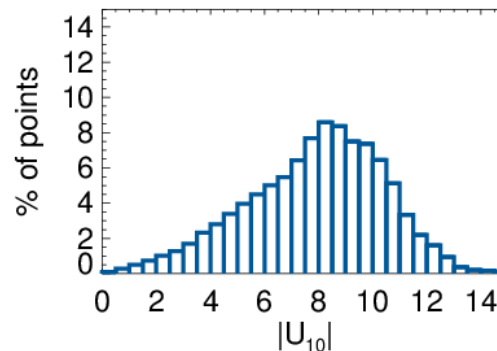
How confident are we in the drag coefficient?

Or do we need to explain the missing low level tendencies with some other physics?



Garfinkel et al (2011)

West Pacific



← Instantaneous 10m wind magnitudes

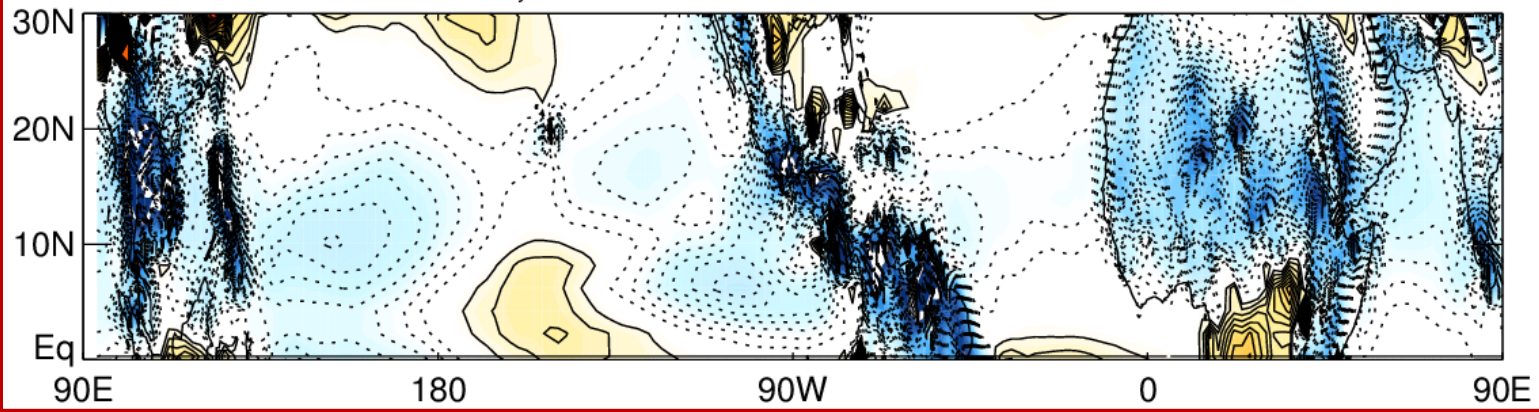
Thanks!





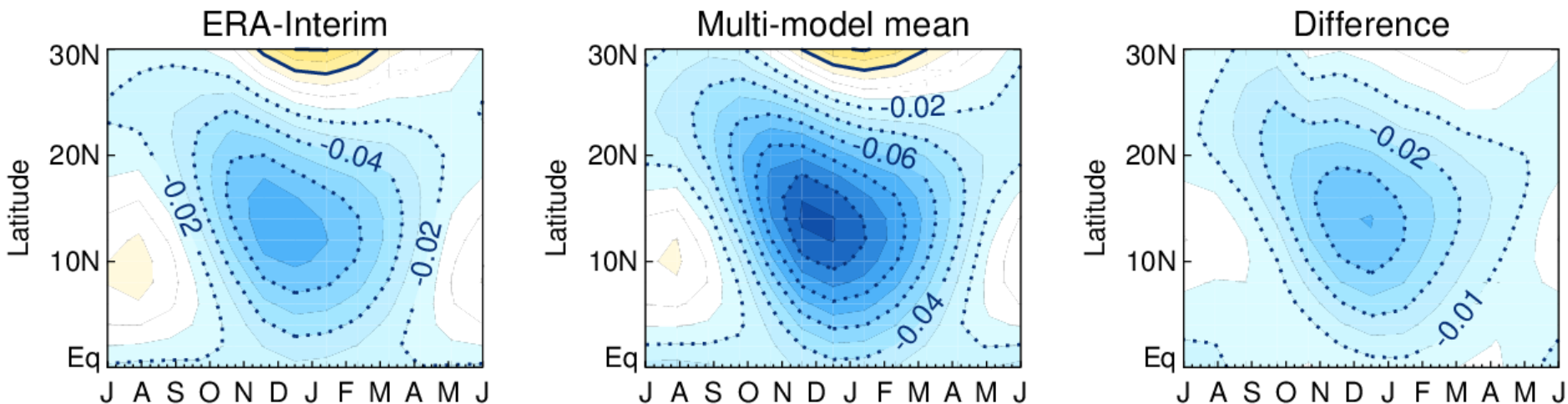
Extra Slides

# TAUX, Multimodel mean - ERA-Interim

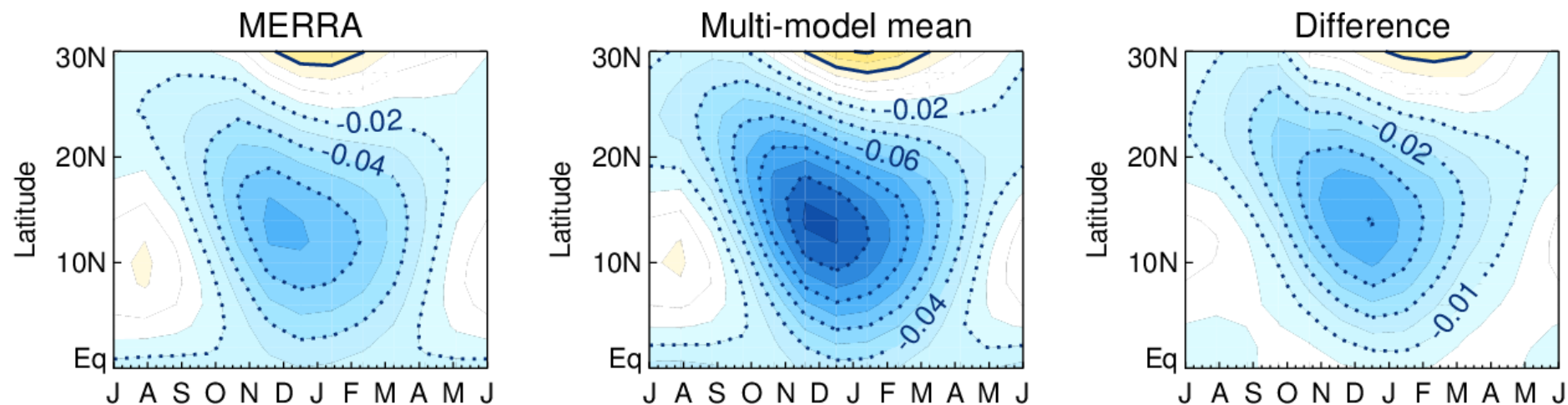


# Seasonal evolution of low latitude wind stress differences

## ERA-Interim vs multi-model mean

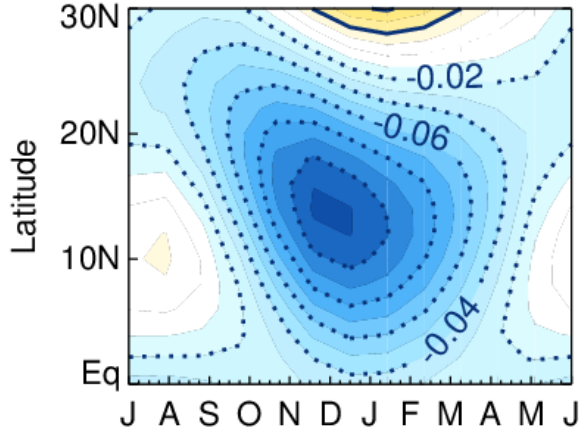


## MERRA vs multi-model mean

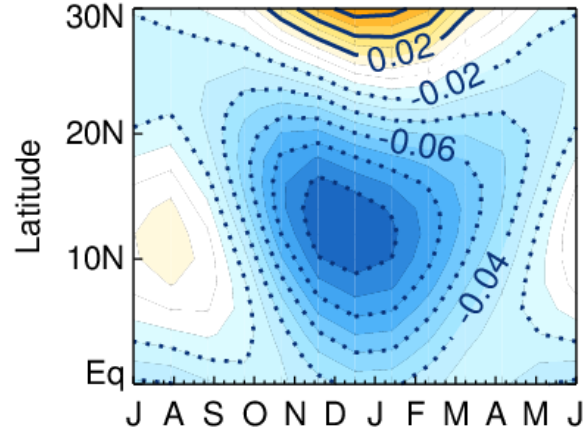


# CMIP5 momentum budget as a function of season

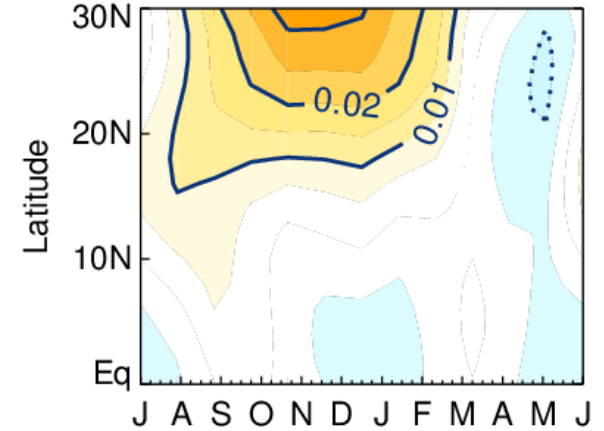
TAUX, CMIP5



RESOLVED, CMIP5

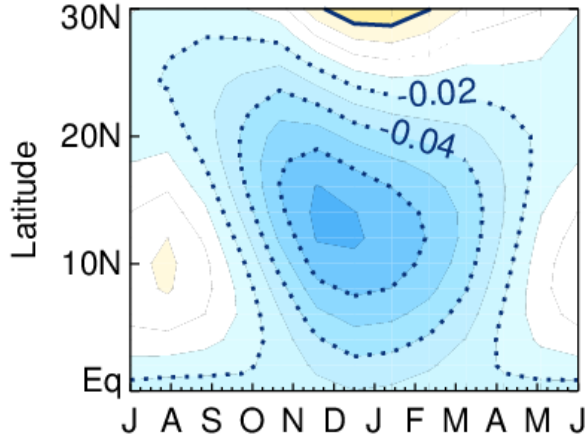


RESIDUAL, CMIP5

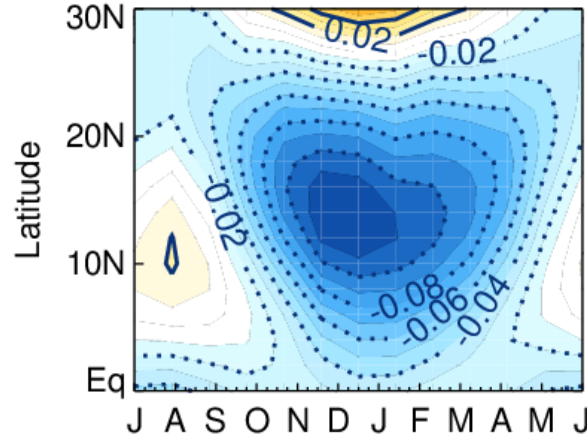


## MERRA Budget

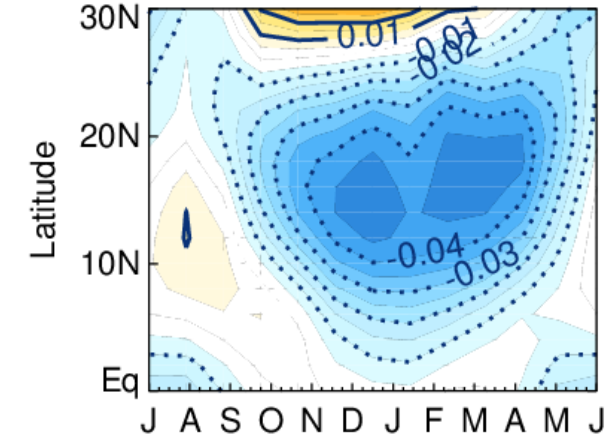
TAUX, MERRA



RESOLVED, MERRA



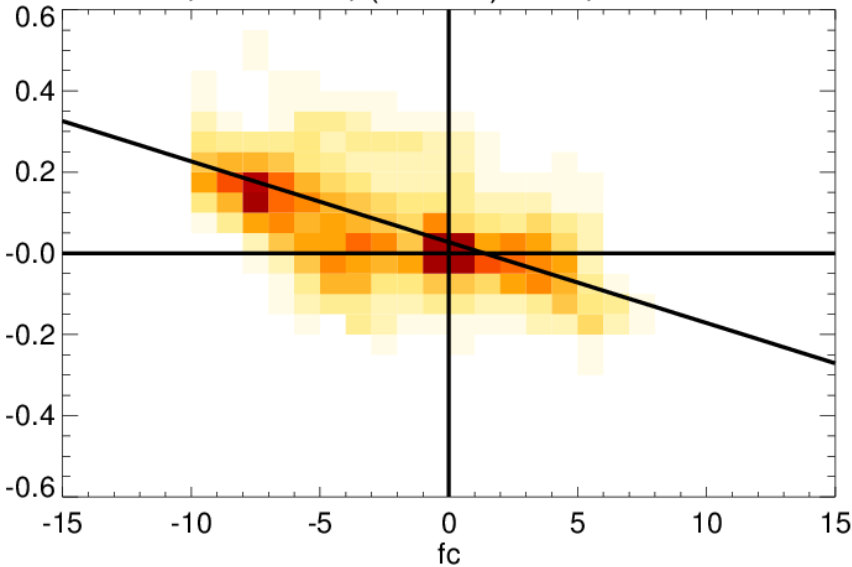
RESIDUAL, MERRA



# (Analysis - Forecast) vs Forecast Ocean points north of 30S, 950hPa

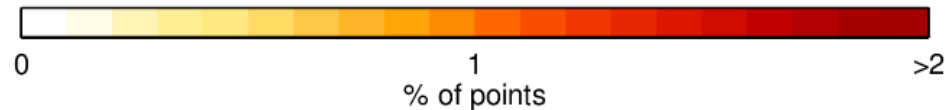
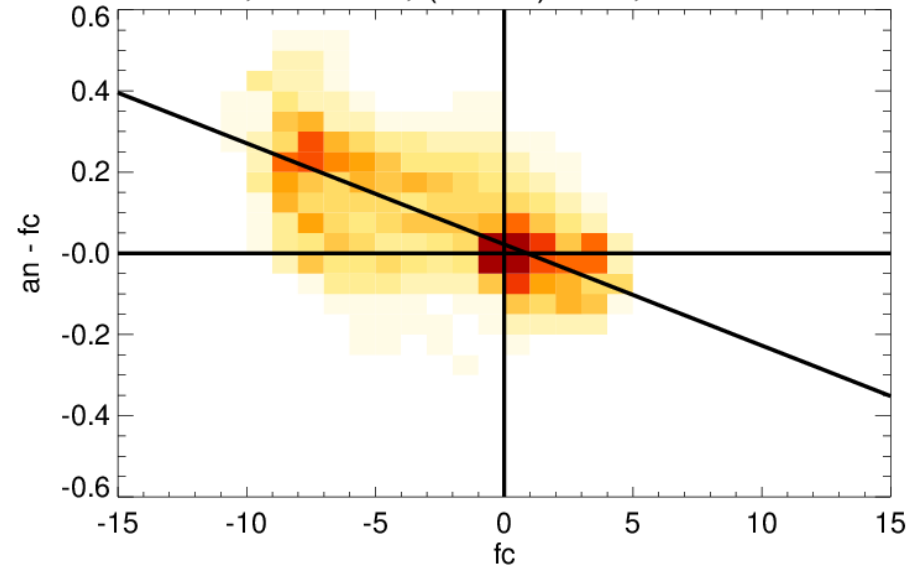
DJF

DJF, 30S-90N, (an - fc) vs fc, cor= -0.50



JJA

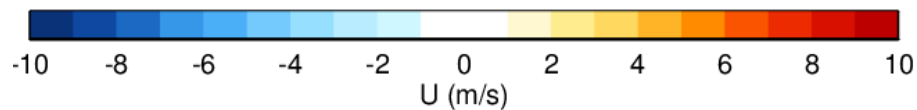
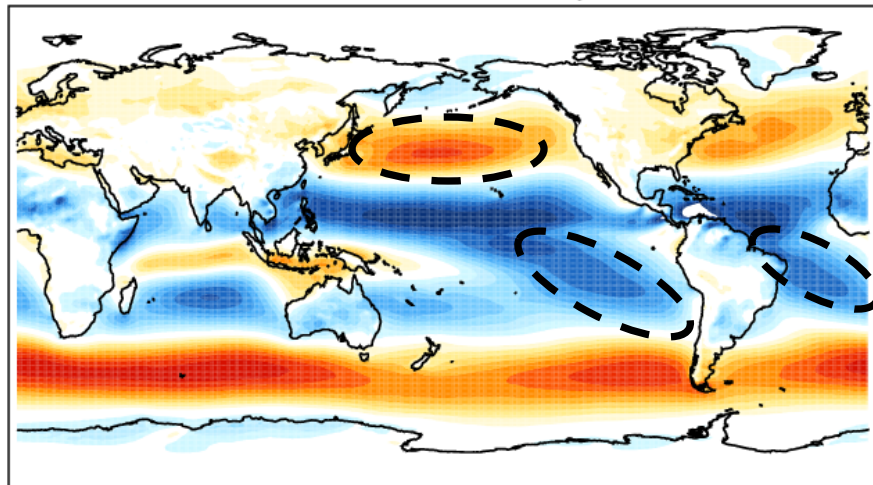
JJA, 30S-90N, (an - fc) vs fc, cor= -0.58



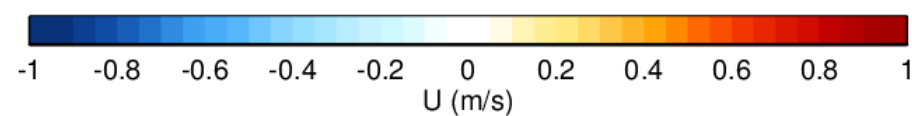
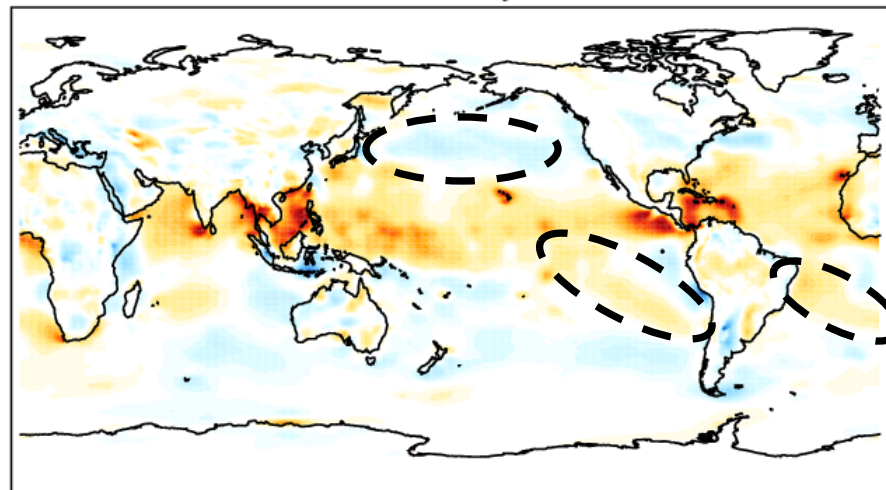
Negative correlation  $\rightarrow$  assimilation of observations acts to reduce the climatological low level winds.



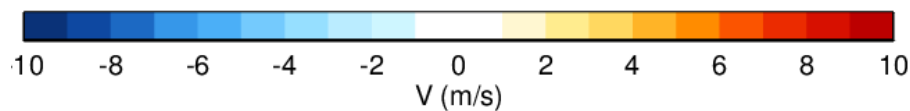
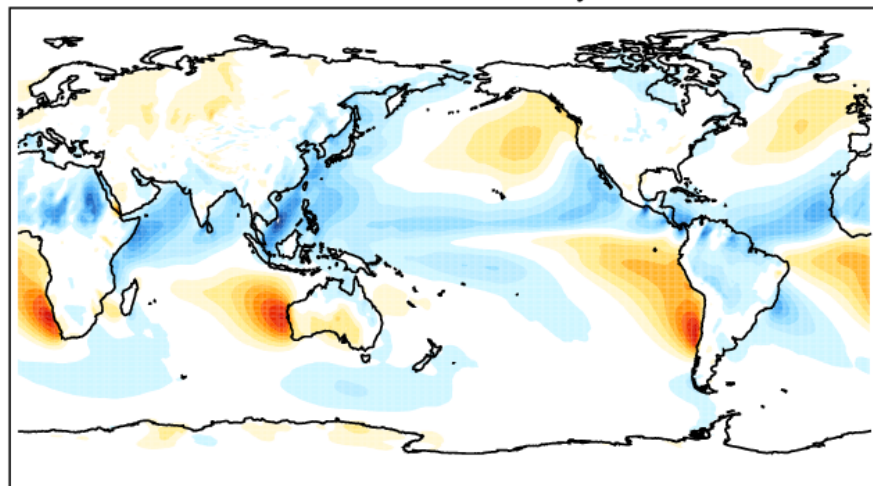
950hPa U, DJF, Analysis



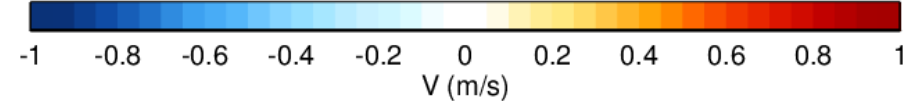
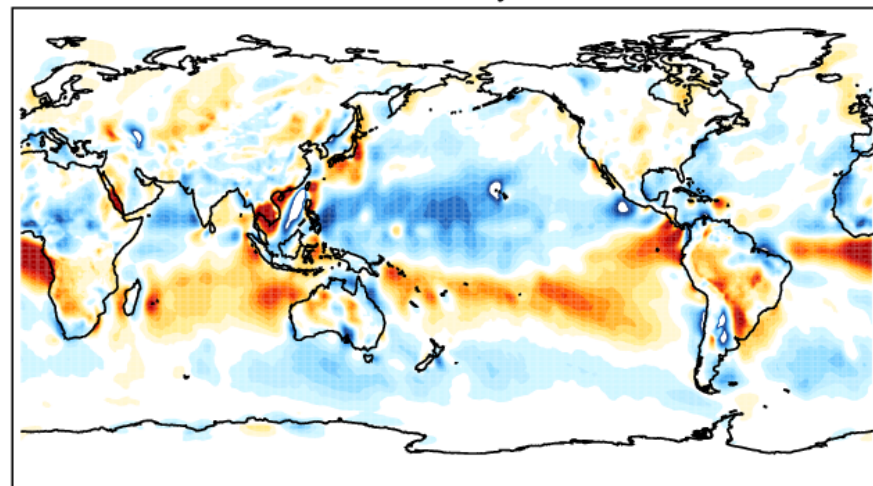
950hPa U, DJF, Analysis - Forecast



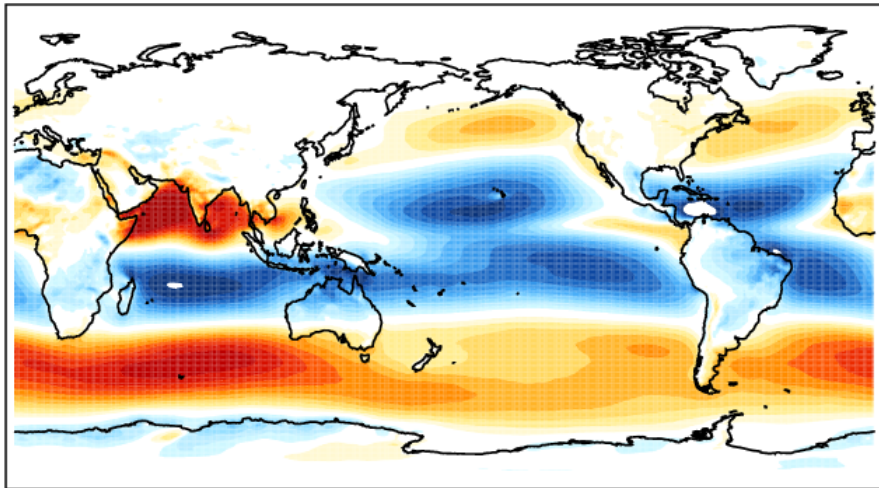
950hPa V, DJF, Analysis



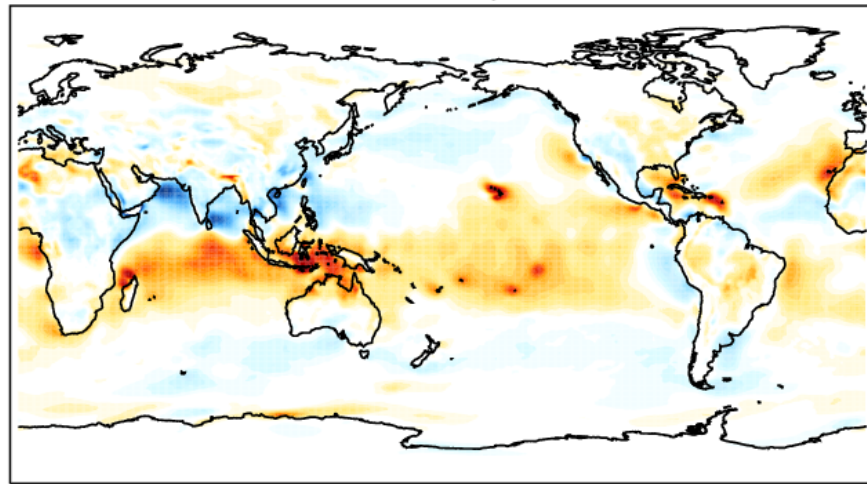
950hPa V, DJF, Analysis - Forecast



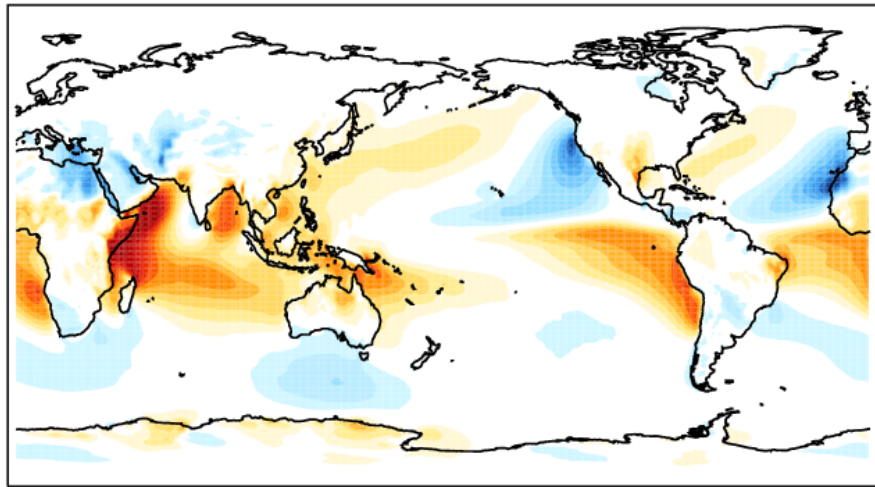
950hPa U, JJA, Analysis



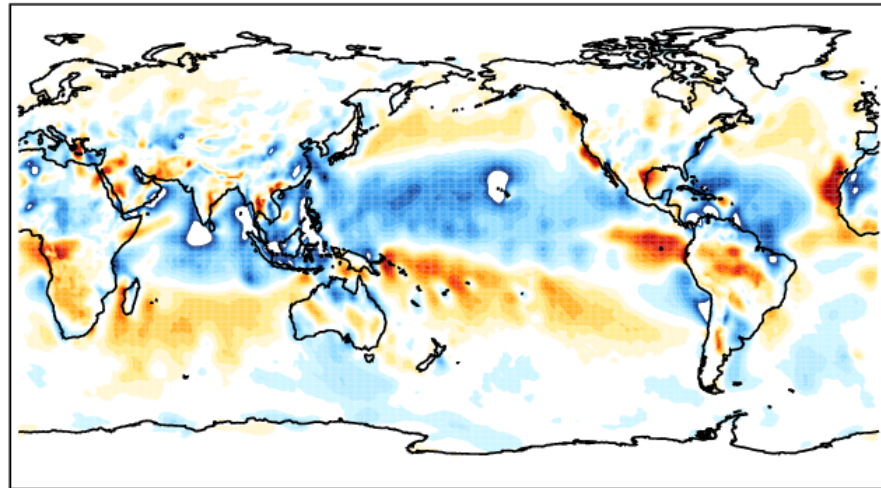
950hPa U, JJA, Analysis - Forecast



950hPa V, JJA, Analysis

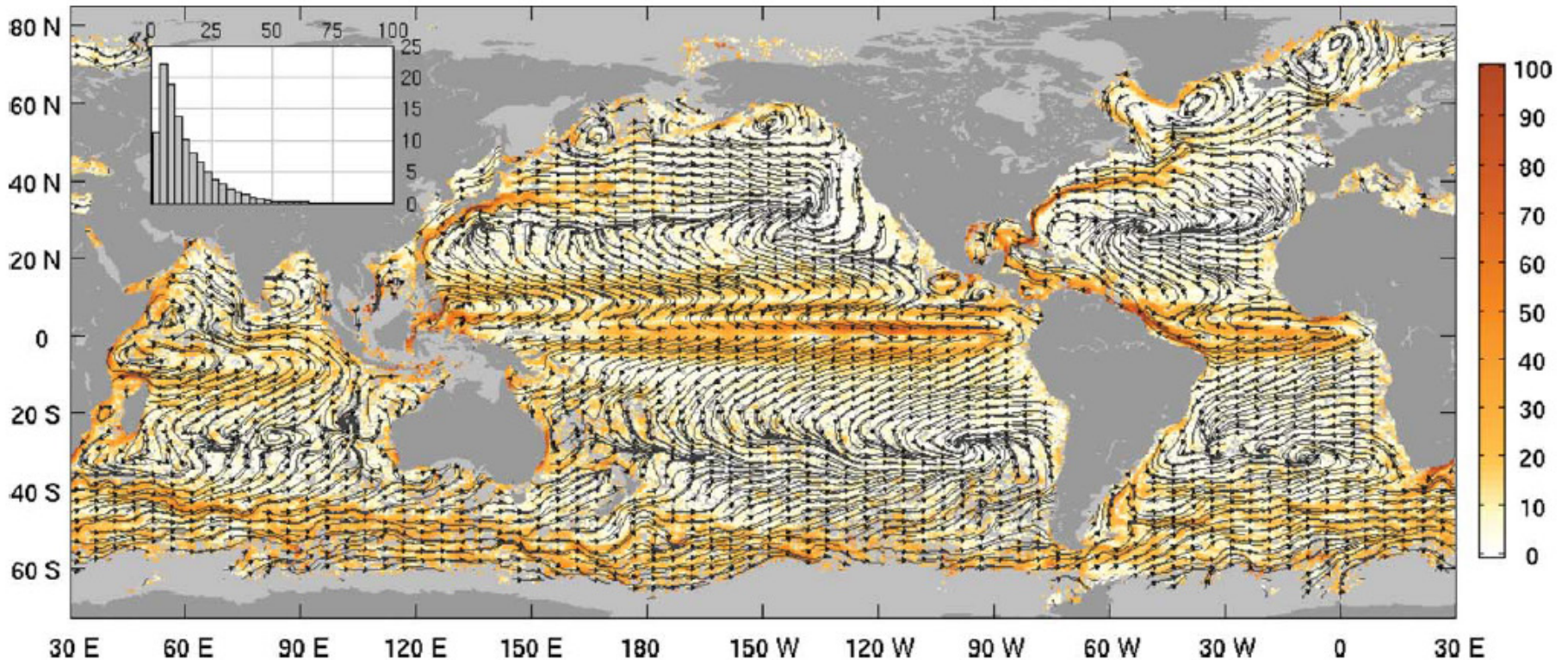


950hPa V, JJA, Analysis - Forecast



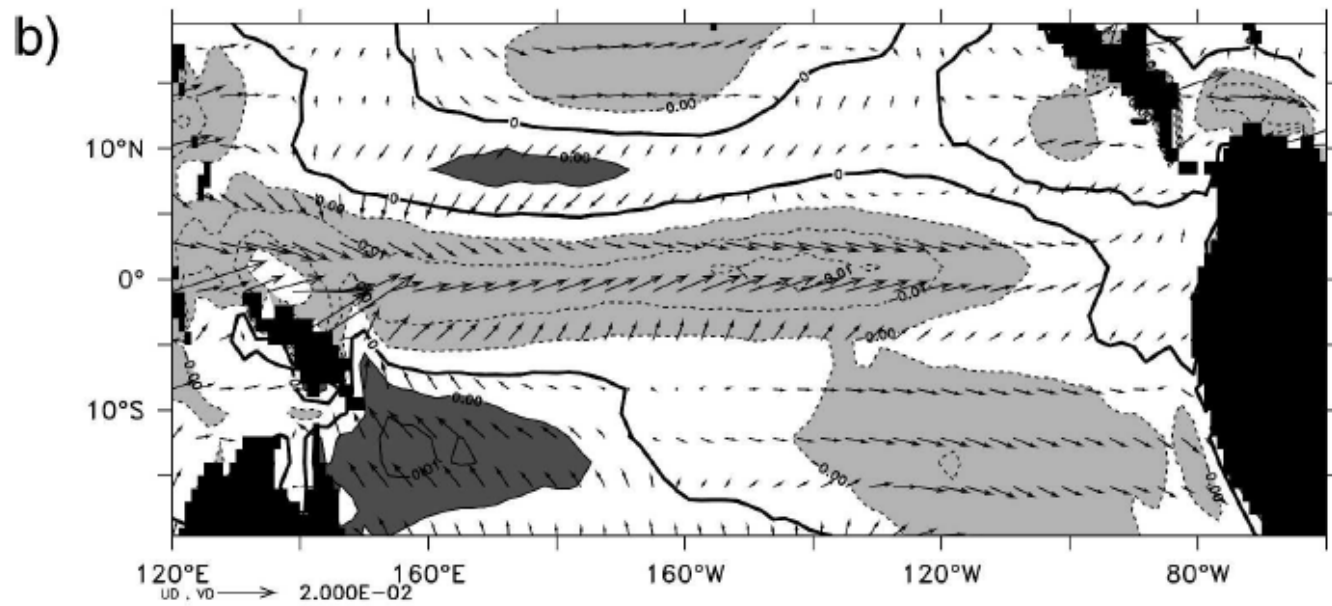
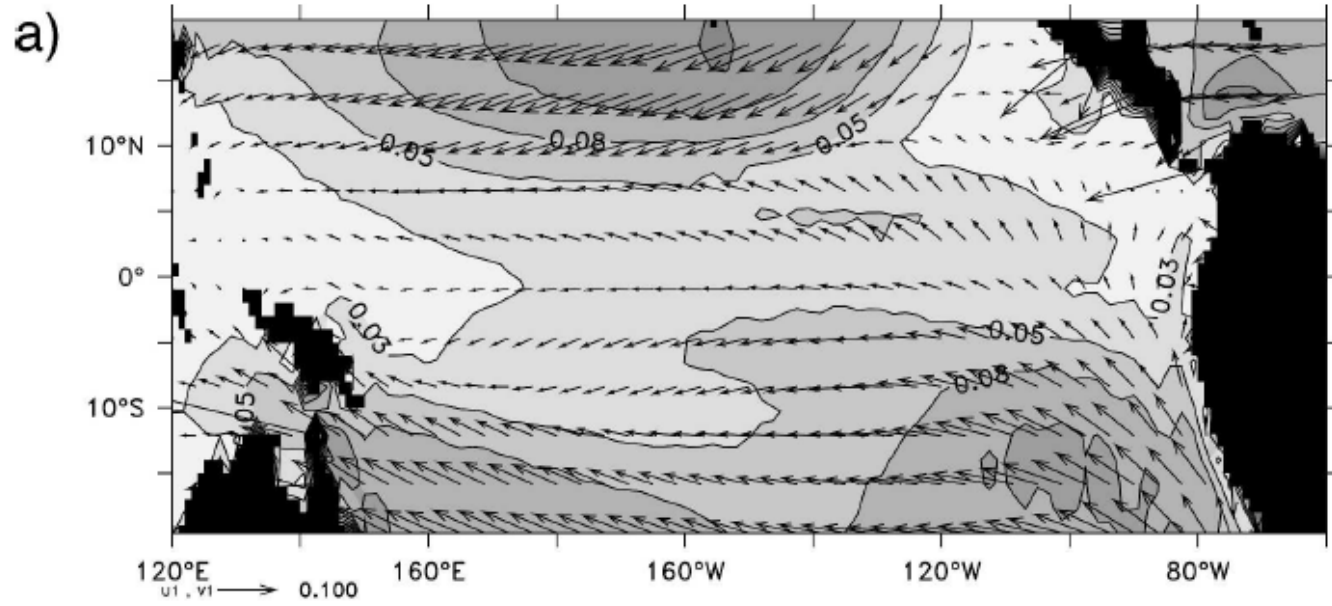


# Ocean Currents



**Figure 2.** Mean current speeds (colors, in  $\text{cm s}^{-1}$ ) from near-surface drifter data with streamlines (black lines). Streamlines are calculated from spatially smoothed currents to indicate flow direction and qualitatively illustrate large-scale circulation features, including surface divergence. Light gray areas have less than 10 drifter days per bin (0.8 per square degree). In addition, only bins with mean current speeds statistically different from zero at one standard error of the mean are shaded. Inset (top left) shows histogram of mean current speed ( $\text{cm s}^{-1}$ , horizontal axis, from 0 to 100 at  $3.125 \text{ cm s}^{-1}$  intervals) versus number of bins (in kilobins, vertical axis, from 0 to 25,000 bins).





All of these wind stress estimates rely on some formulation of the drag coefficient

$$\tau = \rho C_D \vec{v}_{10} |\vec{v}_{10}|$$

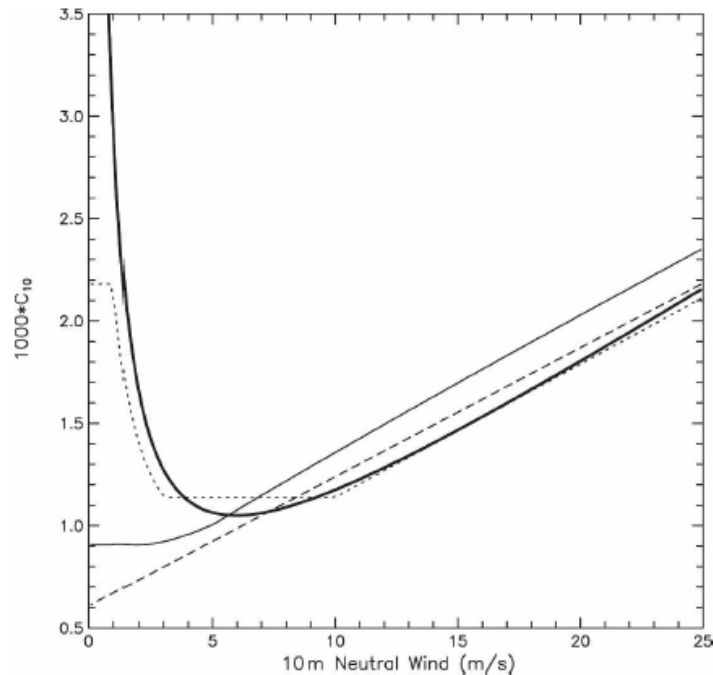
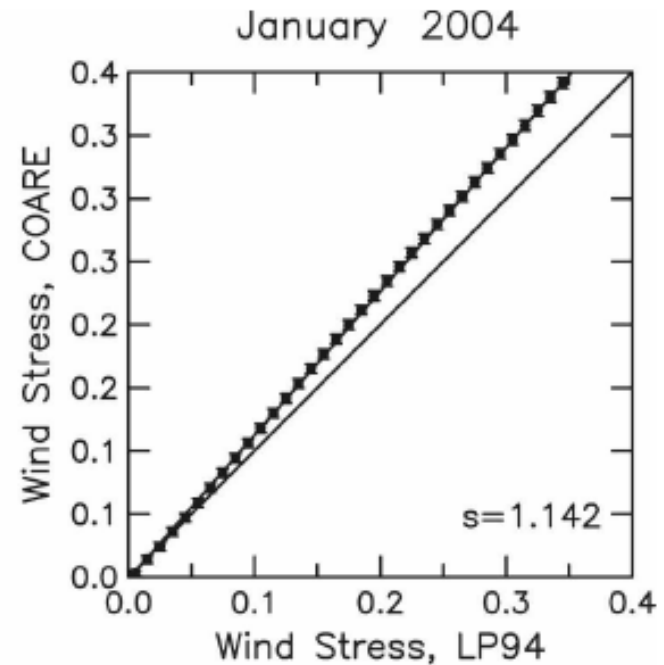
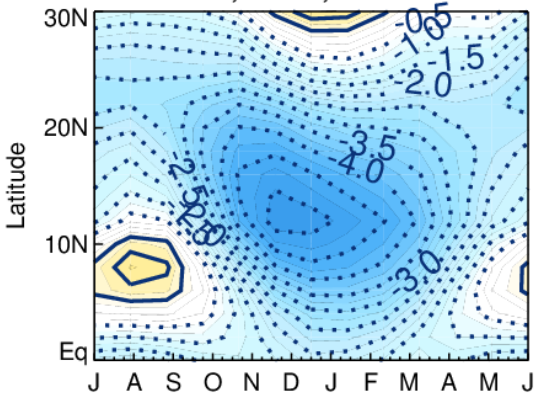


FIG. B1. The wind speed dependence of drag coefficients for neutrally stable conditions: the 1994 modified Large and Pond formulation described in the appendix of Large et al. (1994) (thick solid line); the 1990 modified Large and Pond formulation described by Trenberth et al. (1990) (dotted line); the Smith (1980) formulation (dashed line); and the COARE 3.0 formulation presented by Fairall et al. (2003) (thin solid line).

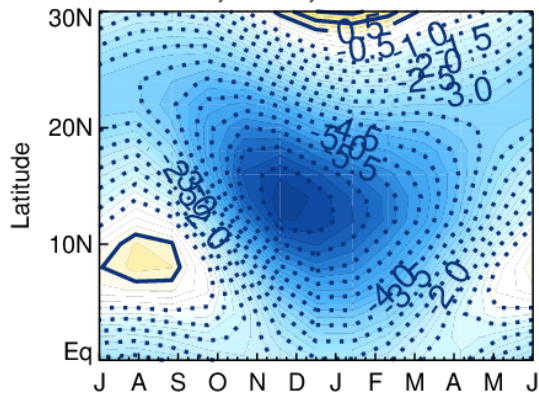


Risien and Chelton (2008)

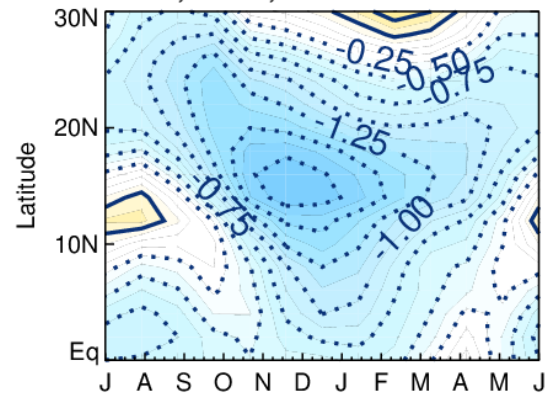
U, lev1, ERA



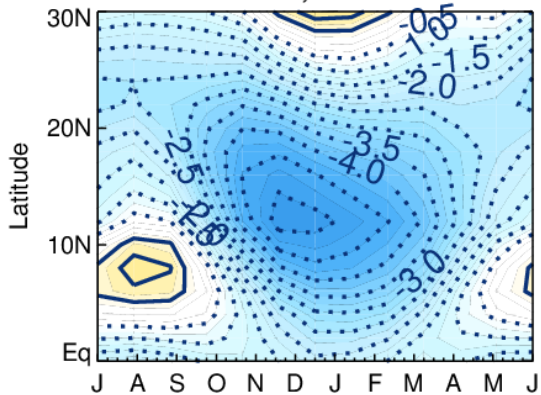
U, lev1, CMIP5



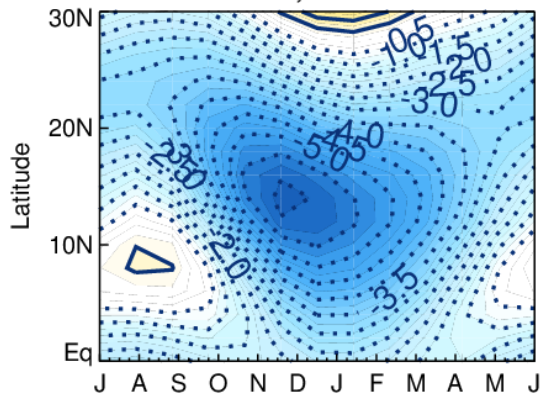
U, lev1, CMIP5-ERA



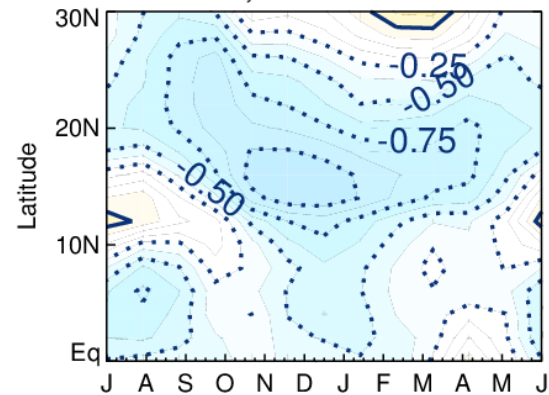
U10, ERA



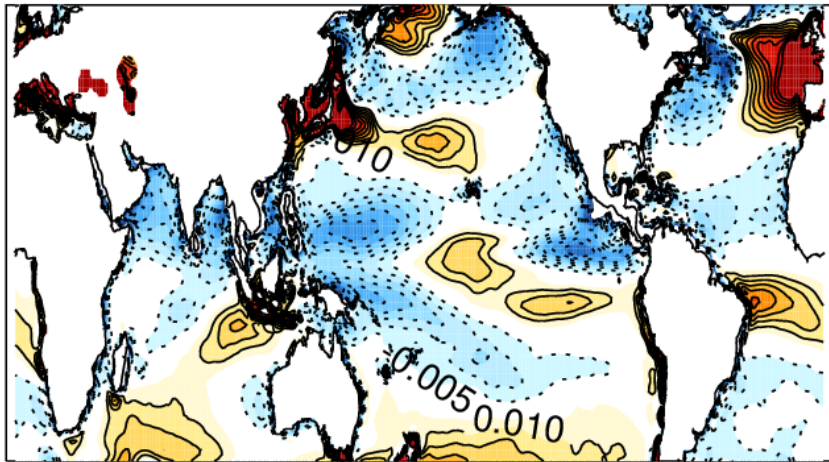
U10, CMIP



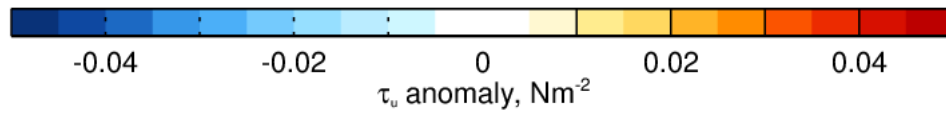
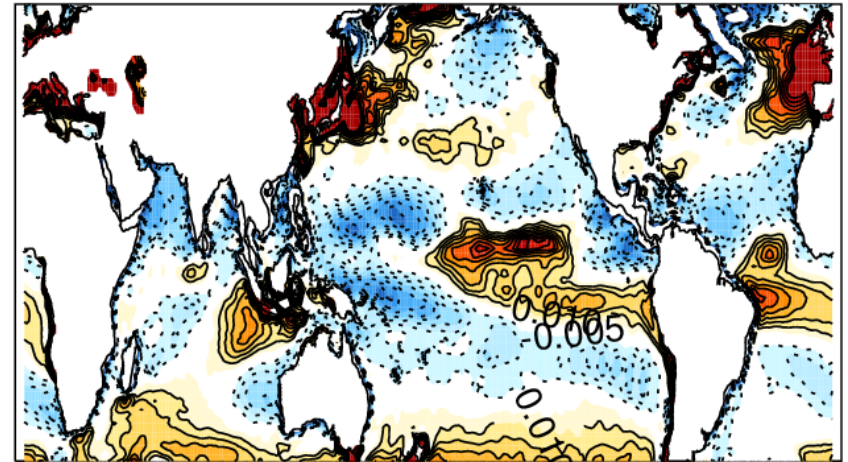
U10, CMIP - ERA



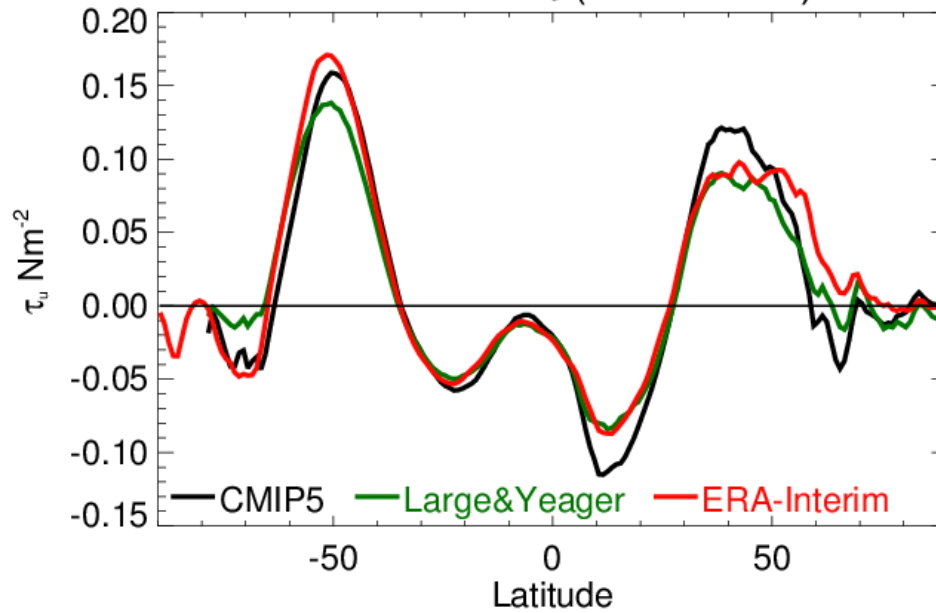
CMIP5 - ERA-Interim, DJF



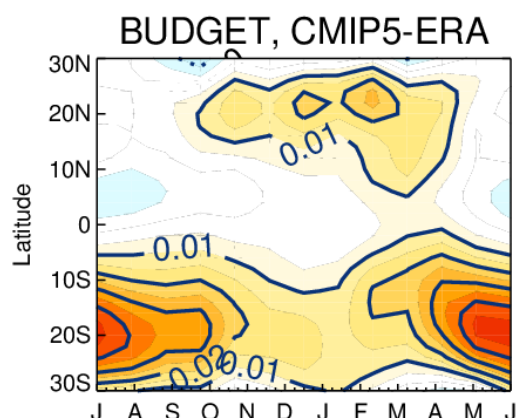
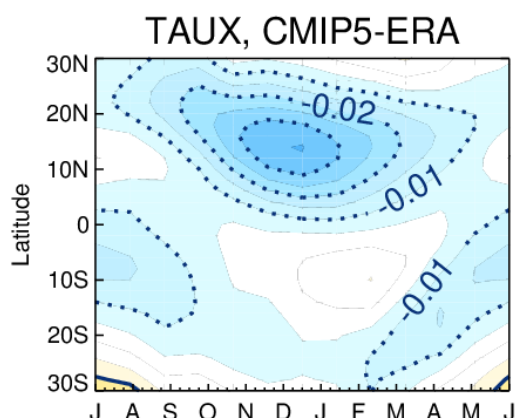
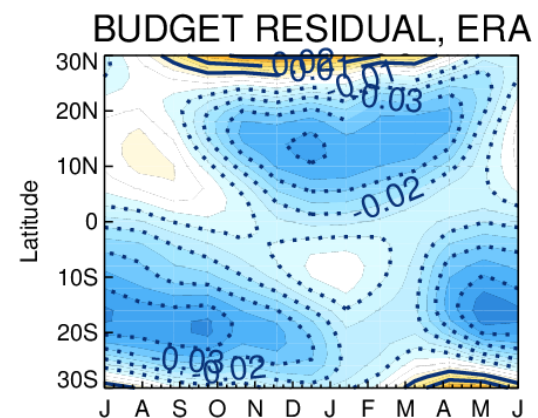
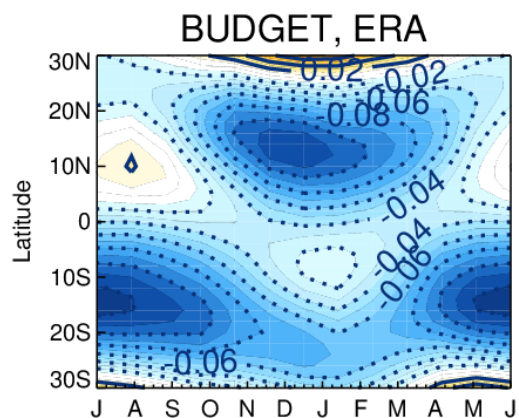
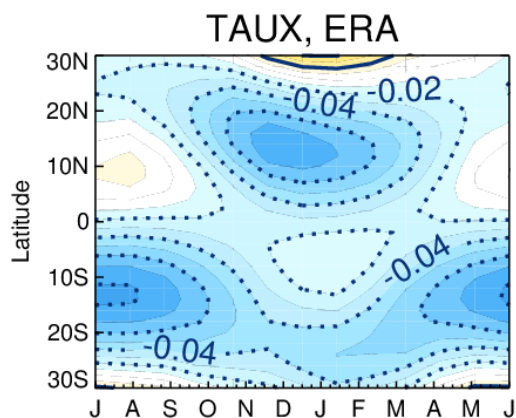
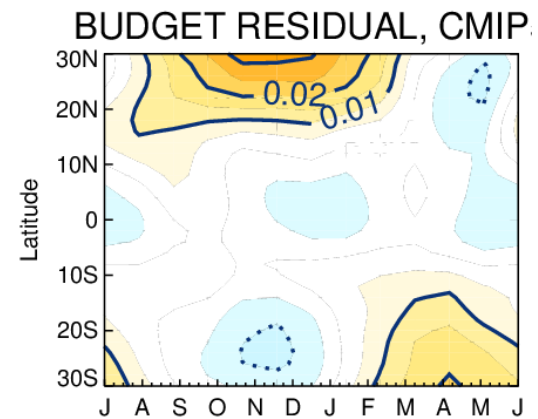
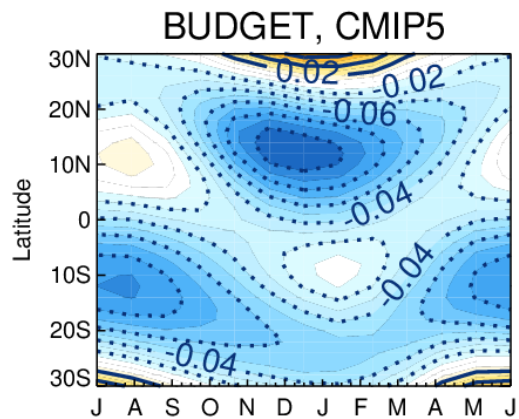
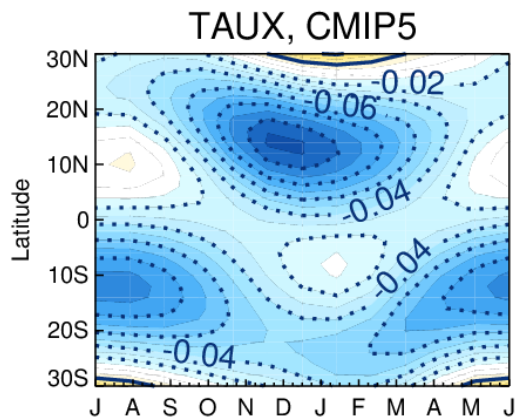
CMIP5 - Large&Yeager, DJF

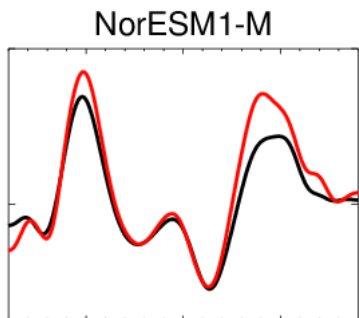
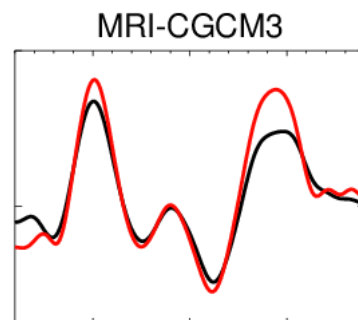
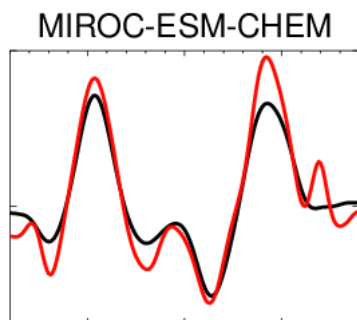
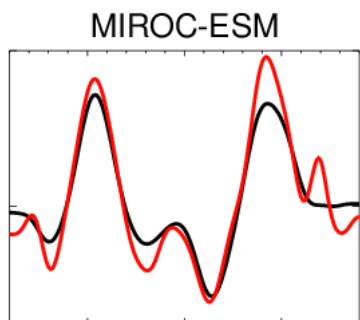
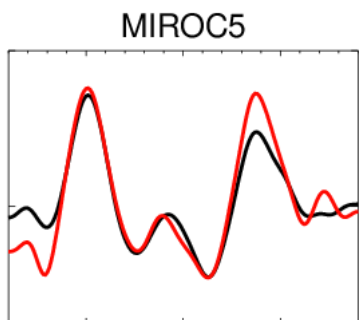
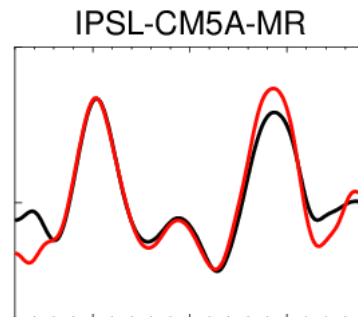
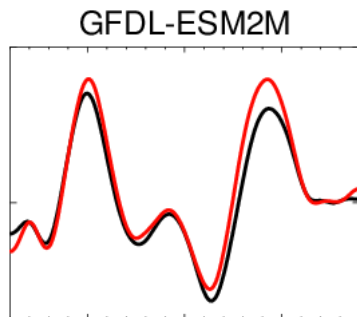
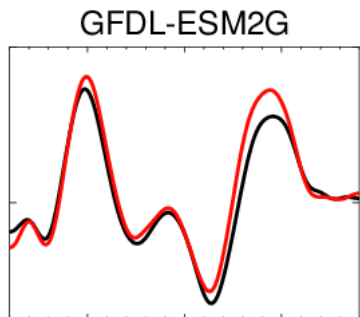
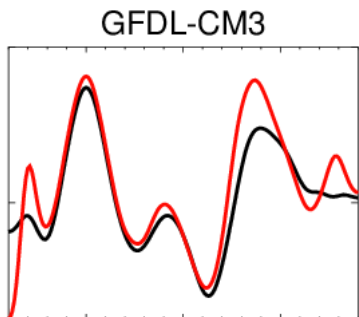
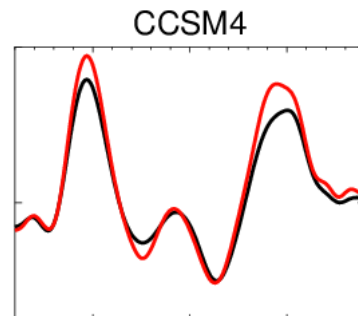
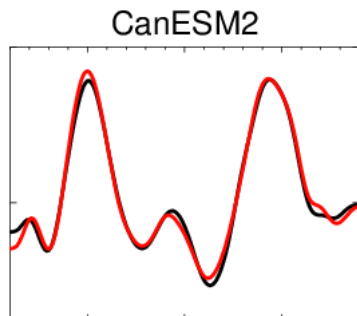
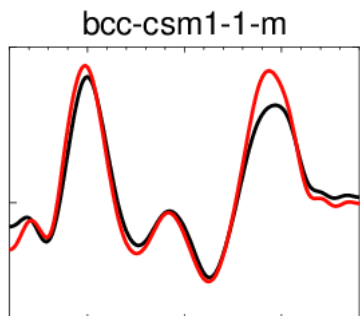
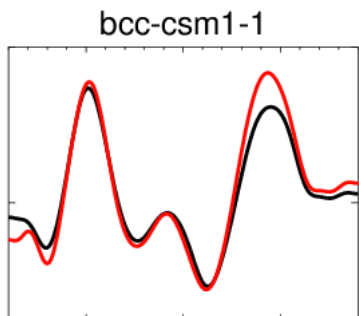


Zonal mean  $\tau_u$  (over ocean)



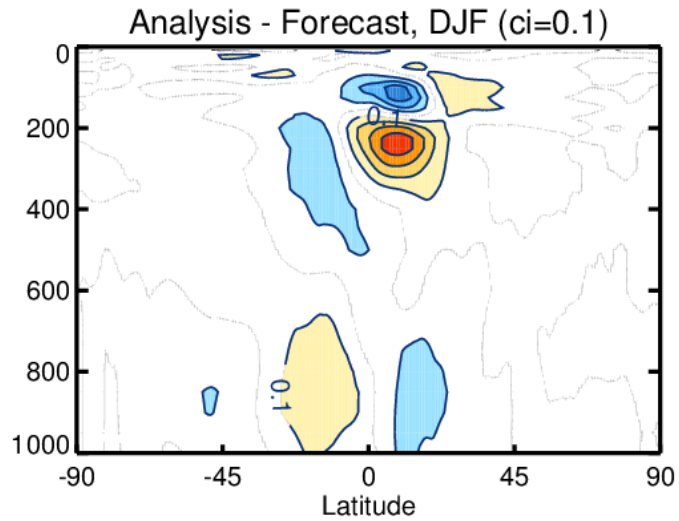




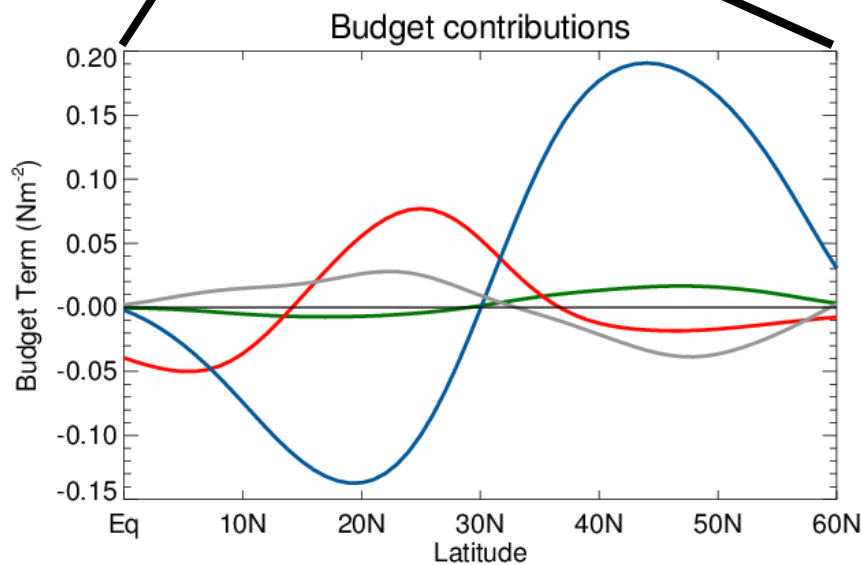
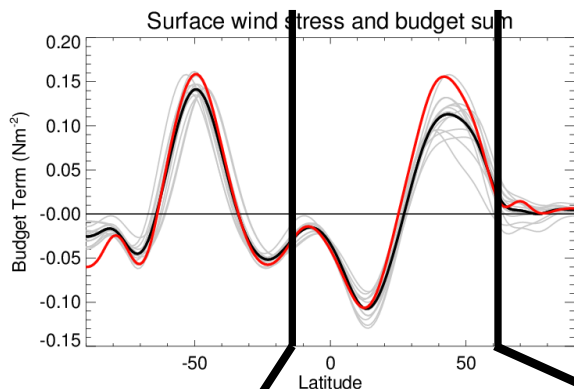


— Surface wind Stress  
— Sum of terms

# Seasonality of v Analysis - Forecast differences



# Contributors to the budget in the CMIP5 models



— Zonal mean advection

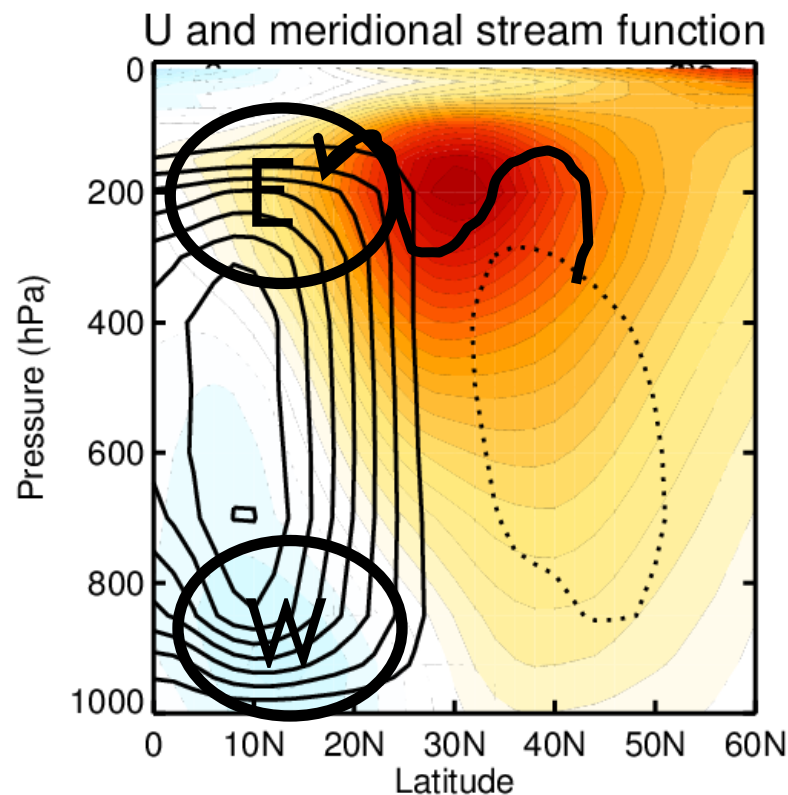
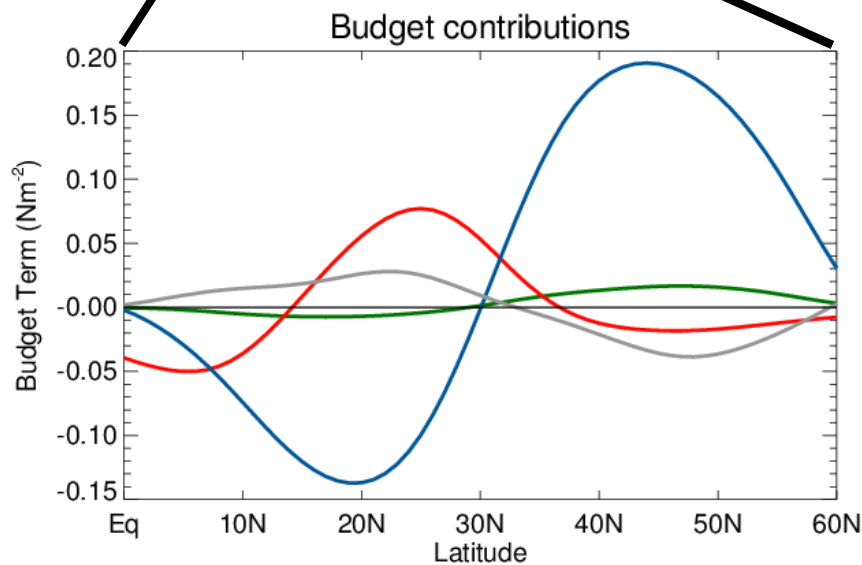
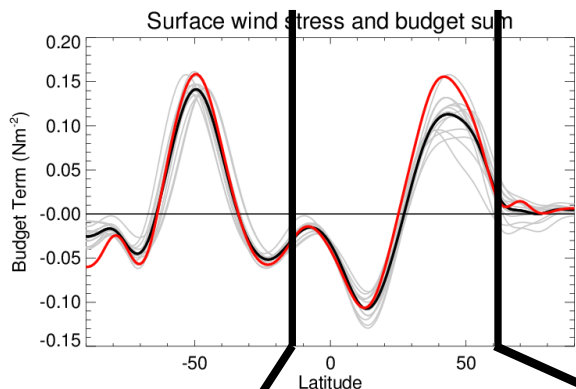
— Eddy momentum flux convergence

— Mountain Torque

— fv



# Contributors to the budget in the CMIP5 models



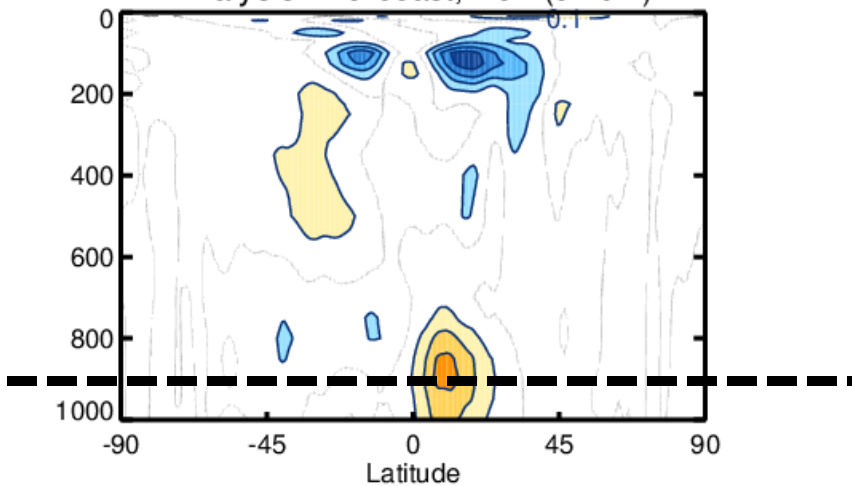
— Zonal mean advection

— Eddy momentum flux convergence

— Mountain Torque

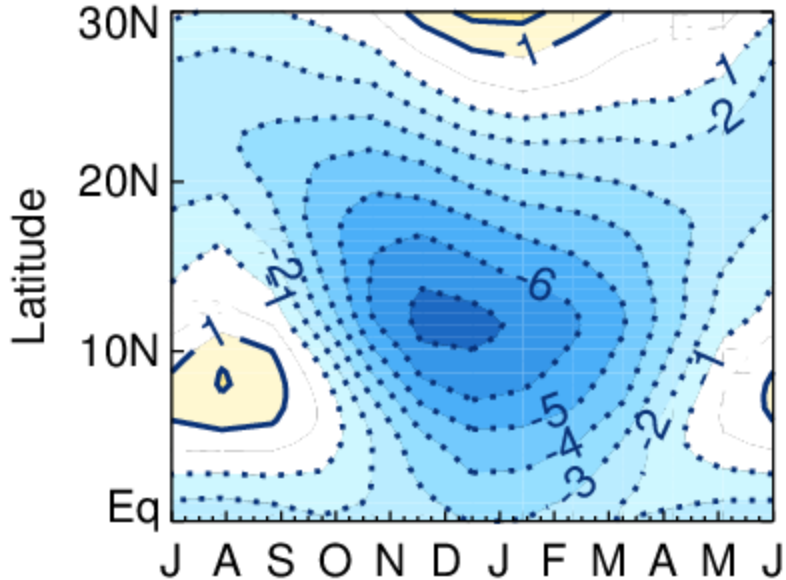
— fv

Analysis - Forecast, DJF (ci=0.1)

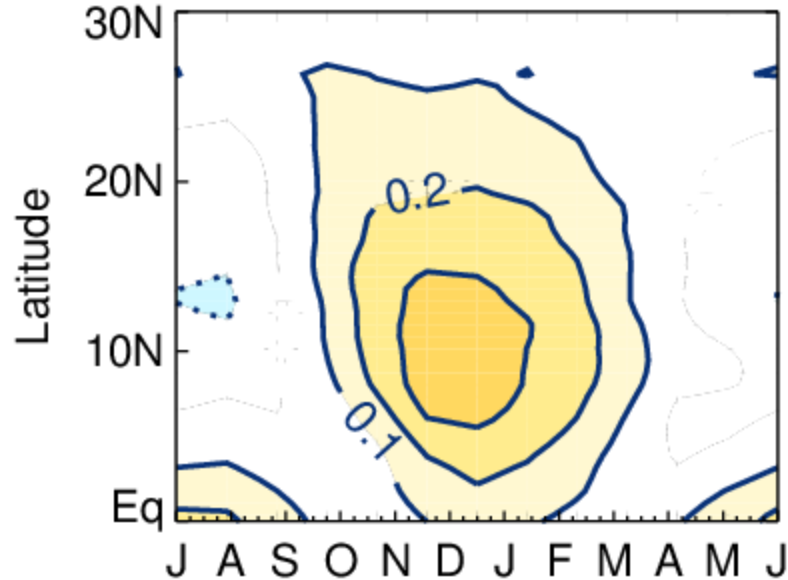


900hPa zonal  
mean zonal wind

ANALYSIS



ANALYSIS - FORECAST



$$\frac{\partial u}{\partial t} = fv + UV_{conv} + Z$$



← Expect

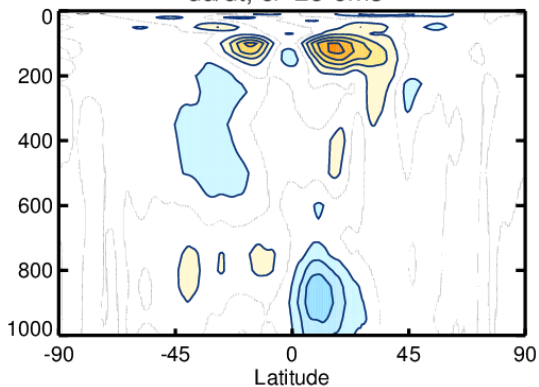
$$\frac{\partial u}{\partial t} - fv - UV_{conv} = Z$$



Forecast Evolution compared to Analysis Evolution = (Forecast - Analysis)

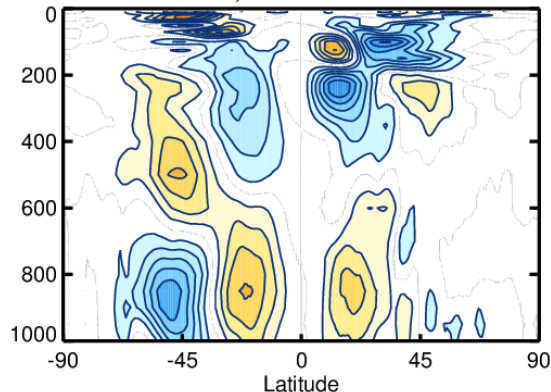
$$\frac{\partial u}{\partial t}$$

du/dt, ci=2e-6ms<sup>-1</sup>



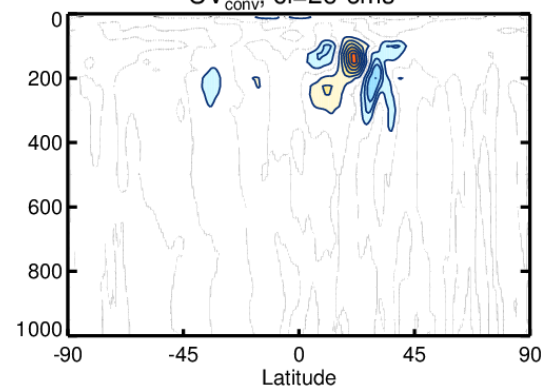
$$fv$$

fv, ci=2e-6ms<sup>-1</sup>



$$UV_{conv}$$

UV<sub>conv</sub>, ci=2e-6ms<sup>-1</sup>



$$\frac{\partial u}{\partial t} = fv + UV_{conv} + M + F_u + Z$$

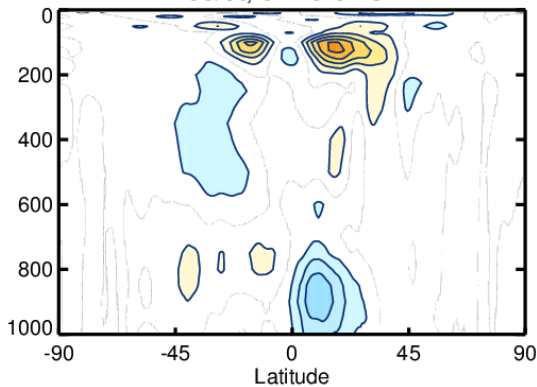
↑ **E**     ↑ **W**     ↑ **W**     ← Expect →     ↑ **E**

$$\underbrace{\frac{\partial u}{\partial t} - fv - UV_{conv} - M}_{\text{E}} = F_u + Z$$

Forecast Evolution compared to Analysis Evolution = (Forecast - Analysis)

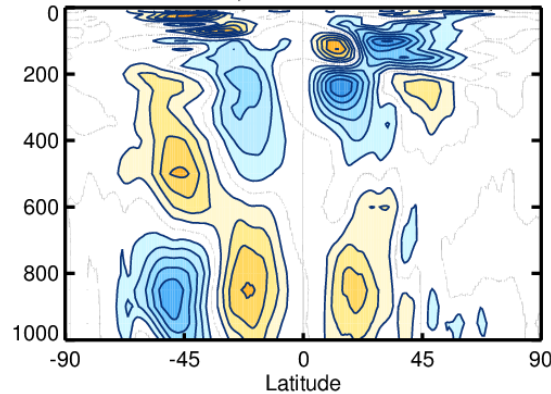
$$\frac{\partial u}{\partial t}$$

du/dt, ci=2e-6ms<sup>-1</sup>



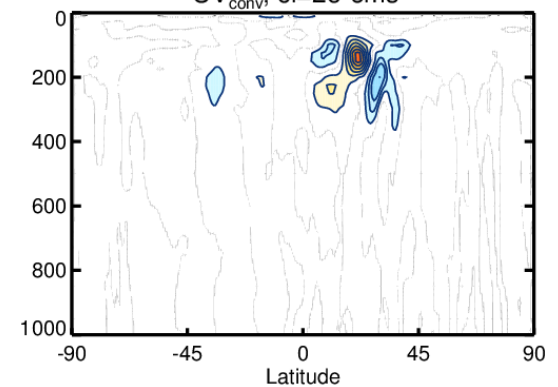
$$fv$$

fv, ci=2e-6ms<sup>-1</sup>



$$UV_{conv}$$

UV<sub>conv</sub>, ci=2e-6ms<sup>-1</sup>



$$\frac{\partial u}{\partial t} = f v + UV_{conv} + M + F_u + Z$$

$\frac{\partial u}{\partial t} - f v - UV_{conv} - M = F_u + Z$

← Expect →

Diagram illustrating the relationship between forecast and analysis evolution. The left side shows the full forecast equation with terms  $\frac{\partial u}{\partial t}$ ,  $f v$ ,  $UV_{conv}$ ,  $M$ ,  $F_u$ , and  $Z$ . The right side shows the analysis equation, which is the forecast equation minus the terms  $f v$ ,  $UV_{conv}$ , and  $M$ . A double-headed arrow labeled "Expect" points from the forecast equation to the analysis equation. Blue arrows labeled "E" point upwards from the  $\frac{\partial u}{\partial t}$  term in both equations. Red arrows labeled "W" point upwards from the  $f v$  and  $UV_{conv}$  terms in the forecast equation.

Forecast Evolution compared to Analysis Evolution = (Forecast - Analysis)

