

DYNAMIC SUB-GRID MODELLING OF AN EVOLVING CBL AT GREY-ZONE RESOLUTIONS

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Modelling **GREY** zone **B**oundary **L**ayers
(**GREYBLS**)

Motivation

- Numerical Weather Prediction at $O(100\text{m})$ is now possible
- Dominant turbulence length scales $\sim z_i$ (100 m – 3 km)
- Boundary Layer (BL) turbulence becomes partially resolved

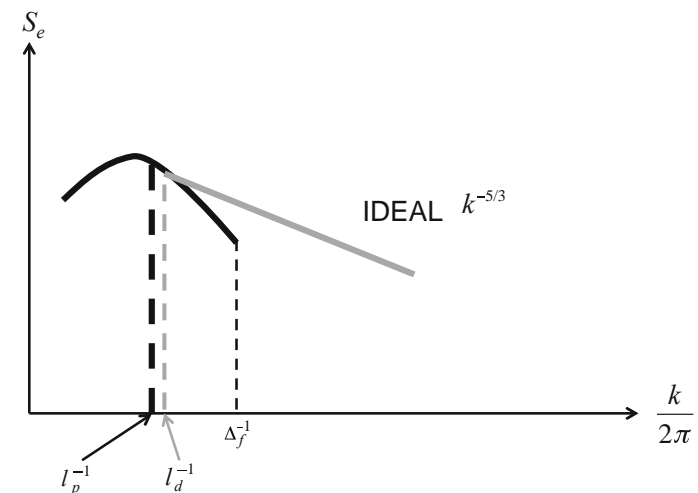
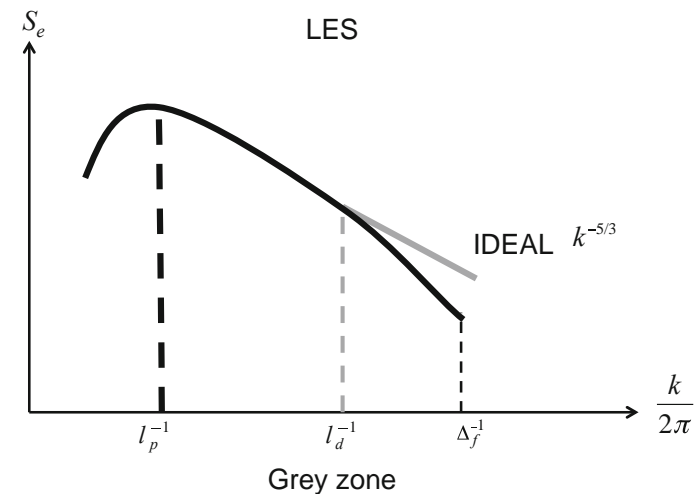
How do we parametrize sub-grid processes in the BL grey-zone?

Spectral view of the grey-zone (Beare, 2014)

- **LES** : Resolved field - scales for production (l_p) and dissipation (l_d) of TKE are well separated
- **Grey zone** : Dissipation has an impact on TKE production – Partially resolved field

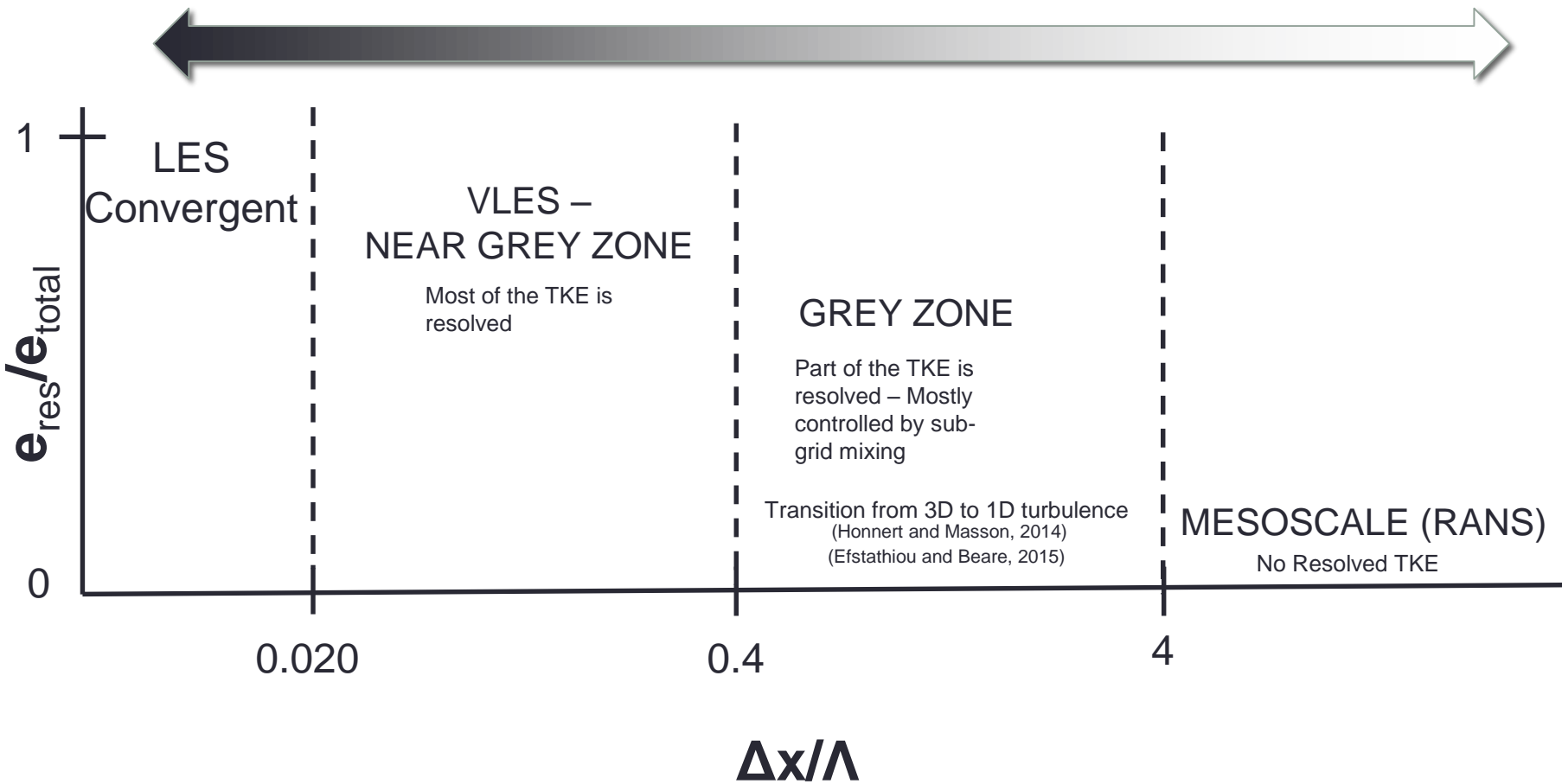
A working definition for the grey-zone

$$\frac{z_i}{l_d} < 0.7$$



(Beare, 2014)

Scales



(Sullivan and Patton, 2011)

(Beare, 2014)

Research Tools

- Numerical simulations with the LEM (Large-Eddy Met Office Model)
 - Quasi-steady state CBL ($z_i=1000$ m)
 - Evolving CBL (Wangara case study)
 - A range of horizontal resolutions (LES-Greyzone-Mesoscale)
- Compare with filtered LES
- Smagorinsky type eddy-viscosity model

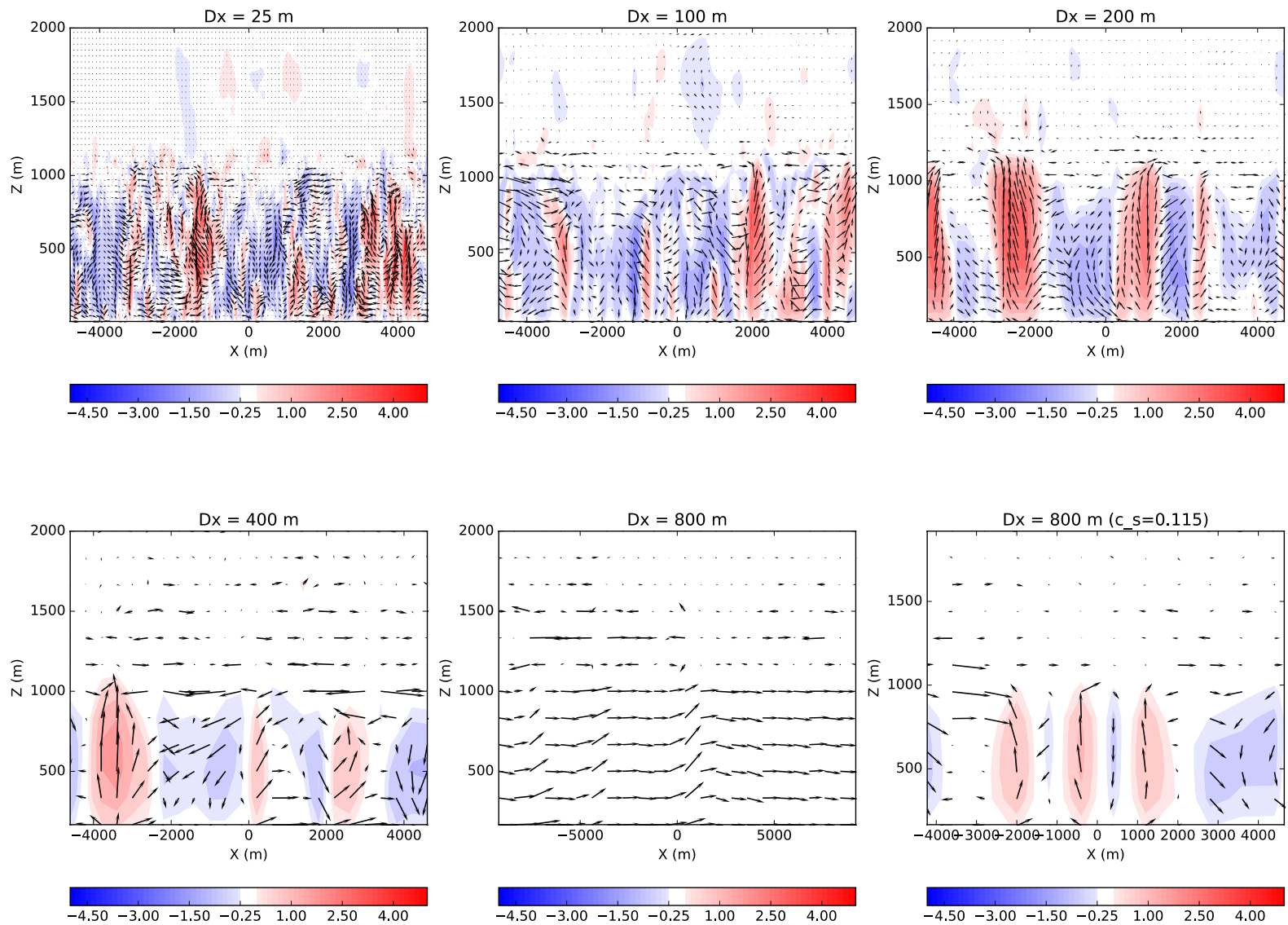
$$K_{M,H} = l^2 S f_{M,H} (Ri)$$

$$l^2 = (k z)^{-2} + \lambda_0^{-2}$$

$$\lambda_0 = c_s \Delta x$$

Control : $c_s = 0.23$

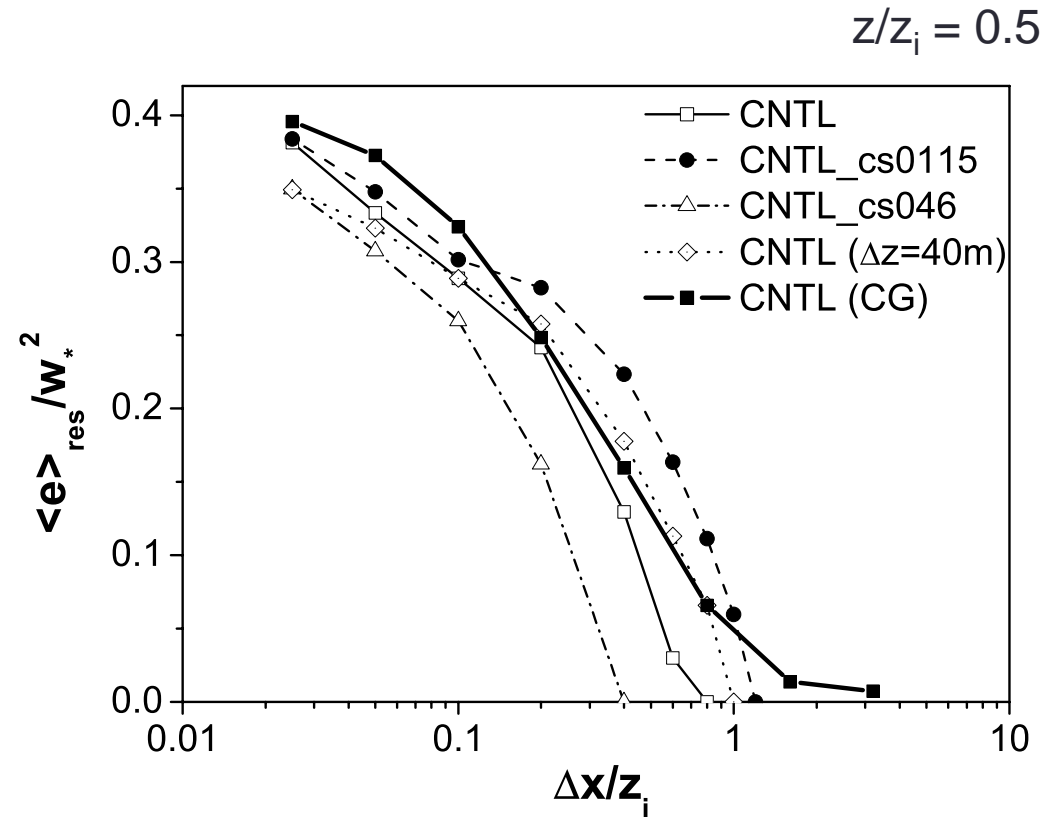
Steady State Simulations (Free Convection)



Quantifying sub-grid diffusion in the grey-zone

- Reducing sub-grid diffusion ?
- Increasing vertical resolution ?

How much resolved TKE?

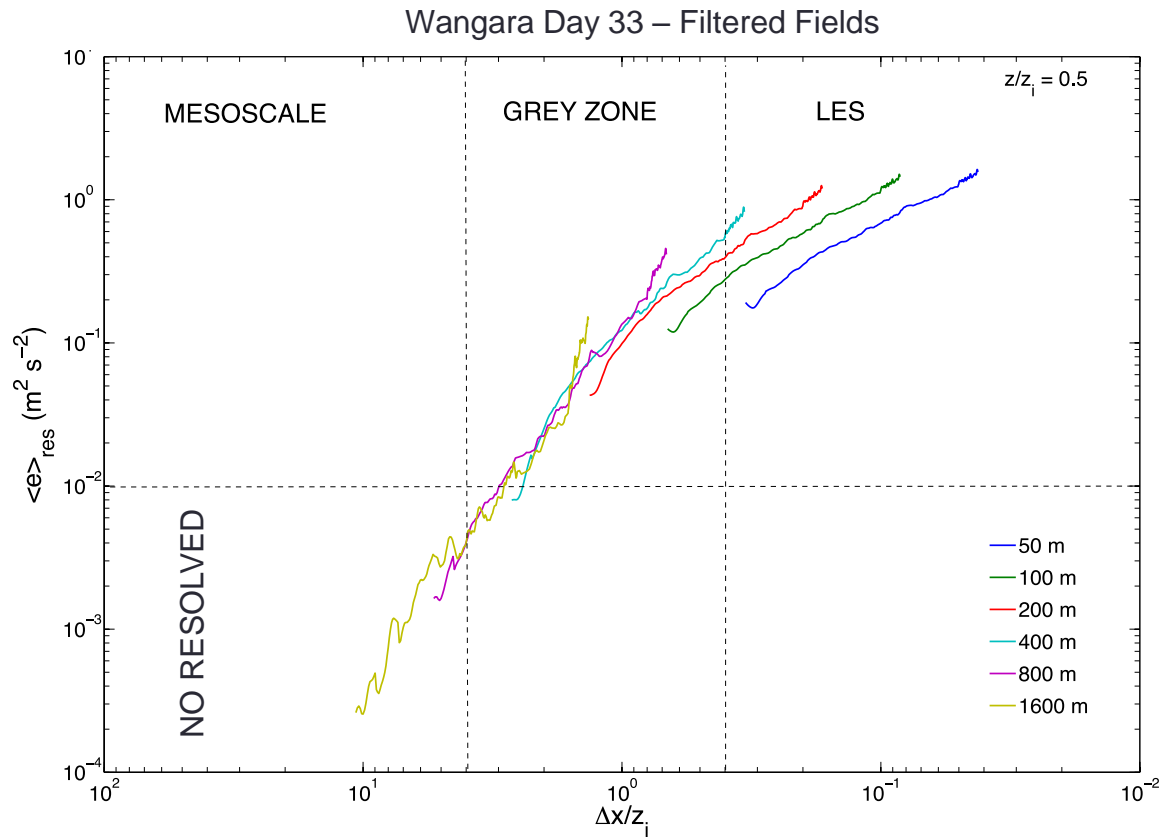


(Efstathiou and Beare, 2015)

Parametrization approaches

- Modifying Smagorinsky
 - BOUND approach (Efstathiou and Beare, 2015)
 - Dynamic Smagorinsky Modelling
 - Dynamic Blending (Preliminary results)

Evolution of Scales – Wangara CBL



During the morning CBL development simulations of different Δx go through different regimes

(Efstathiou et al., 2016)

Dynamic sub-grid modelling

- Using “resolved” scales to estimate C_S
- Apply a test filter ($G_{\alpha\Delta}$) to diagnose sub-filter scales

$$\tau_{ij} = -2(C_s\Delta)^2 |\bar{S}| \bar{S}_{ij} f(Ri)$$

τ : sub-grid stress

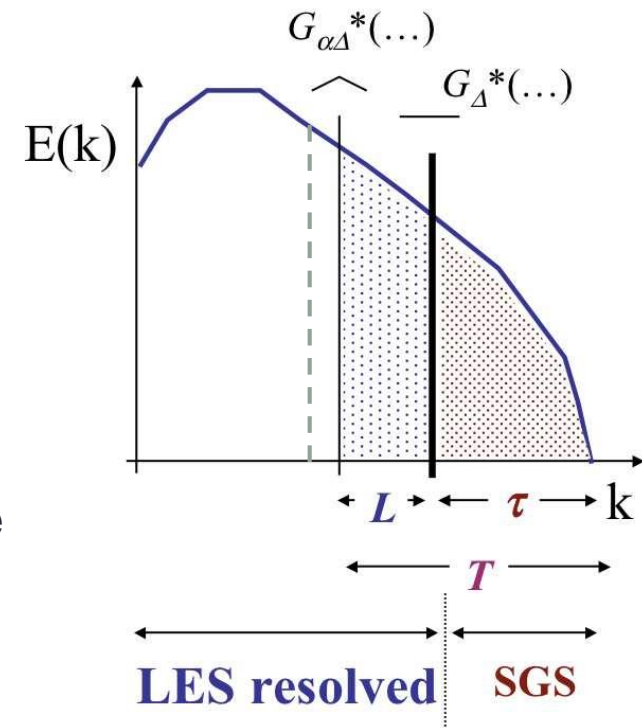
T : interactions between sub-grid - sub-filter

L : “smallest” resolved scales (Leonard stress)

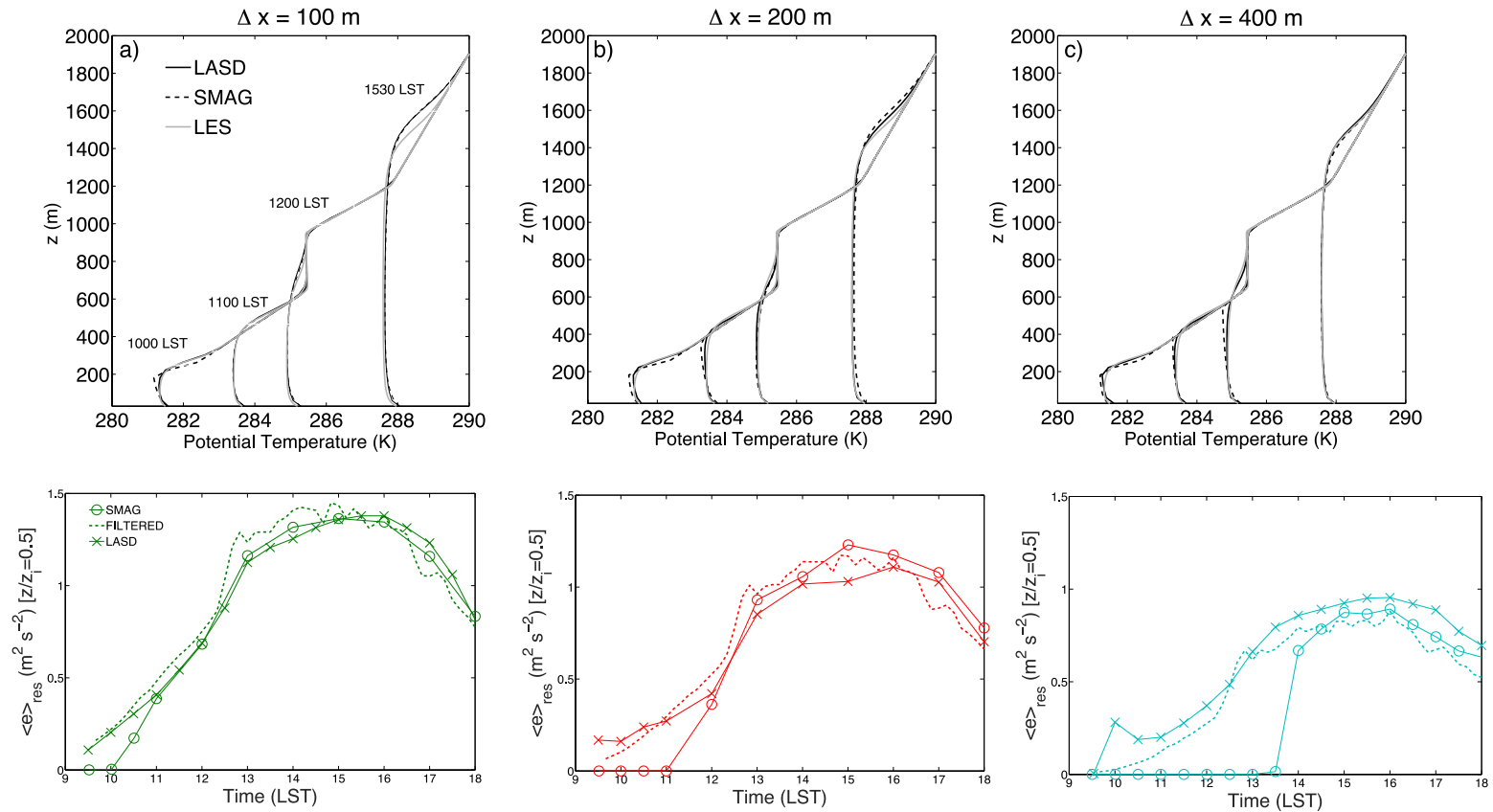
C_S averaged over path lines (LASD)

Second filter ($G_{2\alpha\Delta}$) to account for scale dependence

$$C_S(\Delta) \neq C_S(a\Delta)$$

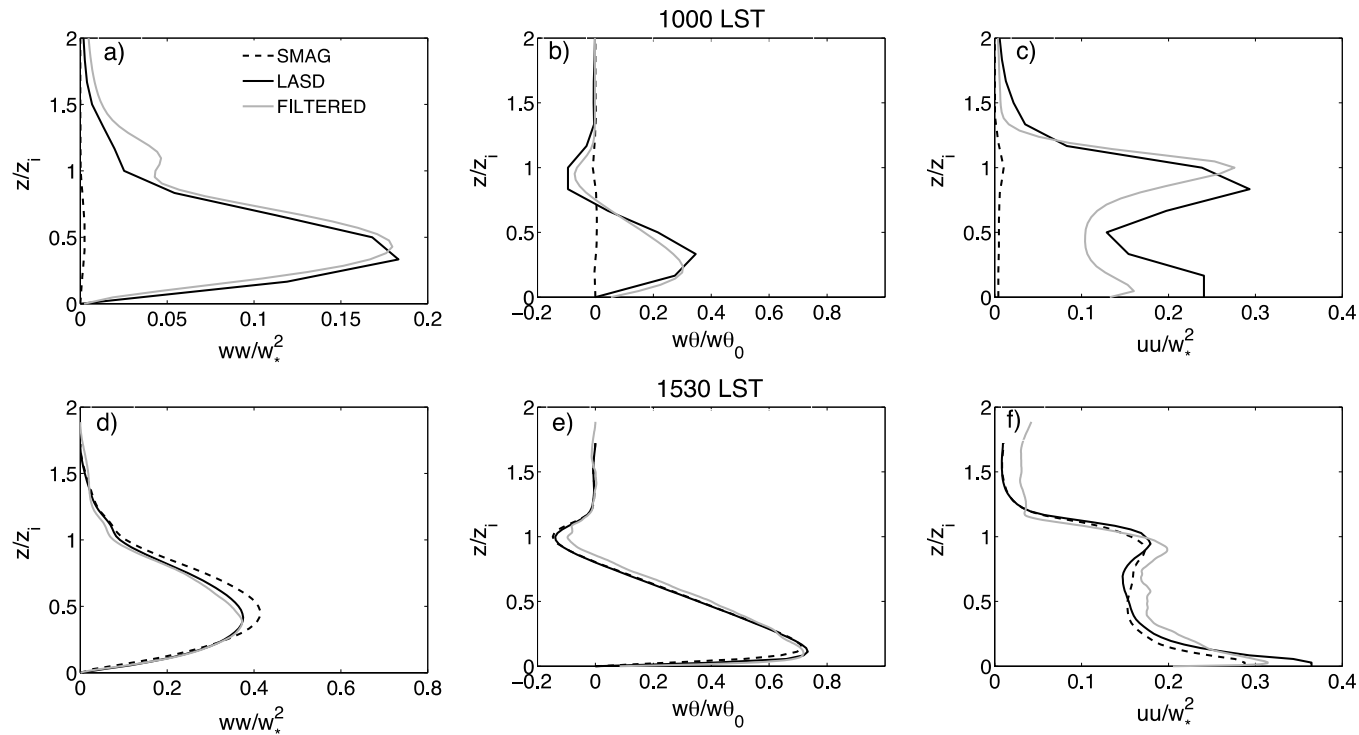


Wangara CBL development



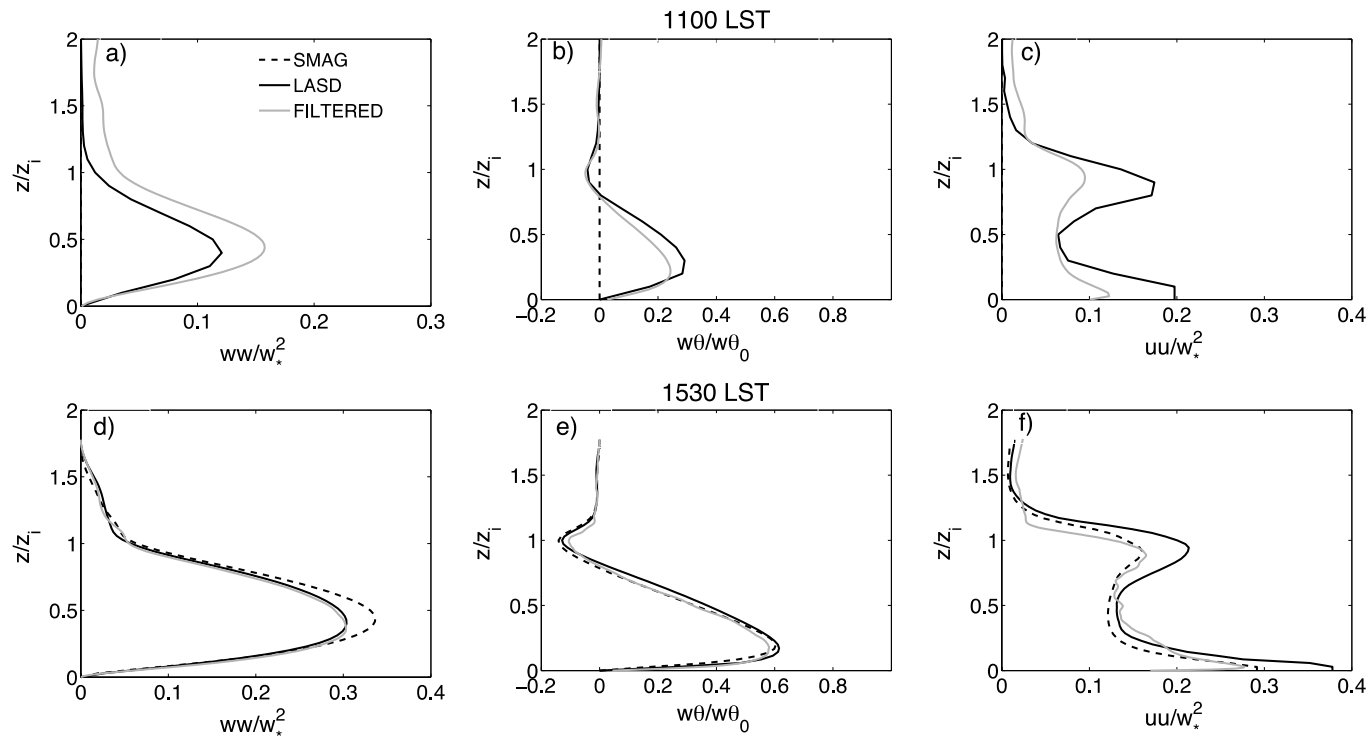
Comparison with the filtered fields

$\Delta x = 100$ m



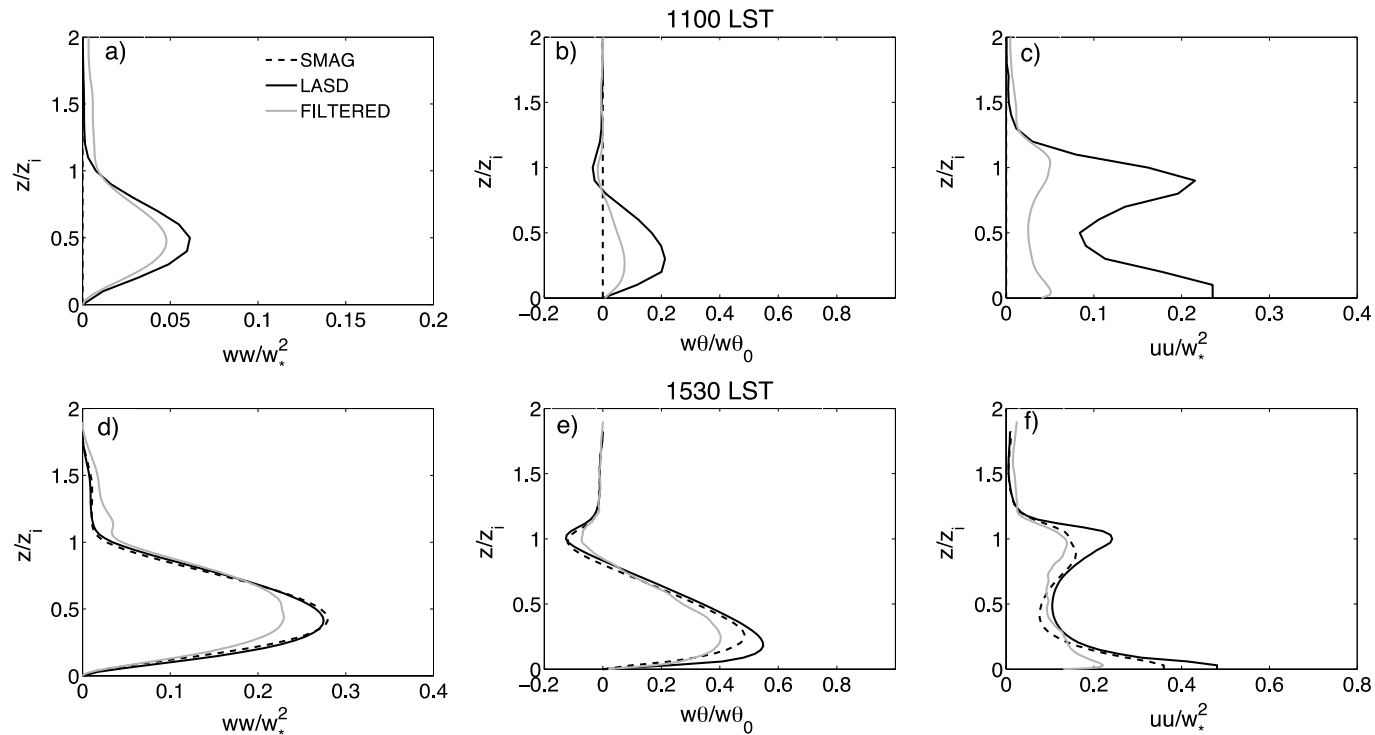
Comparison with the filtered fields

$\Delta x = 200$ m



Comparison with the filtered fields

$\Delta x = 400$ m



Met Office Blending Scheme

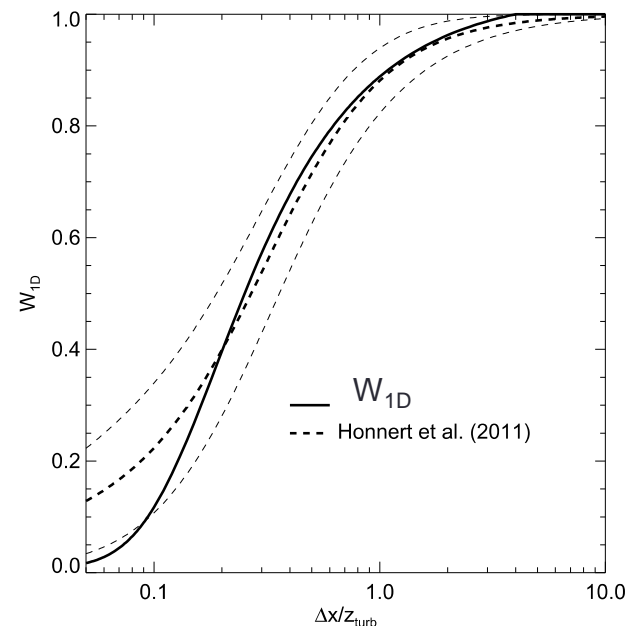
- Blending Scheme (Boutle et al., 2014)
- Implemented in the LEM (Efstathiou et al., 2016)

(based on Hong et al., 2006)

$$\overline{u'_j \theta'} = \overbrace{-K_H \frac{\partial \theta}{\partial x_j}}^{\text{local flux}} + \delta_{3j} W_{1D} \left[\overbrace{K_H \gamma}^{\text{non-local flux}} + \overbrace{\overline{w' \theta'}_{z_h} \left(\frac{z}{z_h} \right)^n}^{\text{explicit entrainment}} \right]$$

$$K_H = \max [W_{1D} K_H(1D), K_H(\text{SMAG})]$$

$$W_{1D} = 1 - \tanh\left(\beta \frac{z_{\text{turb}}}{\Delta x}\right) \max\left(0, 1 - \frac{\Delta x}{4z_{\text{turb}}}\right)$$



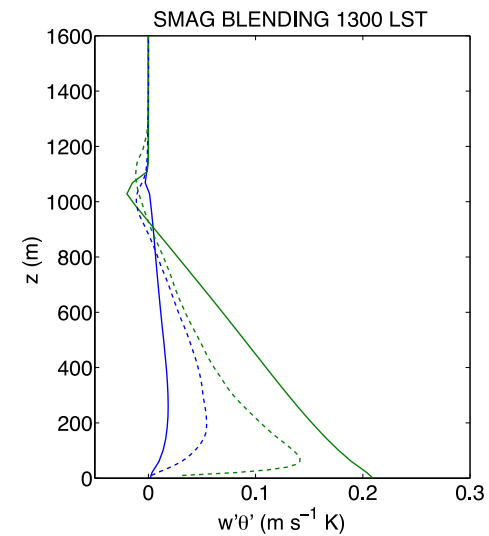
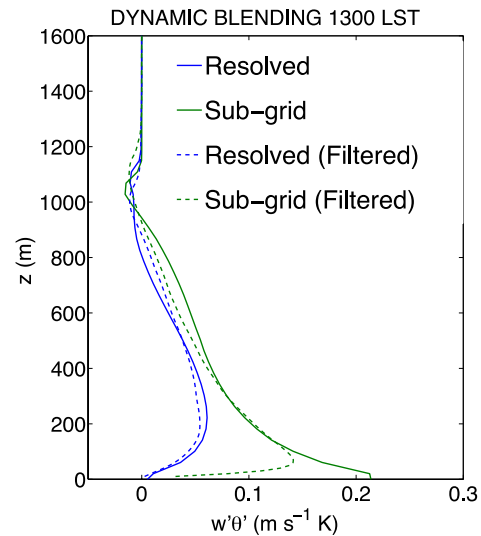
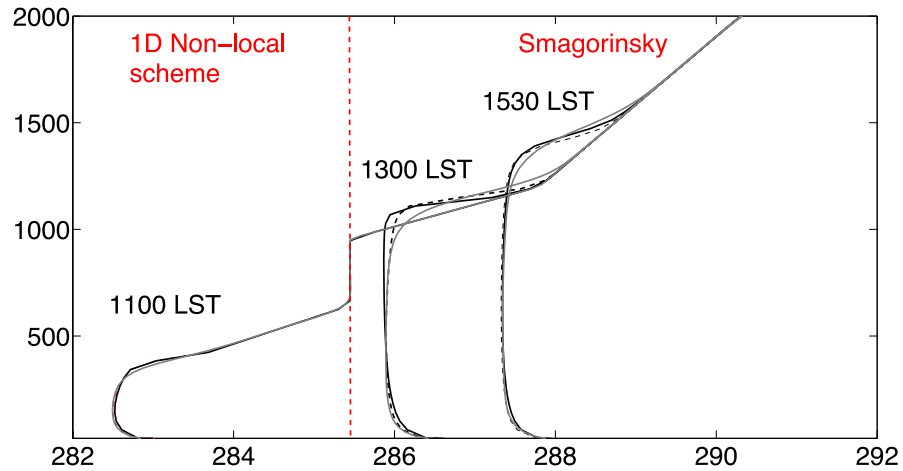
SMAG

1D BL

Wangara CBL development

$\Delta x = 400$ m

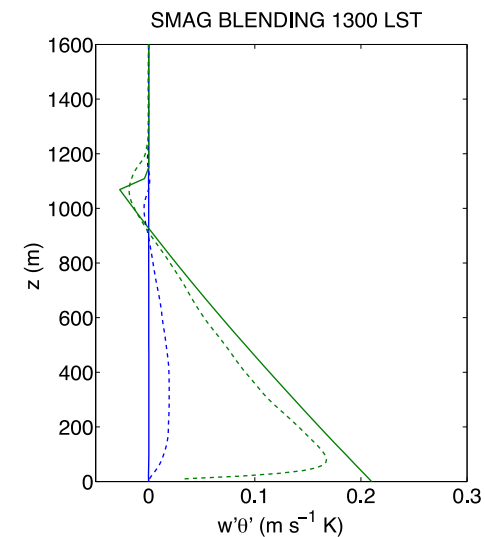
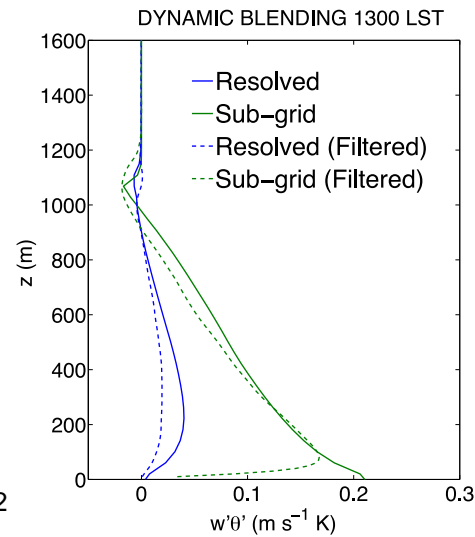
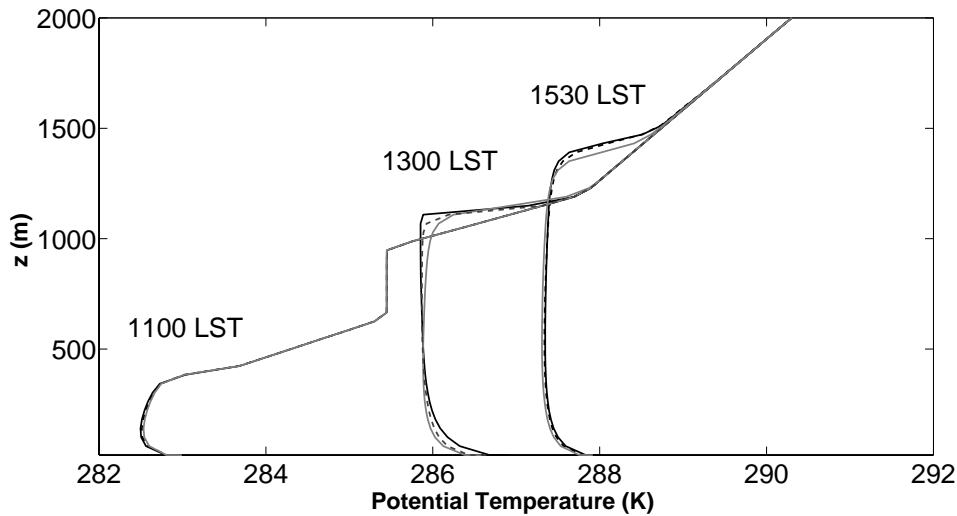
— SMAG BLEND
 - - - LASD BLEND
 — LES



Wangara CBL development

$\Delta x = 800$ m

— SMAG BLEND
- - - LASD BLEND
⋯ LES



Summary

- *The grey-zone imposes practical limitations in very high resolution NWP*
 - **Should any convective overturning be allowed in the grey-zone?**
- **Challenges**
 - Representing coherent structures
 - Quantify the resolved TKE – Energetics – TKE spin-up
 - Form of transition
 - Shape and form of the coherent structures in the CBL would affect the representation of shallow Cu convection
 - Implications with deep convection and convective parametrizations
- **Dynamic modelling of sub-grid diffusion at grey-zone resolutions**
 - Dynamic Smagorinsky a better alternative than Standard Smagorinsky
 - Improves spin-up / Representation of mean quantities and turbulence statistics
 - Relies on dynamics (unable to resolve for $\Delta x/z_i > 2$) – Usability limit
 - Modified 1D schemes suffer from delayed spin-up
 - Dynamic Blending extends the benefits of dynamic modelling further into the grey-zone

Papers

- Beare, R. J., 2014: A length scale defining partially-resolved boundary-layer turbulence simulations. *Boundary-Layer Meteorol.* 151: 39–55.
- Efstathiou, G. A. and R. J. Beare, 2015: Quantifying and improving sub-grid diffusion in the boundary-layer grey zone. *Quarterly Journal of the Royal Meteorological Society*, 141, 3006–3017.
- Efstathiou, G. A., R. J. Beare, S. Osborne, A. P. Lock, 2016: Grey zone simulations of the morning convective boundary layer development, *Journal of Geophysical Research: Atmospheres*, 121, 9
- Efstathiou, G. A., Plant R. S., and M. M. Bopape, 2017: Simulation of an evolving convective boundary layer using a scale-dependent dynamic Smagorinsky model at near grey-zone resolutions. *Journal of Applied Meteorology and Climatology*, submitted.